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Macroeconomic Dynamics and Reallocation in an Epidemic*

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Abstract

In this paper we argue that endogenous shifts in private consumption behavior across sectors of the economy can act as a potent mitigation mechanism during an epidemic or when the economy is reopened after a temporary lockdown. Extending the theoretical framework proposed by Eichenbaum-Rebelo-Trabandt (2020), we distinguish goods by their degree to which they can be consumed at home rather than in a social (and thus possibly contagious) context. We demonstrate that, within the model the “Swedish solution” of letting the epidemic play out without government intervention and allowing agents to shift their sectoral behavior on their own can lead to a substantial mitigation of the economic and human costs of the COVID-19 crisis, avoiding more than 80 of the decline in output and of number of deaths within one year, compared to a model in which sectors are assumed to be homogeneous. For different parameter configurations that capture the additional social distancing and hygiene activities individuals might engage in voluntarily, we show that infections may decline entirely on their own, simply due to the individually rational re-allocation of economic activity: the curve not only just flattens, it gets reversed.

Keywords: Epidemic, Coronavirus, Macroeconomics, Sectoral Substitution

JEL classification: E52, E30

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1 Introduction

The COVID-19 pandemic of 2020 has the world in its grip. Policy makers must wrestle with a serious trade-off: how much economic activity should one allow, possibly risking hundreds of thousands additional deaths as a result? Our paper contributes to the quickly growing literature of understanding this trade-off. Our specific focus is on the question how people can deal with that trade-off on their own already: how much will each individual seek to mitigate economic interactions that carry the risk of infection, given the potentially disastrous consequences for their health?

Our starting point is a simple macroeconomic model, where agents consume and work, combined with a SIR (“Susceptible-Infected-Recovered”) model standard in the epidemiology literature. Our analysis is inspired by and shares many features with the model of [Eichenbaum et al. \(2020\)](#), ERT for short from now on. As in their model infections can occur in the market place by consuming together or working together. We also share with these authors, that participating agents are aware of the resulting infection- and death-risks, and thus may alter their consumption and work patterns as the epidemic unfolds, but do not take into account the externality of their behavior on the infection risks of others. Like them, we view the endogenous response in behaviour of people, motivated by their own interest in preserving their health and avoiding the possibility of dying, as key in understanding the spread of a pandemic and, ultimately, its economic costs, a significant advance from the purely epidemiological models beautifully summarized in [Atkeson \(2020\)](#).

We depart from ERT in one crucial dimension, however. In contrast to them we assume the economy is composed of several heterogeneous sectors that differ technologically in their infection probabilities. There are two interpretations of this assumption. One is, that very similar goods can be consumed in privacy at home (Pizza delivery) rather than in the market place (Pizza restaurant). Likewise, very similar work may be performed remotely rather than in an office, e.g. writing a report online at home rather than in the community of co-workers. [Leibovici et al. \(2020\)](#) provide evidence for very substantial heterogeneity across sectors of the U.S. in the degree of social interaction to facilitate the production of goods and services, and [Dingel and Neimann \(2020\)](#) as well as [Mongey and Weinberg \(2020\)](#) assess what share of jobs can be performed at home, and [Toxvaerd \(2020\)](#) provides an equilibrium in which social distancing is an equilibrium outcome emerging from individually rational behavior. Consistent with our main mechanism, [Farboodi et al. \(2020\)](#) provide evidence from US micro-data for a large reduction in social activity by private household even prior to the implementation of public stay-at-home-orders and lockdowns of economic activity.

The elasticity of substitution across goods (or work activities), denoted by η in our paper, can reasonably assumed to be fairly high: we choose $\eta = 10$ as our benchmark, following [Fernandez-Villaverde](#)

(2010). An alternative interpretation is that these are rather distinct goods and distinct lines of work, and that substitutability may be lower: for that interpretation, we choose $\eta = 3$, following [Adhmad and Riker \(2019\)](#). Furthermore, in our benchmark parameterization, the infection probability in the most infectious sector (for the same consumption or work intensity) is nine times as high as in the least infectious sector.

We interpret the term “consumption” in this paper broadly and applicable to non-market social activities as well. The substitution discussion above is relevant just as much for partying together with friends as opposed to talking online, for congregating in parks as opposed to staying at home, to demonstrating against some cause together in the streets rather than sending petitions per e-mail. Viewed from that perspective, infection is inexorably linked to consumption or work place interaction, and we shall assume as much in our analysis.

We show that the resulting economic and health outcomes differ dramatically as a result. In the economy with homogeneous sectors, we obtain a deep decline of economic activity of ten percent, precisely as in ERT (in a calibration chosen to make our analysis exactly comparable to theirs). In contrast, more than eighty percent of that decline is mitigated in our benchmark economy with heterogeneous sectors. Likewise 80 percent of the deaths are avoided after the first year, compared to the homogeneous sector version. Despite the lack of any government intervention, the “curve” is flattened substantially. For different parameter configurations that capture the additional social distancing and hygiene activities which individuals might engage in voluntarily, we show that infections may decline entirely on their own, simply due to the re-allocation of economic activity: the curve does not just flatten, it gets reversed.

One may view our results as the prediction for the “Swedish” solution: Sweden has largely avoided government restrictions on economic activity, allowing people to make their own choices. The outcomes in terms of the disease spread nonetheless are largely in line with other European countries, which have imposed far more Draconian measures, while the output decline is considerably mitigated. One may also view our results as telling a cautiously optimistic tale about the potential for re-opening economies after a temporary lock down. Put differently, private incentives and well-functioning labor markets as well as social insurance policies or markets (that serve to insure those for which transition into different sectors in the economy takes time or is costly) may solve the COVID-19 spread rather effectively on their own, mitigating the decline in economic activity and in human costs.

Our results are stark, partially because our analysis assumes smoothly functioning labor markets where workers can quickly reallocate to the sectors now in demand: waiters at restaurants deliver food instead, for example. It is easy to argue that the world is not as frictionless as assumed here and that the message of our paper is perhaps a bit too Panglossian. We do not wish to argue that the substantial mitigation happens as easily on its own. The analysis here does show, however, that recognition of

substitution possibilities and recognition of private incentives of agents to become infected is potentially an important aspect in thinking about the current pandemic, both its onset but also its evolution as the economy is again opened to activity following the lock-down implemented in many countries.

Our analysis relates to other recent work that has emphasized the need to think about a multisector economy for the purpose of analyzing the economic effect of the recent epidemic, such as [Alvarez et al. \(2020\)](#), [Glover et al. \(2020\)](#), [Guerrieri et al. \(2020\)](#) or [Kaplan et al. \(2020\)](#). However, these authors do not feature the feedback from the differential infection probabilities across sectors into the private reallocation decision making of agents. A second very active literature evaluates the impact of publicly enforced mobility restrictions and social distancing measures on the dynamics of an epidemic, see e.g. [Correia et al. \(2020\)](#), [Fang et al. \(2020\)](#) or [Greenstone and Nigam \(2020\)](#). Complementary to this work we emphasize that private incentives to redirect consumption behavior might go a long way towards mitigating or even averting the epidemic, even in the absence of mobility restrictions or publicly enforced social distancing measures.

This paper is meant to clarify the key forces, rather than painting a nuanced and detailed picture of the quantities. We therefore focus first, in the model developed in section 2, on the infection risk in the consumption sector only. In section 3 we provide theoretical results that demonstrate the importance of the elasticity of substitution across sectors, and also argue that the same mechanism is at work if the risk of infections is located in the labor market rather than the consumption goods market, though one may wish to argue that the relevant elasticity of substitution is lower in that case. In section 4 we examine the optimal choices of a social planner who can observe which agents are infected and which are not, akin to the planning problem studied by [Alvarez et al. \(2020\)](#). One may think of this as a strong government with wide testing capabilities¹ of individuals, or a sufficiently powerful appeal to in particular the infected agents to do what is good for the country. Section 5 contains the quantitative results, showing how individually rational reallocation of economic activity across sectors is a strong mitigating force of the crisis even in the absence of explicit government intervention. It also shows that the social planner can stop the pandemic in its tracks early and quickly. This should not be all that surprising: the social planner simply prevents infected agents from co-mingling with the susceptible part of the population (by separating consumption of both groups across sectors), even if this imposes considerable, additional pain on the infected agents, which the social planner of course takes into account. What is more surprising, though, is that the decentralized solution with its substitution possibilities can get us there already 80 percent of the way on its own.

¹In this sense our social planner analysis is akin in spirit to the focus on testing in [Berger et al. \(2020\)](#).

2 Model

2.1 The macroeconomic environment

Our framework builds on Eichenbaum-Rebelo-Trabandt (2020) or ERT for short, and shares some key model components. Time is discrete, $t = 0, 1, 2, \dots$, measuring weeks. There is a continuum $j \in [0, 1]$ of individuals, maximizing the objective function

$$U = \mathbf{E}_0 \sum_{t=0}^{\infty} \beta^t u(c_t^j, n_t^j)$$

where β denotes the discount factor, c_t^j denotes consumption of agent j and n_t^j denotes hours worked, and where expectations \mathbf{E}_0 are taken with respect to stochastic health transitions describe below in detail. Like ERT, we assume that preferences are given by

$$u(c, n) = \ln c - \theta \frac{n^2}{2}$$

In contrast to ERT, we assume that consumption c_t^j takes the form of a bundle across a continuum of sectors $k \in [0, 1]$,

$$c_t^j = \left(\int (c_{tk}^j)^{1-1/\eta} dk \right)^{\eta/(\eta-1)} \quad (1)$$

where $\eta \geq 0$ denotes the elasticity of substitution across goods and c_{tk}^j is the consumption of individual j at date t of sector k goods. Workers can split their work across all sectors and earn a wage W_t in units of a numeraire good² for a unit of labor, regardless where they work. As the choice of the numeraire is arbitrary, we let a unit of labor denote that numeraire: thus, wages are equal to unity, $W_t = 1$.

Goods of sector k are priced at P_{tk} in terms of the numeraire, i.e. in units of labor. We suppose that production of goods in sector k is linear in labor, i.e. total output of goods in sector k equals the total number of hours worked there times some aggregate productivity factor A , and that pricing in each sector is competitive. Thus, prices equal marginal costs and are the same across all sectors,

$$P_{tk} = P_t = 1/A$$

²The presentation of the model is easier assuming a numeraire rather than payment in a bundle of consumption goods. We will not examine sticky prices or sticky wages in this model.

