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"Wages and the Allocation of Hours and Effort"

by

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Wages and the Allocation of Hours and Effort *

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Abstract: We examine the impact of wage stickiness when employment has an effort as well as hours dimension. Despite wages being predetermined, the labor market clears through the effort margin. We compare this model quantitatively to models with flexible and sticky wages, but no effort margin. Fluctuations in hours are intermediate to the standard flexible-wage and sticky-wage models; but output and consumption behave much like in the flexible-wage economy. Consequently, welfare costs of wage stickiness are potentially much, much smaller if one entertains an effort dimension.

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1. Introduction

There is an immense literature on the impact of nominal wage rigidities. This literature is presumably motivated by the large numbers of workers whose wage rates are updated to reflect economic news, including inflation, only at intervals of a year or longer. According to many writers, these wage rigidities fundamentally alter the short-run response of the economy to shocks, particularly nominal shocks. For instance, an unexpectedly low price level is understood to drive up the real wage, causing firms to cut back on labor until this reduction sufficiently drives up the marginal product of labor to the level of the "too high" real wage.

One criticism leveled at sticky-wage models is that they suggest that expansions in output will exhibit declines in labor productivity. Yet many cyclical fluctuations exhibit procyclical labor productivity. A common explanation for procyclical productivity is that cyclical movements in labor input are mismeasured. For instance, from N. Gregory Mankiw's text *Macroeconomics* (1994, page 382).

"If firms do hoard labor, then labor input is overestimated in recessions, because the hoarded workers are probably not working as hard as usual."

We argue, however, that choices for effort, in the face of sticky wages, will not work this way. If we recognize intensity of effort as a margin of choice for workers or firms, then it no longer makes sense to speak of workers as being pushed off their labor supply curves—a central element of the sticky-wage story. Figure 1 illustrates. Suppose that a nominal shock, given a sticky nominal wage, drives the real wage above its flexible-wage counterpart. The conventional interpretation of the impact of sticky wages has the economy move from point E to E', with labor supply exceeding labor demand. But it is clearly more profitable for a firm to ask more of its workers. As firms ask more of workers this shifts the demand for hours of labor upward. It also shifts the labor supply curve upward reflecting the greater cost to workers of each hour at the higher effort. This

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continues until work intensity justifies the "too high" real wage at a point like E''. Given the upward shift in labor demand, hours are reduced by less than at $E'_{.1}^{.1}$

The next section formalizes this story of sticky-wages with endogenous effort within a general equilibrium. Under flexible wages individuals make choices on how hard to labor at work, as well as how many hours to work. Under sticky wages this choice is restricted. Workers must produce sufficiently to merit the agreed upon wage in order to maintain employment.

Section 3 quantifies the model for empirical purposes. A key issue is the willingness of workers to trade off exertion and hours in production. We calibrate this willingness based on World War II evidence on how a number of piece-rate workers responded in work efficiency to large swings in their hours of work.

Section 4 examines model responses for hours, output, productivity, and a variety of other variables to a nominal and a set of real shocks. We compare responses for our model to those for a model with complete wage flexibility and a model with sticky wages and no endogenous effort response. Although real wages for our model respond to shocks very much like real wages in the typical sticky wage setting, the deviations of wages from the flexible wage response are largely mirrored by increases in effort. The response of hours worked is very much intermediate to its responses in the standard flexible-wage and sticky-wage models. Finally, output and consumption respond very much like in the flexible-wage economy. Additionally, our model is the only one considered capable of generating TFP and labor productivity leading hours worked over the business cycle. Consider a real shock that increases consumption, thereby raising the demand for money and lowering the price level. Initially, because the wage is sticky, this creates a rise in the real wage, a rise in effort, and a rise in labor productivity. With time the real wage, effort, and productivity decline, generating further increases in hours. Empirically fluctuations in the real wage, labor productivity, and TFP all dramatically lead fluctuations in hours worked.

¹ Becker (1985) models effort choice at work and home. Oi (1990) depicts the firm-size effect on wage rates as arising partly from a higher effort choice in larger firms. Hartley (1992) shows how a minimum wage might lead to greater effort, mitigating the legislation's impact on employment.

We also examine the welfare cost of sticky wages in the face of monetary shocks. We calibrate that this cost is smaller by nearly a factor of 100 for our model compared to a standard sticky-wage model without effort choice. This can help to rationalize the observed lack of short-run wage flexibility in wage setting.

2. Model

Consumers:

There are a large number of identical infinitely lived consumers in the economy. At time *t*, the representative consumer maximizes expected discounted utility defined over a stream of effective consumption, x_r .

$$U(t) = E_t \sum_{\tau=t}^{\infty} \beta^{\tau-t} u(x_{\tau}), \ \beta < 1,$$

 E_t is the expectations operator; the discount factor is β . Following Becker (1965), consumption activity requires an input of time as well as goods. More exactly, effective consumption reflects commodities c_t , real balances m_t/P_t and effective labor spent on consumption activities \tilde{l}_t . We assume the utility function reflects the following relations.

$$u(x_t) = \log x_t$$

$$x_t = z_t^{\theta_t} \tilde{l}_t^{1-\theta_t}$$

$$z_t