The date- t budget constraint of the household is therefore³

$$\int c_{tk}^j dk = An_t^j \quad (2)$$

2.2 The epidemic

As in ERT, we assume that the population will be divided into four groups: the “susceptible” people of mass S_t , who are not immune and may still contract the disease but are not currently infected, the “infected” people of mass I_t , the “recovered” people of mass R_t and the dead of mass D_t . We assume that the risk of becoming infected, and the rate of death or recovery do not depend on the sector of work, but exclusively depend on consumption interactions. Our focus here is on the sectoral shift in consumption: for simplicity and in contrast to ERT, we assume that infected individuals continue to work at full productivity, but that the disease can only spread due to interacting consumers. We show in subsection 3.2, that this is similar to a model, where the infection can only spread via the workplace. In our robustness analysis, we also allow for the additional, purely mechanical possibility of autonomous transmissions from infected to susceptible individuals, regardless of their choices.

Different goods or, perhaps better, different ways of consuming rather similar goods differ in the contagiousness. To that end, we assume that there is an increasing function $\phi : [0, 1] \rightarrow [0, 1]$, where $\phi(k)$ measures the degree of social interaction or relative contagiousness of consumption in sector k (or variety k of a consumption good). We normalize this function to integrate to unity,

$$\int \phi(k) dk = 1 \quad (3)$$

Consider an agent j , who is still “susceptible”: we denote this agent therefore with “ s ” rather than j . This agent is consuming the bundle $(c_{tk}^s)_{k \in [0, 1]}$ at date t . Symmetrically, let $(c_{tk}^i)_{k \in [0, 1]}$ denote the consumption bundle of infected people. Extending ERT, we assume that the probability τ_t^s for an agent of type s to become infected depends on his own consumption bundle, on the total mass of infected people and their consumption choices, and the degree $\phi(k)$ to which infection can be spread per unit of consumption in sector k ,

$$\tau_t = \pi_s I_t \int \phi(k) c_{tk}^s c_{tk}^i dk + \pi_a I_t, \quad (4)$$

where π_s is a parameter for the social-interaction infection risk. For the robustness exercise later on, we have also included the autonomous infection risk parameter π_a . With (4), the total number of newly

³Different from ERT, we do not feature a tax-like general consumption discouragement and thus no government transfers. We also abstract from capital and thus from intertemporal savings decisions, at they do.

infected people is given by

$$T_t = \tau_t S_t \quad (5)$$

The dynamics of the four groups now evolves as in a standard SIR epidemiological model,

$$S_{t+1} = S_t - T_t \quad (6)$$

$$I_{t+1} = I_t + T_t - (\pi_r + \pi_d)I_t \quad (7)$$

$$R_{t+1} = R_t + \pi_r I_t \quad (8)$$

$$D_{t+1} = D_t + \pi_d I_t \quad (9)$$

$$\text{Pop}_{t+1} = \text{Pop}_t - D_t \quad (10)$$

where π_r is the recovery rate and π_d is the death rate, and where Pop_t denotes the mass of the total population at date t . As in ERT, we assume that the epidemic starts from initial conditions $I_0 = \epsilon$ and $S_0 = 1 - \epsilon$, as well as $R_0 = D_0 = 0$.

2.3 Choices

We proceed to analyze the choices of the individuals.

Susceptible people: Denote as $U_t^s(U_t^i)$ the lifetime utility, from period t on, of a currently susceptible (infected) individual. As in ERT, the lifetime utility U_t^s follows the recursion

$$U_t^s = u(c_t^s, n_t^s) + \beta[(1 - \tau_t)U_{t+1}^s + \tau_t U_{t+1}^i] \quad (11)$$

where the probability τ_t is given in equation (4) and depends on the choice of the consumption bundle $(c_{tk}^s)_{k \in [0,1]}$. An s -person maximizes the right hand side of (11) subject to the budget constraint (2) and the infection probability constraint (4), by choosing labor n_t^s , the consumption bundle $(c_{tk}^s)_{k \in [0,1]}$ and the infection probability τ_t .

The first-order condition for consumption of c_{tk}^s is

$$u_1(c_t^s, n_t^s) \cdot \left(\frac{c_t^s}{c_{tk}^s} \right)^{1/\eta} = \lambda_{bt}^s + \lambda_{\tau t} \pi_s I_t \phi(k) c_{tk}^i \quad (12)$$

where λ_{bt}^s and $\lambda_{\tau t}$ are the Lagrange multipliers associated with the constraints (2) and (4). This equation

can be rewritten as

$$u_1(c_t^s, n_t^s) \cdot \left(\frac{c_t^s}{c_{tk}^s} \right)^{1/\eta} = \lambda_{bt}^s + \nu_t \phi(k) c_{tk}^i \quad (13)$$

where

$$\nu_t = \pi_s I_t \lambda_{\tau t} \quad (14)$$

Equation (13) reveals, that the risk of becoming infected induces an additional goods-specific component, scaled with the aggregate multiplier ν_t , compared to the usual first order conditions for Dixit-Stiglitz consumption aggregators (at constant prices across goods). In the absence of the impact of consumption on infection $\lambda_{\tau t} = \nu_t = 0$ and there is no consumption heterogeneity across sectors, $c_{tk}^s = c_t^s$ for all k , as in the standard model. In the presence of this effect, then susceptible households shift their consumption to sectors with low risk of infection (i.e. those with a low $\phi(k) c_{tk}^i$).

Taking the consumption profile of infected households (c_{tk}^i) as given, by choosing her consumption portfolio a susceptible individual effectively chooses her infection probability τ_t . As in ERT, the first-order condition for τ_t reads as

$$\beta(U_{t+1}^s - U_{t+1}^i) = \lambda_{\tau t} \quad (15)$$

The first-order condition with respect to labor is completely standard and reads as

$$u_2(c_t^s, n_t^s) + A\lambda_{bt}^s = 0 \quad (16)$$

Note that we have excluded the workplace infection, in contrast to ERT. We examine this possibility in subsection 3.2 below. With the chosen utility function, this first order condition simplifies to:

$$\theta n_t^s = A\lambda_{bt}^s \quad (17)$$

Infected people and recovered people: As in ERT, the lifetime utility of an infected person is

$$U_t^i = u(c_t^i, n_t^i) + \beta[(1 - \pi_r - \pi_d)U_{t+1}^i + \pi_r U_{t+1}^r + \pi_d \times 0] \quad (18)$$

Taking first order conditions with respect to the consumption choices and labor results in

$$u_1(c_t^s, n_t^s) \cdot \left(\frac{c_t^i}{c_{tk}^i} \right)^{1/\eta} = \lambda_{bt}^i, \quad (19)$$

where λ_{bt}^i is the Lagrange multiplier on (2) for an infected person. This is the usual Dixit-Stiglitz CES first order condition at constant prices, with solution

$$c_{tk}^i \equiv c_t^i \quad (20)$$

That is, as long as $\eta \in (0, \infty)$, infected individuals find it optimal to spread their consumption evenly across sectors, given that all sector goods have the same price, are imperfect substitutes, and differential infection probabilities across sectors are irrelevant for already infected individuals. Exploiting this result and the specific form of the period utility function (which implies $u_1(c, n) = 1/c$) in equation (19) yields $1/c_t^i = \lambda_{bt}^i$. For labor, we obtain the standard first order condition

$$\theta n_t^i = A \lambda_{bt}^i = \frac{A}{c_t^i} \quad (21)$$

Finally, exploiting the budget constraint (2), we arrive at the equilibrium allocations for infected people given by

$$n_t^i = \frac{1}{\sqrt{\theta}}, \quad c_t^i = \frac{A}{\sqrt{\theta}}$$

Likewise, the lifetime utility for a recovered person is

$$U_t^r = u(c_t^r, n_t^r) + \beta U_{t+1}^r \quad (22)$$

Given our assumptions, the optimal decision for both the i group and r group is the same⁴: we will therefore use c_t^i , $c_{t,k}^i$, n_t^i and λ_{bt}^i to also denote the choices of recovered individuals.

⁴Note here that we implicitly assume that infected people will be fully at work. One might alternatively wish to assume that only a fraction of them are at work instead. Given our assumptions about excluding infections in the work place, this does not affect the infection rate via that channel. However, lowering the amount of income of infected people lowers their consumption and thus lowers their ability to infect others in the consumption market. We do not wish to emphasize this channel, though: in a somewhat richer model, people will have a buffer stock of savings, and an infected person would then draw on these savings to finance consumption rather than respond to the temporary decline in labor income. Alternatively, income may fall considerably less in practice than the model would otherwise imply here, due to various social insurance policies.

2.4 Equilibrium Characterization

In equilibrium, each individual solves her or his maximization problem, and the labor and goods market has to clear in every period. Let n_{tk} be total labor employed in sector k . The market clearing conditions then read as:

$$S_t c_{tk}^s + (I_t + R_t) c_{tk}^i = A n_{tk} \quad (23)$$

$$\int n_{tk} dk = S_t n_t^s + (I_t + R_t) n_t^i \quad (24)$$

Given the solution to the problem of infected and recovered people, this can be simplified to

$$S_t c_{tk}^s + (I_t + R_t) \frac{A}{\sqrt{\theta}} = A n_{tk}$$

$$\int n_{tk} dk = S_t n_t^s + (I_t + R_t) \frac{1}{\sqrt{\theta}}$$

The equations can be simplified further to a set of aggregate variables as well as an equation determining the sectoral allocation, see appendix section [B](#).

3 Theoretical Results

3.1 Two extremes

It is instructive to consider extreme values for the elasticity of substitution η . The first extreme is an elasticity of substitution of zero such that the consumption aggregator is of the Leontieff form.

Proposition 1. *Suppose that $\eta = 0$, i.e. that the consumption aggregation in [\(1\)](#) is Leontieff. In that case, the multisector economy is equivalent to a multisector economy with a ϕ -function, which is constant and equal to 1,*

Proof. With Leontieff consumption aggregation, consumption is sector independent, $c_{tk}^j \equiv c_t^j$. Equations [\(4\)](#) and [\(5\)](#) now become

$$\tau_t = \pi_s I_t \int \phi(k) c_t^s c_t^i dk = \pi_s I_t c_t^s c_t^i \int \phi(k) dk = \pi_s I_t c_t^s c_t^i \quad (25)$$

and

$$T_t = \pi_s S_t I_t \int \phi(k) c_{tk}^s c_{tk}^i dk = \pi_s S_t I_t c_t^s c_t^i \quad (26)$$

□

Equations (25) and (26) furthermore show, that the Leontieff version is equivalent to the one-sector economy in ERT.

The other extreme is the case where goods are perfect substitutes.

Proposition 2. *Suppose that $\eta \rightarrow \infty$, i.e. that the sector-level consumption goods in (1) are perfect substitutes in the limit, Let $\underline{k} = \sup_k \{k \mid \phi(k) = \phi(0)\}$. Assume that $\underline{k} > 0$, i.e. that there is a nonzero mass of sectors with the lowest level of infection interaction. Suppose that $I_0 > 0$. Then there is a limit consumption c_{tk}^j for $j \in \{s, i, r\}$ as $\eta \rightarrow \infty$, satisfying*

$$c_{tk}^s = \begin{cases} c_t^s / \underline{k} & \text{for } k < \underline{k} \\ 0 & \text{for } k > \underline{k} \end{cases} \quad (27)$$

and

$$c_{tk}^j \equiv c_t^j \text{ for } j \in \{i, r\} \quad (28)$$

Equations (4) and (5) are replaced by

$$\tau_t = \pi_s \phi(0) I_t c_t^s c_t^i \quad (29)$$

and

$$T_t = \pi_s \phi(0) S_t I_t c_t^s c_t^i \quad (30)$$

That is, susceptible individuals only consume in the lowest infection-prone sectors with $\phi(k) = \phi(0)$, and infected (as well as recovered) individuals consume uniformly across all sectors.

Proof. Equation (28) is just equation (20), which also holds for recovered agents: it will therefore also hold, when taking⁵ the limit $\eta \rightarrow \infty$. Equation (27) follows from (14) together with (1), taking $\eta \rightarrow \infty$. Define the consumption distribution of type $j \in \{s, i, r\}$ as $\kappa_t^j(k) = c_{tk}^j / c_t^j$ and note that

$$\int \kappa_t^j(k) dk = 1 \quad (31)$$

and that

$$\kappa_t^j(k) \geq 0, \text{ all } k \quad (32)$$

⁵Note that it does not necessarily hold **at** the limit, as infected and recovered agents there are indifferent as to which goods to consume

Rewrite (4) and (5) as

$$\tau_t = \pi_s I_t c_t^s c_t^i \int \phi(k) \kappa_t^s(k) \kappa_t^i(k) dk \quad (33)$$

Therefore and analogously to ERT, the total number of newly infected people is given by

$$T_t = \pi_s S_t I_t \int \phi(k) \kappa_t^s(k) \kappa_t^i(k) dk \quad (34)$$

Equations (29) and (30) now follow from observing that $\kappa_t^i(k) \equiv 1$ and $\kappa_t^s(k) = 1/k$ for $k \in [0, \underline{k}]$ and zero elsewhere as well as noting that $\phi(k) = \phi(0)$ for $k \in [0, \underline{k}]$. \square

Equations (29) and (30) also show, that the limit is equivalent to the one-sector economy in ERT, with π_s replaced by $\pi_s \phi(0)$. Infection only takes place in the sector with lowest infection hazard, thus introducing the extra factor $\phi(0)$. The size of the sector, however, does not enter. With a smaller size of that sector and with equal distribution of infected agents across all sectors, susceptible agents meet a smaller fraction of infected agents in that sector on the one hand, a mitigating force. On the other hand, the consumption activity of susceptible agents in these sectors rises, an enhancing force. These two exactly cancel. Given that the size of the sector with lowest infection hazard does not matter at both extreme ends given in propositions 1 and 2, one might conjecture that it is never relevant. However, numerical simulations indicate, that larger rates of infection occur if that sector is smaller, for substitution elasticities $0 < \eta < \infty$.

Proposition 2 above exploits the fact that infected agents wish to spread their consumption equally across all sectors for any finite value of η . At the limit $\eta = \infty$, infected agents are entirely indifferent, though. At the one extreme, they might consume rather large portions of the low- k goods. At the other extreme, they stick to each other in the high-infection-risk segments, and not consume the low- k -goods at all. In that latter case, the infection probabilities become zero and the spread of the disease is stopped entirely. The following proposition provides the resulting range for the infection probabilities.

Proposition 3. *Suppose that $\eta = \infty$, i.e. that the sector-level consumption goods in (1) are perfect substitutes. Let μ_t be any function of time satisfying*

$$0 \leq \mu_t \leq \bar{\mu}$$

where $\bar{\mu}$ is defined as

$$\bar{\mu} = \frac{1}{\int \frac{1}{\phi(k)} dk} \quad (35)$$

and note that it satisfies

$$\phi(0) \leq \bar{\mu} \leq 1 \quad (36)$$

Then there is an equilibrium with equations (4) and (5) replaced by

$$\tau_t = \pi_s \mu_t I_t c_t^s c_t^i \quad (37)$$

and

$$T_t = \pi_s \mu_t S_t I_t c_t^s c_t^i \quad (38)$$

Proof. We first show (36). For the lower bound, note that

$$\int \frac{1}{\phi(k)} \leq \int \frac{1}{\phi(0)} = \frac{1}{\phi(0)}$$

The upper bound follows from Jensen's inequality and (3). We next shall show, that there is an equilibrium, when μ_t equals one of the two bounds. Given the consumption distribution function κ_t^i , note that the problem of the susceptible agents is to choose their own consumption distribution function κ_t^s so as to minimize (33), subject to the constraints (31) and (32). The Kuhn-Tucker first order condition imply that $\kappa_t^s(k) = 0$, unless

$$k \in \{k \mid \phi(k) \kappa_t^i(k) = \min \phi(k) \kappa_t^i(k)\}$$

For $\mu_t = 0$, let infected agents consume zero, $\kappa_t^i(k) = 0$ for all k in some subset \mathcal{K} of $[0, 1]$. In that case and per the argument just provided, susceptible people choose $\kappa_t^s(k) > 0$ only if $k \in \mathcal{K}$. Conversely, the worst case scenario in terms of infection arises, if $\phi(k) \kappa_t^i(k)$ is constant. Given (31), this yields

$$\kappa_t^i(k) = \frac{\bar{\mu}}{\phi(k)} \quad (39)$$

Given this κ_t^i function, susceptible agents are now indifferent in their consumption choice. Any κ_t^s function satisfying (31) and (32) then results in

$$\int \kappa_t^s \phi(k) \kappa_t^i(k) dk = \bar{\mu}$$

and thus (37) and (38) at $\mu_t = \bar{\mu}$, i.e. the upper bound. Finally, let $0 < \mu_t < \bar{\mu}$ and let $\lambda = \mu_t / \bar{\mu}$. Let \mathcal{K}

be a measurable subset of $[0, 1]$ with mass strictly between 0 and 1. Set

$$\kappa_t^i(k) = \begin{cases} \lambda \frac{\bar{\mu}}{\phi(k)}, & \text{for } k \in \mathcal{K} \\ \tilde{\lambda} \frac{\bar{\mu}}{\phi(k)}, & \text{for } k \in [0, 1] \setminus \mathcal{K} \end{cases}$$

where $\tilde{\lambda}$ is chosen such that (31) holds. Then, susceptible agents will choose $\kappa_t^s(k) = 0$ for all $k \in [0, 1] \setminus \mathcal{K}$, are indifferent between $k \in \mathcal{K}$, and (37) and (38) hold true for the chosen μ_t . \square

The proposition shows, that the perfect substitutability might be nearly as bad as the Leontieff case, if infected people behave particularly badly and distribute their consumption according to (39). Equations (37) and (38) are then the same equations as in the ERT model with π_s replaced by $\pi_s \bar{\mu}$. On the other hand, perfect substitutability can also result in the most benign scenario of a zero spread of consumption, if infected and susceptible people simply consume different goods.

There are fascinating policy lessons in here. Given that infected people will end up seeking services and consumption, it might be best to encourage them to seek out those types, where the degree of interaction is high, rather than forcing all agents, including the infected agents, into the low infection transmission segments. The model here shows that this can have dramatic consequences for the spread of the disease.

3.2 Infections in the Labor Market

Thus far we have assumed that infections can take place when acquiring consumption goods. We could have similarly allowed for heterogeneity in labor and assumed that it is at work in the labor market where individuals face the risk of contracting the virus. We explore this possibility in this section, offering two alternative approaches, and shall show that the formal analysis is conceptually similar and, for the first approach, actually equivalent to the model analyzed above. In economic terms and interpretation, the key distinction is arguably less in the formal differences between both versions of the model, but rather in the empirically plausible choice for the elasticity of substitution η : while it may be possible to easily substitute between different types of similar consumption goods (“Pizza at home” versus “Pizza in a restaurant”), the same may not be true for work (restaurants will still have to produce the to-be-delivered pizza in the restaurant kitchen, rather than having their workers stay at home and produce in their own kitchens). Our results for the lower elasticity of substitution $\eta = 3$ may thus be more appropriate for the analysis of infection-at-the-work-place. In the extreme without substitution possibilities, we are back at the homogeneous sector case.

As for the formal analysis, maintain the assumption that the period utility function is given by

$$u(c, n) = \log(c) - \theta \frac{n^2}{2} \quad (40)$$

but now assume that consumption c is a homogeneous good, while household labor n is a composite of differentiated sector-specific labor n_k , $k \in [0, 1]$. For the first, production-based approach to aggregation, assume that labor supplied by the household to the market is a CES composite of sector-specific labor, i.e. that $n = \int n_k dk$ as far as preferences are concerned, but that the budget constraint reads

$$c = A \left(\int n_k^{1-(1/\alpha)} dk \right)^{\alpha/(\alpha-1)} \quad (41)$$

Assume now, that infections occur in the labor market instead of per joint consumption, i.e. assume that the probability of a susceptible individual to become infected is given by

$$\tau_t = \tilde{\pi}_s I_t \int \phi(k) n_{tk}^i n_{tk}^s dk + \pi_a I_t \quad (42)$$

In Appendix C we establish the following result.

Proposition 4. *Suppose that $\tilde{\pi}_s = A^2 \pi_s$ and that $\alpha = \eta$. In that case, the production-based labor aggregation with infection in the labor market is equivalent to the consumption-infection economy described above, i.e. all aggregates remain the same, while $n_{tk}^s/n_t^s = c_{tk}^s/c_t^s$, when comparing the ratio of sector-specific labor to the labor aggregate in the labor-market-infection economy to the ratio of sector-specific consumption to the consumption aggregate in the consumption-infection economy.*

For this formal equivalence, it is important that the aggregation (41) takes place at the household level and not at the firm level, i.e. in firms hiring labor from different households. The latter would provide an interesting alternative environment for studying the sectoral shift issues raised here, but requires additional restrictions to preclude complete separation of infected and susceptible agents in equilibrium.

The household-level labor aggregation described above may be hard to envision as an environment for sector-specific contagion risk. We therefore offer a second, preference-based approach. For that, think of the household as composed of individual workers, each specialized to work in sector k , and that total household leisure, described by $\ell = f(n)$ for some strictly decreasing and differentiable function⁶ f is a CES-aggregate of worker-specific leisure,

$$f(n) = \left(\int f(n_k)^{1-1/\alpha} dk \right)^{\alpha/(\alpha-1)} \quad (43)$$

⁶Useful specifications are $f(n) = \bar{L} - n$ for some time endowment \bar{L} or $f(n) = 1/n$.

for some elasticity of substitution $\alpha \geq 0$. The household budget constraint is $c = A \int n_k dk$. The probability of infection is given by (42). This economy shares the the same basic forces as the heterogeneous consumption sector economy, although its analysis it is not exactly equivalent. In Appendix C we demonstrate this more formally. The remarks here are simply meant to show that the mechanisms in both types of labor-infection-based models are rather similar to our baseline consumption-based-infection economy indeed. We therefore skip a full quantitative analysis and do not to integrate this feature into the ensuing analysis.

4 Social Planning Problem

It is instructive to compare our results to that of a social planner with the ability to test individuals, i.e. with full knowledge of who is susceptible, infected or recovered. However, in the same way the agents in our model the planner cannot separate the infected from the susceptible (and recovered), when they consume (that is, the planner cannot change the consumption technology). Therefore, as in the decentralized economy, the spread of the disease while consuming can at best be mitigated by allocating consumers to low-infectious sectors. The social planner maximizes date-0 aggregate social welfare W_0 , where

$$W_0 = \sum_{t=0}^{\infty} \beta^t [S_t u(c_t^s, n_t^s) + I_t u(c_t^i, n_t^i) + R_t u(c_t^r, n_t^r)]$$

subject to the following constraints, and with the respective Lagrangian multipliers, after substituting out the infection risk for susceptible people, τ_t , and the number of newly infected people, T_t :

$$\mu_{f,t} : \quad \int S_t c_{tk}^s + I_t c_{tk}^i + R_t c_{tk}^r dk = A (S_t n_t^s + I_t n_t^i + R_t n_t^r) \quad (44)$$

$$\mu_{S,t} : \quad S_t = S_{t-1} - I_t + (1 - \pi_r - \pi_d) I_{t-1} \quad (45)$$

$$\mu_{I,t} : \quad I_t = \pi_s S_{t-1} I_{t-1} \int \phi(k) c_{t-1,k}^s c_{t-1,k}^i dk + (1 - \pi_r - \pi_d) I_{t-1} \quad (46)$$

$$\mu_{R,t} : \quad R_t = R_{t-1} + \pi_r I_{t-1} \quad (47)$$

The social planner takes S_0, I_0 and R_0 as given. It chooses the time paths of consumptions for susceptible, infected and recovered people c_{kt}^x for $x \in \{s, i, r\}$, the path for labor supply n_t^x , $x \in \{s, i, r\}$, and the paths for the mass of agents in the four groups S_t , I_t , and R_t . The first order conditions of the social planner's problem are presented in Appendix D.

5 Quantitative results

5.1 Computational Strategy

The unknowns to be carried around (aside from the sector-specific consumption): $U_t^s, c_t^s, n_t^s, \lambda_{bt}^s, \nu_t, \tau_t$. The equations determining these variables are the Bellman equation (11), the budget constraint (2), the infection constraint (B.8), the share constraint (B.5) replacing the original first order condition with respect to consumption, the first order condition with respect to labor (16) and the first order condition with respect to τ (15) combined with (14). One can easily eliminate λ_{bt} and n_t^s , using (2) and (16), as well as eliminate ν_t with (14) and (15): what remains then is a system in three unknowns U_t^s, c_t^s, τ_t and three equations, two of which are nonlinear integral equations, that would need to be solved. The way to proceed is from a distant horizon, and working backwards. Knowing U_{t+1}^s allows one to compute ν_t with (14) and (15). Using the two integral equations (having substituted out λ_{bt}^s and n_t^s) allows one to compute c_t^s and τ_t . From there compute n_t with (2) and U_t^s . We use Dynare to perform these calculations.

5.2 Parameterization

We choose parameters much in line with Eichenbaum et al. (2020) and summarize them in Table 1. Given that our infection interaction only takes place in the consumption sector, we choose π_s so that we obtain their 10-percent decline in consumption in a homogeneous-sector economy, see Fig. 1. We mostly investigate a two-sector economy, where both sectors are of equal size, and sector 1 has infection intensity ϕ_1 satisfying $0 < \phi(k) = \phi_1 < 1$ for $k \in [0, 0.5]$. Given the maintained assumption that the average $\phi(k)$ is equal to one, this implies that $\phi_2 = 2 - \phi_1$ for $k \in (0.5, 1]$. We pick $\phi_1 = 0.2$ for our benchmark calibration, implying $\phi_2 = 1.8$. We set $\eta = 10$ as well as, alternatively, $\eta = 3$. We also investigate higher values for η , in order to compare to the limit case discussed in Proposition 2.

In contrast to ERT, we shut down the autonomous infection possibility π_a for our benchmark calculations, resulting in a considerably lower number of ultimately recovered agents and a lower peak of infected agents, compared to their results. For comparison and robustness, we also provide a version of our main results, when allowing for autonomous infection possibility π_a , with parameters set so that the consumption decline in the homogeneous sector case remains at 10 percent at its bottom, but targeting a ratio of around 50 percent for the share of recovered people in the long run, as in their results.

Table 1: Parameter Values

Parameter	$\pi = 0$	$\pi \neq 0$	Description
π_s	4.05×10^{-7}	1.77×10^{-7}	Infection intensity
π_r	0.387	0.387	Recovery rate
π_d	1.944×10^{-3}	1.944×10^{-3}	Death rate
π_a	0.000	0.340	Autonomous Infection Intensity
η	10.000	10.000	Elasticity of substitution
θ	1.275×10^{-3}	1.275×10^{-3}	Labor supply parameter
A	39.835	39.835	Productivity
β	$0.96^{1/52}$	$0.96^{1/52}$	Discount factor
ϕ_1	0.200	0.200	Intensity of interaction in the low-interaction sector
v_1	0.500	0.500	Size of the low-interaction sector
ϕ_2	1.800	1.800	Intensity of interaction in the high-interaction sector
v_2	0.500	0.500	Size of the high-interaction sector

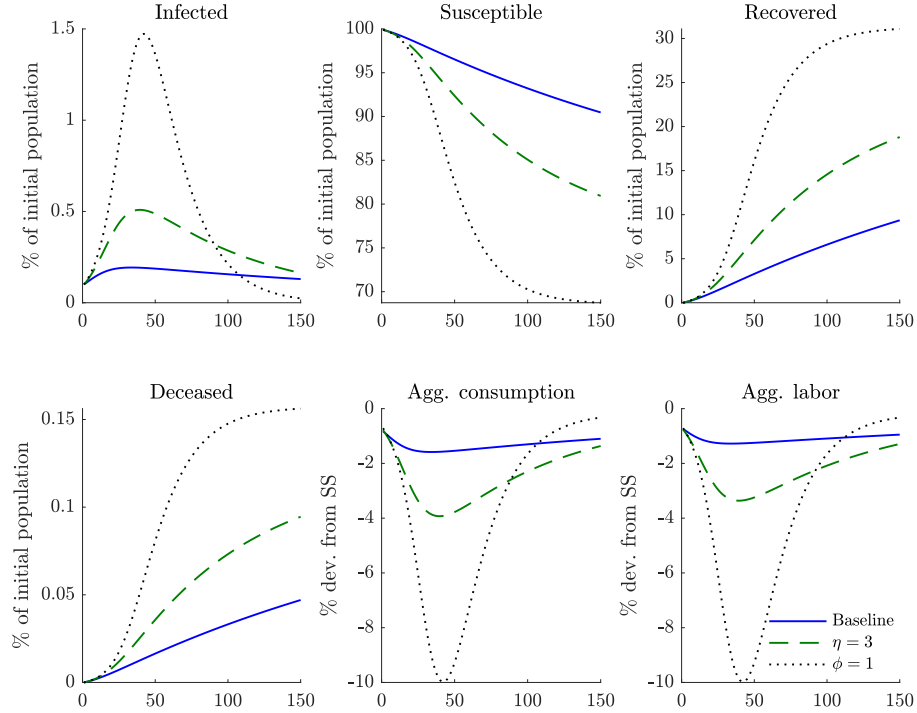


Figure 1: Comparison of our baseline model with a homogeneous-sector economy.

6 Results

We now present our results, starting in Section 6.1 with the findings for our benchmark economy with two sectors and contrasting them to the representative sector economy of ERT. We then explore, in Section 6.2 the sensitivity of the results to the inclusion of more than two sectors, as well as the possibility that some infections occur through non-economic interactions. Finally, we contrast the findings from the decentralized economy with the allocations chosen by a social planner in Section 6.3.

6.1 Results for the Benchmark Economy

Our simulations show that a heterogeneous-sector economy delivers a lower infection rate, as compared to a homogeneous-sector economy. Fig. 1 contains a comparison of the homogeneous-sector case $\phi \equiv 1$ as in ERT (the dotted black line) with our heterogeneous-sector case for our baseline elasticity of substitution $\eta = 10$ (solid blue line) as well as the alternative value $\eta = 3$ (dashed green line). In the event of a virus outbreak, susceptible households are able to substitute consumption goods from the high-infection sector with goods from the low-infection sector, while maintaining a relatively stable consumption path. Such a behaviour lowers the risk of being infected from participating in high-infection activities. As a result, the infection rate is only a fraction of that in a homogeneous-sector economy. Both the consumption decline and the number of deaths are considerably mitigated. For our baseline parameterization of $\eta = 10$, consumption declines by no more than 2 percent, and even for $\eta = 3$, the consumption decline is a more modest 4 percent rather than 10 percent, at its steepest point. The results are actually stronger in terms of measured consumption rather than the consumption composite shown in the second panel at the bottom. From the resource constraint, measured consumption is equal to measured labor and thus, given the production technology, equal to measured output. The decline in labor for $\eta = 10$ is just 1.3% rather than 10%, i.e. 87% of the measured output loss is avoided due to the substitution of consumption across sectors. The infection curve is considerably flattened as well, compared to the homogeneous-sector case.

For the deceased, the left panel of Fig. 9 shows the ratio of the heterogeneous sector scenario to that of the homogeneous sector case. Around week 50, i.e. around a year after the outbreak, the ratio declines to less than 20 percent for the $\eta = 10$ heterogeneous-sector scenario, compared to the homogeneous case. The ratio then starts climbing again and gradually. While we show these results, one probably wants to take into account that proper testing, vaccination and cures will likely be available two years from now, if needed. Therefore, the first 100 weeks is probably the truly relevant range of the simulations.

The comparison of $\eta = 3$ to $\eta = 10$ in Fig. 1 shows the importance of the substitution mechanism between goods: with a higher elasticity of substitution, households are more willing to substitute into

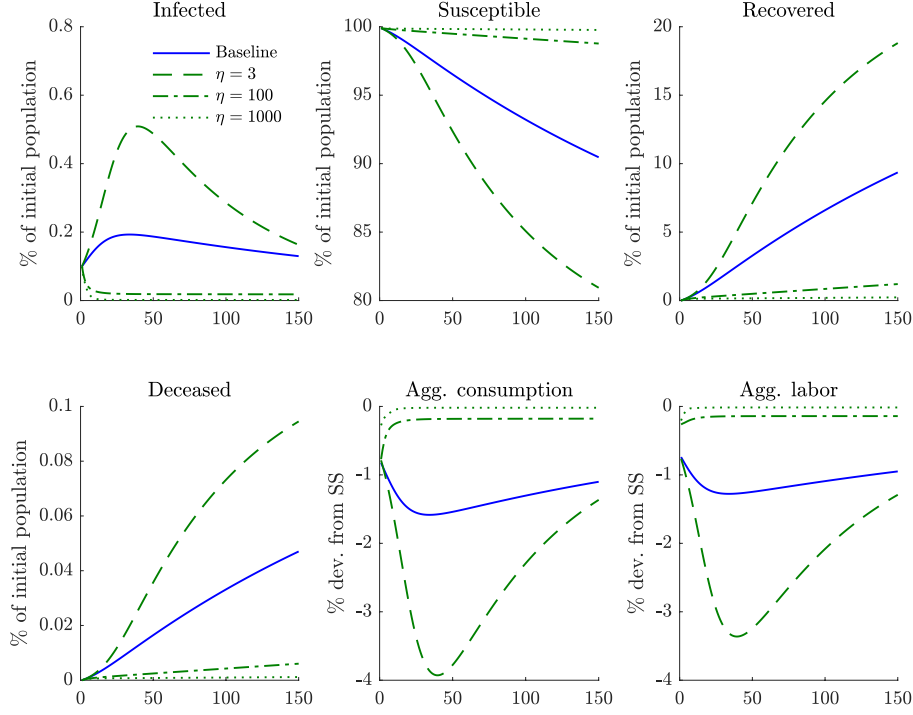


Figure 2: Heterogeneous-sector economy: variations in η .

the low-infection-risk sectors. [Fig. 2](#) contains a greater in-depth analysis of the role of η . In cases where the elasticity of substitution is approaching infinity, i.e. $\eta = 100$ and $\eta = 1000$, the infection curve is not just flattened, it is reversed: the number of infected people decays on its own. This is consistent with [Proposition 2](#). When goods from the two sectors are nearly perfectly substitutable, susceptible households consume exclusively from the low-infection sector, as depicted in [Fig. 3](#).

[Fig. 1](#) already shows that the heterogeneous sector scenario with $\eta = 10$ predicts a considerable flattening of the infection curve. It does not take much of a parameter change to obtain a reversal of the infection curve. [Fig. 2](#) has shown this already for higher values of η , but a similar effect holds with a slightly lower value for the infection parameter π_s . In [Fig. 4](#), we decrease the value of π_s in the scale of 10^{-9} until the number of infected people is lower in period 1 than in period 0. This exercise results in a π_s value of 3.51×10^{-7} , or 87% of the calibrated value in [Table 1](#). One can see how the number of infected agents declines on their own at the lower π_s value, shown in green dashed lines. Such a lower value for π_s might either reflect our still considerable uncertainty regarding the replication rate of the Coronavirus infection, or may reflect a modest success of non-economic policy measures, such as social distancing and enhanced personal hygiene.

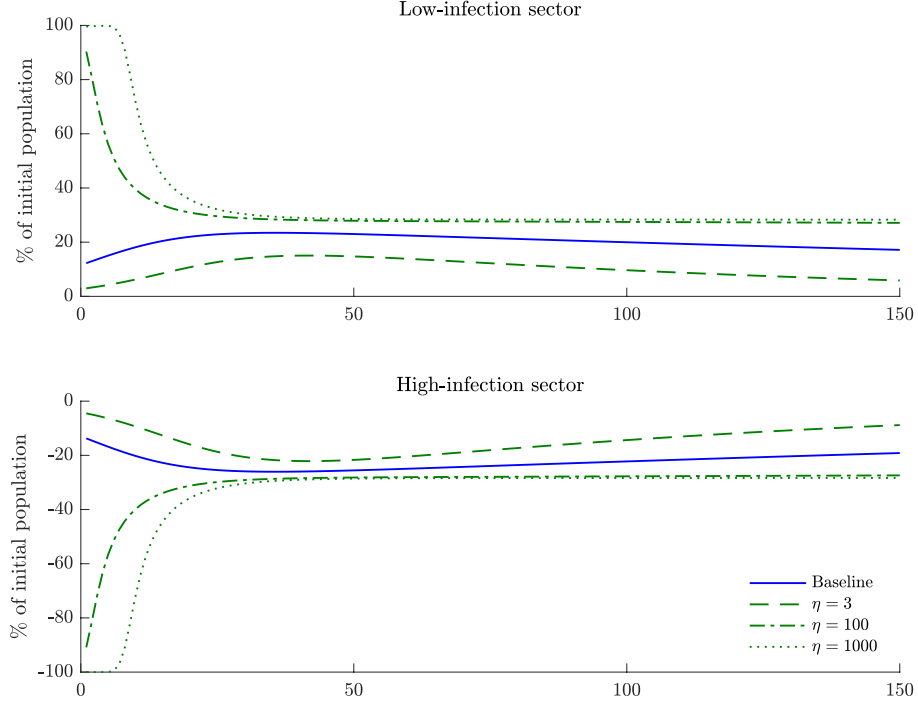


Figure 3: Heterogeneous-sector economy: consumption dynamics.

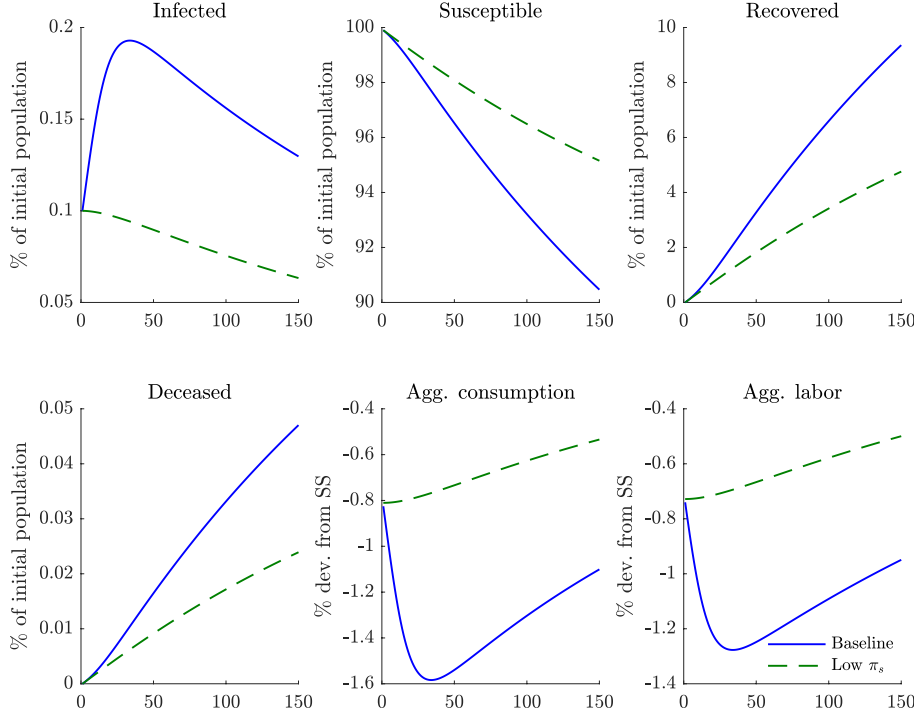


Figure 4: Reversal of the curve, when $\phi_1 = 0.2$ and π_s at 87% of the calibrated value.

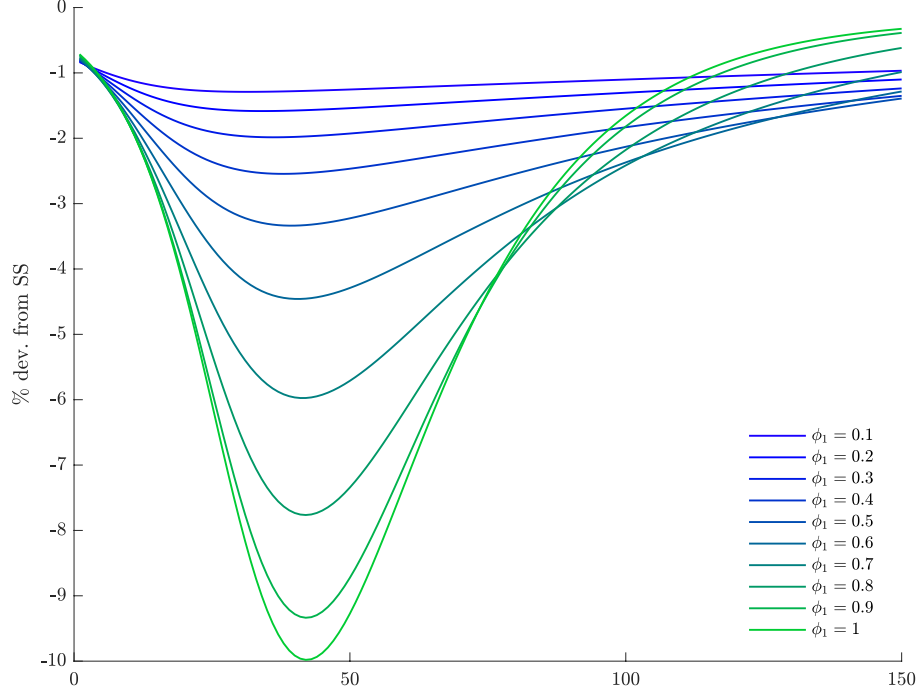


Figure 5: Consumption dynamics across ϕ_1 values.

6.2 Sensitivity Analysis

6.2.1 Varying infection risks

Our choice of $\phi_1 = 0.2$ implies a much lower risk of infection in the low-infection sector, as compared to the high-infection sector. In Fig. 5, we show the dynamics of aggregate consumption at varying values of ϕ_1 , with $\phi_1 = 0.1$ representing the largest difference in infection risk between the two sectors. Note that the average value of ϕ_1 and ϕ_2 is kept at 1. As the difference in infection risks decreases, the decline in aggregate consumption is larger. It is also of interest to note that despite the larger decline, the economy recovers to a higher level in cases of larger ϕ_1 values, two years after the epidemic. In Fig. 6, we show that for smaller value of ϕ_1 , the deceased population is only a fraction of that in the homogeneous-sector scenario.

6.2.2 More than Two Sectors

The model with two sectors is admittedly a stark (albeit transparent) representation of the U.S. economy. It is therefore of interest to examine the robustness of our findings in an economy with multiple sectors. Fig. 7 shows the outcome in an economy with nine sectors rather than just two, and the resulting shifts of economic activities across sectors. Sectors with lower infection, in general, experience an expansion as susceptible households substitute high-infection goods with low-infection ones. The effect appears to be

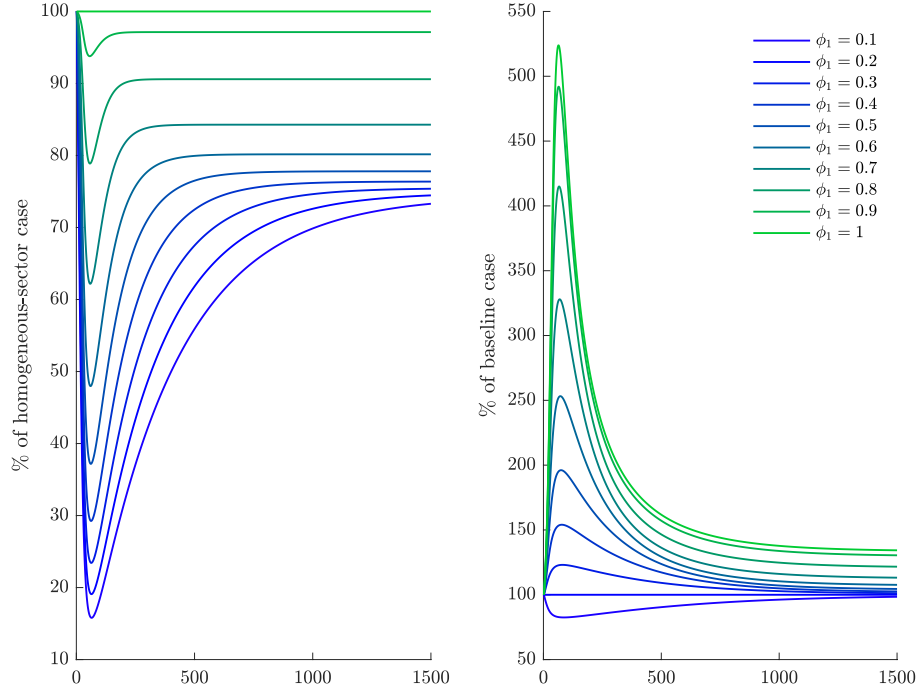


Figure 6: Dynamics of deceased across ϕ_1 values.

fairly linear rather than “heaping” all of the consumption on the lowest-infection sector. It is not quite linear, though: note that the distance of the lines increases with decreasing ϕ . Put differently, some modest “heaping” does take place. Notably, the dynamics of aggregate consumption traces that of the two-sector economy rather closely.

6.2.3 Autonomous Infections

For Fig. 8, we allow for the possibility of autonomous infections, outside the social consumption or labor activity, i.e. we allow for $\pi_a \neq 0$. For comparison with the results in ERT and the homogeneous sector case, we keep the target of a 10 percent consumption decline for the ERT economy, but now also impose the target of 50 percent recovered or deceased agents in the long run, see the black dotted line. Imposing $\eta = 10$ now results in a consumption decline of 4 percent rather than the 2 percent calculated above. This is due to the infection dynamics, which keeps on going: given the autonomously large number of infected people in the economy, susceptible agents will choose to reduce their consumption more now. Likewise, the decline in the number of deaths is no longer quite as dramatic. The right panel of Fig. 9 shows the result: still, slightly more than 50 percent of the deaths (rather than 80 percent in the left panel) are avoided in the heterogeneous sector economy, compared to the homogeneous sector case, around 1 year after the outbreak. Given the considerable autonomous nature of the pandemic in this version of the model, we still view this as a remarkably large number. In any case and as argued in the introduction,

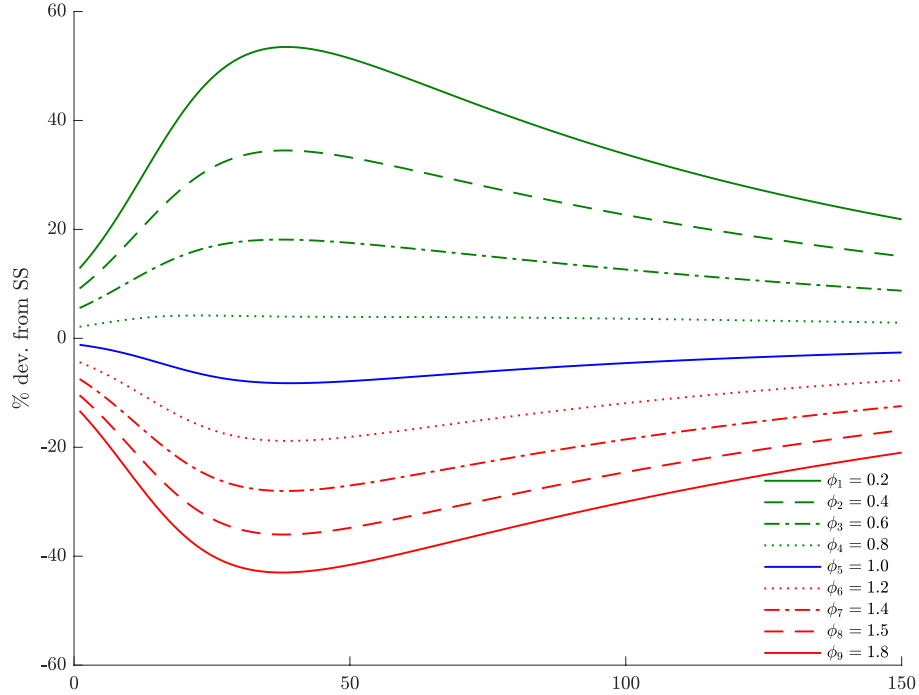


Figure 7: Consumption dynamics in a 9-sector economy.

it is hard to think of a source of infection not related to social activity, and it is hard to think of social activity as not being some form of consumption or work, even if these activities are not accounted for in the National Income and Product Accounts. For these reasons, we view our results in Fig. 1 as ultimately more relevant.

6.3 Socially Optimal Allocations

Lastly, we explore the solution to the social planner's problem described in section 4. Fig. 10 shows the outcome of the social planner solution (green line) in comparison to our baseline decentralized economy with $\eta = 10$ (blue line) as well as the homogeneous-sector case (black-dotted line).⁷ The social planner essentially stops the outbreak dead in its tracks: the number of infected agents declines quickly, and is barely noticeable within a few weeks after the start of the outbreak. The social planner achieves this outcome by restricting consumption of infected agents in a Draconian manner, thereby hugely mitigating the infection risk and stopping the infection at the onset. Compared to the competitive equilibrium outcome, a planner with the power to distinguish between the health status of infected and susceptible therefore is even more successful in averting the epidemic. However, as we saw above, private incentives together with substitution possibilities across sectors makes the epidemic much more

⁷The social planner solution for the homogeneous sector case (not plotted) is practically indistinguishable from the planner solution for the heterogeneous sector economy: as far as aggregates chosen by a social planner are concerned, sector heterogeneity plays practically no role.

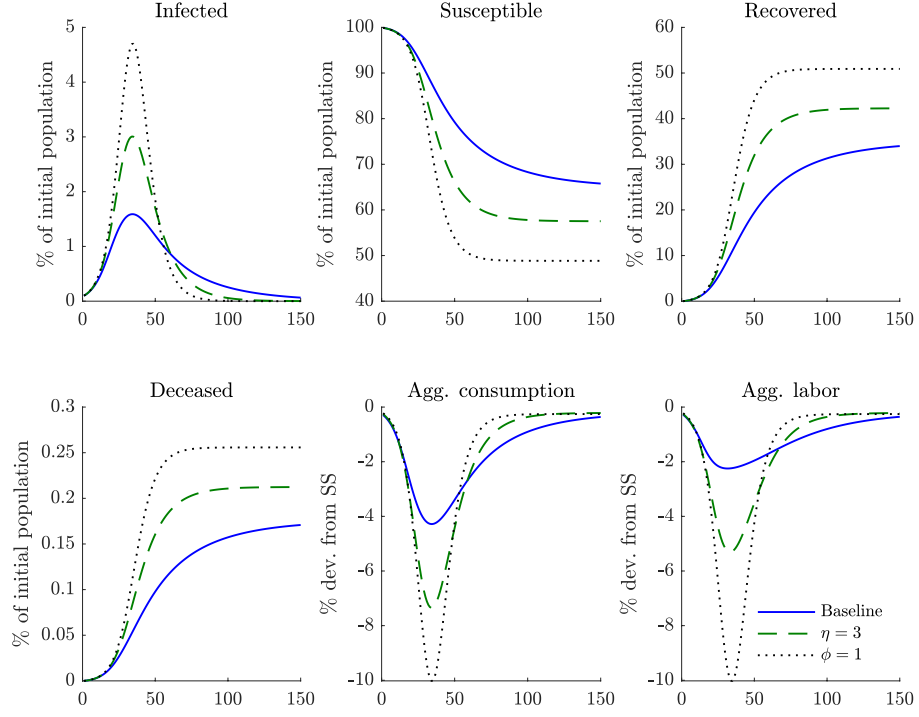


Figure 8: Dynamics with autonomous infection ($\pi_a \neq 0$).

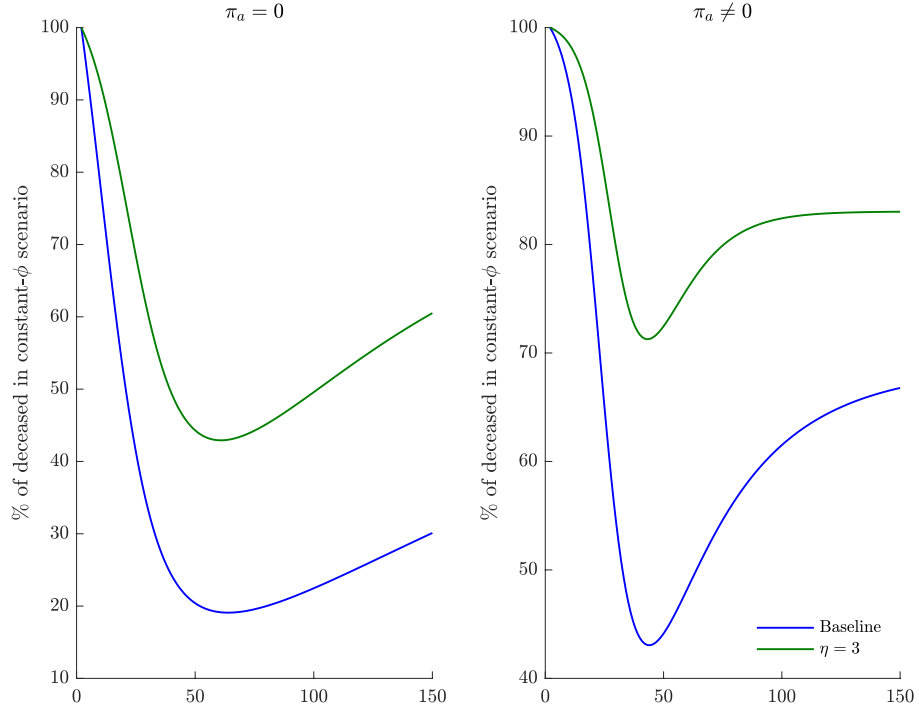


Figure 9: Deceased as percentages of constant- ϕ scenario.

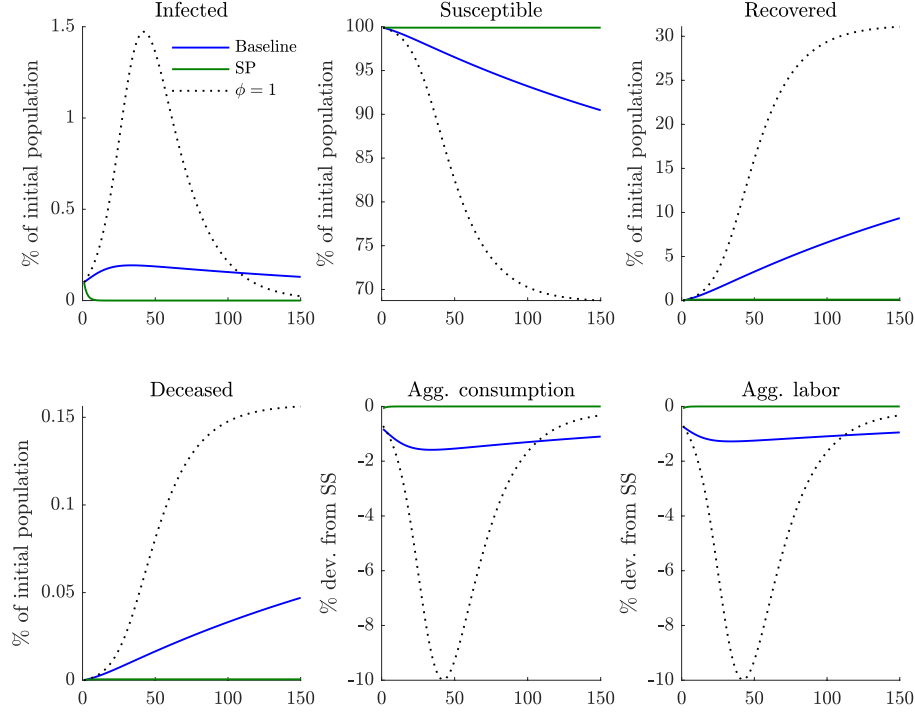


Figure 10: Heterogeneous-sector economy: social planning solution.

benign already, relative to the one-sector economy studied in most of the literature. Thus, the wedge between equilibrium and socially optimal allocations is much smaller if private households are given more opportunity to shift activity away from highly infectious sectors. The additional powers afforded to the social planner are therefore less potent in our economy, relative to a world where private adjustments to the epidemic are more limited.

Fig. 11 further illustrates how the consumption of infected people is restricted. In the baseline scenario, the per capita consumption of an infected household is restricted to less than 17% of its steady state of the non-infectious competitive equilibrium. In particular and due to the high substitutability between the goods in our baseline case of $\eta = 10$, nearly all the consumption of infected agents takes place in the low-infection sector. Effectively, the planner insulates with large infection risk from infected individuals. In an alternative case with lower elasticity of substitution, $\eta = 3$, the social planner does not impose quite as drastic a difference across the sectors (since this would be very costly in terms of lifetime utility of the infected individuals, which the planner values), and rather lowers the total consumption of the infected agent to around 20% of the non-infectious steady state. In the homogeneous sector case, alternatively, the case for $\eta = 0$, consumption in both sectors is the same, as the dotted-black line shows: now, consumption for the infected is reduced to only 8 percent of the non-infectious steady state. It is in this treatment of the infected, where the sectoral substitution possibilities matter considerably.

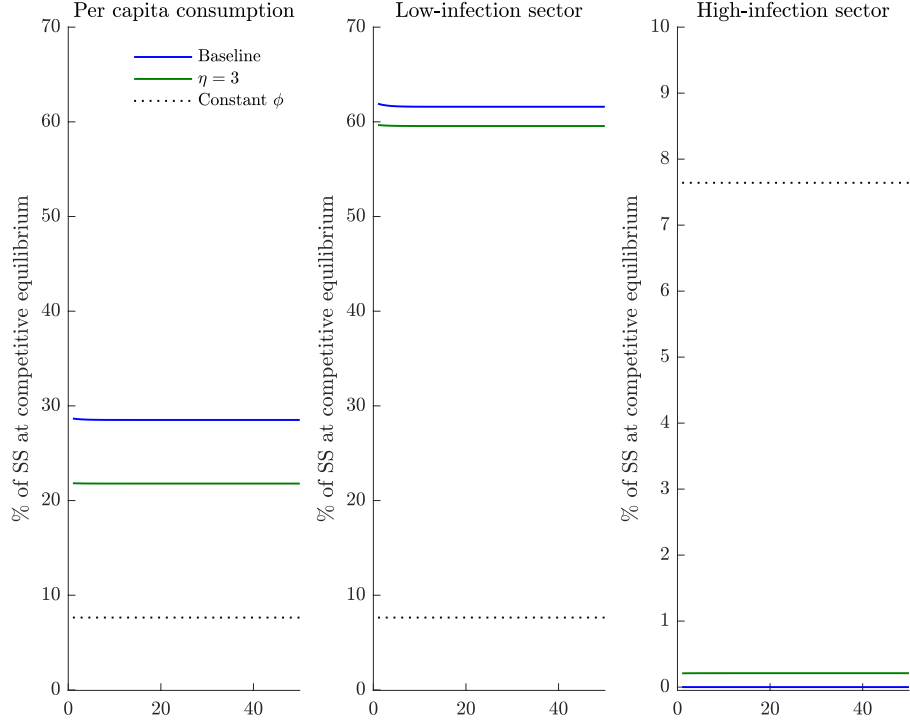


Figure 11: Per capita consumption of infected people.

One should take the social planner solution with a grain of salt, of course. Presumably, a really powerful social planner would entirely separate the infected and recovered people from the susceptible people. If this is technologically feasible, the disease cannot spread any further, and no consumption decline for the infected is needed. The formulation of our social planner problem precludes this possibility. In summary, our calculations and this remark shows that the possibility for containing the pandemic depends crucially on the tools available to the government, and they may involve imposing considerable hardship on a few (the initially infected) in order to rescue the many.

7 Conclusion

Our paper is inspired by the macroeconomics-cum-SIR model of [Eichenbaum et al. \(2020\)](#). We depart from their analysis in that we permit substitution of consumption across sectors with different degrees of infection probabilities. We show that the resulting economic outcome differ dramatically as a result. With homogeneous sectors, we obtain a steep decline of economic activity, fully in line with ERT. If the substitution mechanism is activated, eighty percent of that decline is mitigated in our benchmark calibration and in the decentralized economy: the “curve” is flattened substantially, without much prolongation. Pushing the parameters a bit more and thus capturing that people practice additional social

distancing and hygiene, we show that infections may decline entirely on their own, simply due to the re-allocation of economic activity: the curve does not just get flattened, it gets reversed. One may view our results as the “Swedish” outcome: Sweden has largely avoided government restrictions on economic activity, allowing people to make their own choices. These private incentives and well-functioning labor-and-social-insurance markets, we submit, may solve the COVID19-spread on their own, mitigating the decline in economic activity.

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A Two-sector simulations

The consumer interaction indicator $\phi(k)$ is defined piece-wisely as

$$\phi(k) = \begin{cases} \phi_1 & k \in [0, v) \\ \phi_2 & k \in [v, 1] \end{cases}$$

where v is the size of the sector with lower consumer interactions. For each sector $j \in \{1, 2\}$, there is a first-order condition with respect to c_{jt}^x , where $x \in \{s, i, r\}$. The equations for infected and recovered people are substituted out, because their consumption and labor are constant. The following equations consist the system delivering the paths of key variables.

$$v_1^{1/\eta} \frac{1}{c_t^s} \left(\frac{c_t^s}{c_{1t}^s} \right)^{1/\eta} = \frac{\theta}{A} n_t^s + \pi_s I_t \lambda_{\tau,t} \phi_1 \frac{A}{\sqrt{\theta}} \quad (\text{A.1})$$

$$v_2^{1/\eta} \frac{1}{c_t^s} \left(\frac{c_t^s}{c_{2t}^s} \right)^{1/\eta} = \frac{\theta}{A} n_t^s + \pi_s I_t \lambda_{\tau,t} \phi_2 \frac{A}{\sqrt{\theta}} \quad (\text{A.2})$$

$$c_{1t}^s + c_{2t}^s = A n_t^s \quad (\text{A.3})$$

$$c_t^s = \left[v_1^{1/\eta} c_{1t}^{s \cdot 1-1/\eta} + v_2^{1/\eta} c_{2t}^{s \cdot 1-1/\eta} \right]^{\frac{\eta}{\eta-1}} \quad (\text{A.4})$$

$$\lambda_{\tau,t} = -\beta (U_{t+1}^i - U_{t+1}^s) \quad (\text{A.5})$$

$$U_t^s = u(c_t^s, n_t^s) + \beta [(1 - \tau_t) U_{t+1}^s + \tau_t U_{t+1}^i] \quad (\text{A.6})$$

$$U_t^i = u(c_t^i, n_t^i) + \beta (1 - \pi_d) U_{t+1}^i \quad (\text{A.7})$$

$$\tau_t = \frac{A}{\sqrt{\theta}} \pi_s I_t (\phi_1 c_{1t}^s + \phi_2 c_{2t}^s) \quad (\text{A.8})$$

$$T_t = \tau_t S_t \quad (\text{A.9})$$

$$S_t = 1 - I_t - R_t - D_t \quad (\text{A.10})$$

$$R_t = R_{t-1} + \pi_r I_{t-1} \quad (\text{A.11})$$

$$D_t = D_{t-1} + \pi_d I_{t-1} \quad (\text{A.12})$$

$$I_t = T_{t-1} + (1 - \pi_d - \pi_r) I_{t-1} + 1_{t=1} \varepsilon \quad (\text{A.13})$$

Note that the time convention of disease dynamics is modified for implementation in Dynare. An MIT shock of size 0.001 is added to (A.13) in period 1. The paths of aggregate consumption and labor are given by

$$C_t = S_t c_t^s + (I_t + R_t) \frac{A}{\sqrt{\theta}} \quad (\text{A.14})$$

$$N_t = S_t n_t^s + (I_t + R_t) \frac{1}{\sqrt{\theta}} \quad (\text{A.15})$$

B Eliminating c_{tk}^s

Note that $c_{tk}^i = A/\sqrt{\theta}$. Let us reexamine (13) and write it as

$$\left(\frac{c_t^s}{c_{tk}^s}\right)^{1/\eta} = x_{tk} \quad (\text{B.1})$$

where we define

$$x_{tk} = c_t^s \left(\lambda_{bt}^s + \nu_t \phi(k) A / \sqrt{\theta} \right) \quad (\text{B.2})$$

Rewrite (B.1) as

$$c_{tk}^s = x_{tk}^{-\eta} c_t^s \quad (\text{B.3})$$

Thus

$$(c_{tk}^s)^{1-1/\eta} = x_{tk}^{1-\eta} (c_t^s)^{1-1/\eta} \quad (\text{B.4})$$

and integrate

$$\int (c_{tk}^s)^{1-1/\eta} dk = \int x_{tk}^{1-\eta} dk \times (c_t^s)^{1-1/\eta}$$

Taking this to the power $\eta/(\eta-1)$ finally yields

$$c_t^s = \left(\int x_{tk}^{1-\eta} dk \right)^{\eta/(\eta-1)} c_t^s$$

or the constraint

$$1 = \left(\int x_{tk}^{1-\eta} dk \right)^{\eta/(\eta-1)}$$

This can be simplified to

$$1 = \int x_{tk}^{1-\eta} dk \quad (\text{B.5})$$

or

$$c_t^s = \left(\int \left(\lambda_{bt}^s + \nu_t \phi(k) A / \sqrt{\theta} \right)^{1-\eta} dk \right)^{1/(1-\eta)} \quad (\text{B.6})$$

Thus, (4) and (5) can be rewritten as

$$\tau_t = \pi_s I_t \int \phi(k) x_{tk}^\eta c_t^s A / \sqrt{\theta} dk \quad (\text{B.7})$$

$$= \pi_s I_t \int \phi(k) \left(\lambda_{bt}^s + \nu_t \phi(k) A / \sqrt{\theta} \right)^{-\eta} (c_t^s)^{1-\eta} A / \sqrt{\theta} dk \quad (\text{B.8})$$

and

$$T_t = \pi_s S_t I_t \int \phi(k) x_{tk}^\eta c_t^s A / \sqrt{\theta} dk \quad (\text{B.9})$$

$$= \pi_s S_t I_t \int \phi(k) \left(\lambda_{bt}^s + \nu_t \phi(k) A / \sqrt{\theta} \right)^{-\eta} (c_t^s)^{1-\eta} A / \sqrt{\theta} dk \quad (\text{B.10})$$

C Details for the Heterogeneous Labor Economy

Proof of Proposition 4. To see the similarities and differences between the heterogeneous consumption- and heterogeneous labor economy more formally, observe that the first order conditions for infected and recovered agents are unchanged. In particular, we obtain $c_t^i = c_{tk}^i \equiv A / \sqrt{\theta}$ and $n_t^i = n_{tk}^i = 1 / \sqrt{\theta}$, regardless as to whether consumption or labor is heterogeneous and regardless of the particular approach taken for labor heterogeneity. It therefore suffices to examine the first order conditions for susceptible agents.

For the consumption-infection baseline model, the first-order conditions can be summarized by

$$\frac{1}{c_t^s} \left(\frac{c_t^s}{c_{tk}^s} \right)^{1/\eta} - \frac{\theta}{A} n_t^s = \pi_s \phi_k \lambda_{\tau t} \frac{A}{\sqrt{\theta}} I_t \quad (\text{C.1})$$

while the aggregation constraint and budget constraint are

$$c_t^s = \left(\int (c_{tk}^s)^{1-1/\eta} dk \right)^{\eta/(\eta-1)}$$

$$A n_t^s = \int c_{tk}^s dk$$

Define $n_{tk}^s = c_{tk}^s / A$ and rewrite these two equations equivalently as

$$c_t^s = A \left(\int (n_{tk}^s)^{1-1/\eta} dk \right)^{\eta/(\eta-1)} \quad (\text{C.2})$$

$$n_t^s = \int n_{tk}^s dk \quad (\text{C.3})$$

Recall that the infection probability is given by equation (4). Substituting out the solution for c_t^i as well as c_{tk}^s with $An_{tk}^s = c_{tk}^s$, it can be restated as

$$\tau_t = \pi_s I_t \int \phi(k) An_{tk}^s dk \frac{A}{\sqrt{\theta}} + \pi_a I_t, \quad (\text{C.4})$$

For the production-based heterogeneous-labor model, the first-order conditions can be summarized by

$$\frac{1}{c_t^s} \left(\frac{n_t^s}{n_{tk}^s} \right)^{1/\alpha} - \frac{\theta}{A} n_t^s = \frac{\tilde{\pi}_s}{A} \phi_k \lambda_{\tau t} \frac{1}{\sqrt{\theta}} I_t \quad (\text{C.5})$$

while the aggregation constraint and budget constraint are

$$c_t^s = A \left(\int (n_{tk}^s)^{1-1/\alpha} dk \right)^{\alpha/(\alpha-1)} \quad (\text{C.6})$$

$$n_t^s = \int n_{tk}^s dk \quad (\text{C.7})$$

Recall that the infection probability is given by equation (42), which can be restated as

$$\tau_t = \tilde{\pi}_s I_t \int \phi(k) n_{tk}^s dk \frac{1}{\sqrt{\theta}} + \pi_a I_t, \quad (\text{C.8})$$

For $\alpha = \eta$, $\tilde{\pi}_s = A^2 \pi_s$ and $n_{tk}^s/n_t^s = c_{tk}^s/c_t$, equations (C.5) becomes (C.1), equations (C.6) become equations (C.2) and (C.8) becomes (C.4). \square

For the preference-based heterogeneous-labor formulation, the first-order conditions can be summarized by

$$\frac{1}{c_t^s} - \frac{\theta}{A} n_t^s \frac{f'(n_{tk}^s)}{f'(n_t^s)} \left(\frac{f(n_t^s)}{f(n_{tk}^s)} \right)^{1/\alpha} = \frac{\tilde{\pi}_s}{A} \phi_k \lambda_{\tau t} \frac{1}{\sqrt{\theta}} I_t \quad (\text{C.9})$$

while the aggregation constraint and budget constraint are

$$c_t^s = A \int n_{tk}^s dk \quad (\text{C.10})$$

$$n_t^s = \left(\int (n_{tk}^s)^{1-1/\alpha} dk \right)^{\alpha/(\alpha-1)} \quad (\text{C.11})$$

While there is considerable formal similarity, there no longer is a formal equivalence as in proposition 4.

D First Order Conditions of the Social Planner Problem

The social planner's problem in the main text yields the following first-order conditions:

$$\begin{aligned}
\left(\frac{\partial}{\partial c_t^s} : \right) \quad & u_{1,t}^s \left(\frac{c_t^s}{c_{tk}^s}\right)^{1/\eta} + \mu_{f,t} &= \beta \pi_s \phi \mu_{I,t+1} I_t c_{tk}^i \\
\left(\frac{\partial}{\partial c_t^i} : \right) \quad & u_{1,t}^i \left(\frac{c_t^i}{c_{tk}^i}\right)^{1/\eta} + \mu_{f,t} &= \beta \pi_s \phi \mu_{I,t+1} S_t c_{tk}^s \\
\left(\frac{\partial}{\partial c_t^r} : \right) \quad & u_{1,t}^r \left(\frac{c_t^r}{c_{tk}^r}\right)^{1/\eta} + \mu_{f,t} &= 0 \\
\left(\frac{\partial}{\partial n_t^s} : \right) \quad & u_{2,t}^s &= \mu_{f,t} A \\
\left(\frac{\partial}{\partial n_t^i} : \right) \quad & u_{2,t}^i &= \mu_{f,t} A \\
\left(\frac{\partial}{\partial n_t^r} : \right) \quad & u_{2,t}^r &= \mu_{f,t} A \\
\left(\frac{\partial}{\partial S_t} : \right) \quad & u(c_t^s, n_t^s) + \mu_{f,t} \int c_{tk}^s dk + \mu_{S,t} &= \mu_{f,t} A n_t^s \\
& & + \beta \left[\mu_{S,t+1} + \mu_{I,t+1} \pi_s I_t \int \phi(k) c_{tk}^s c_{tk}^i dk \right] \\
\left(\frac{\partial}{\partial I_t} : \right) \quad & u(c_t^i, n_t^i) + \mu_{f,t} \int c_{tk}^i dk + \mu_{I,t} &= \mu_{f,t} A n_t^i - \mu_{S,t} \\
& & + \beta [(\mu_{S,t+1} + \mu_{I,t+1})(1 - \pi_r - \pi_d) \\
& & + \pi_r \mu_{R,t+1} + \mu_{I,t+1} \pi_s S_t \int \phi(k) c_{tk}^s c_{tk}^i dk] \\
\left(\frac{\partial}{\partial R_t} : \right) \quad & u(c_t^r, n_t^r) + \mu_{f,t} \int c_{tk}^r dk + \mu_{R,t} &= \mu_{f,t} A n_t^r + \beta \mu_{R,t+1}
\end{aligned}$$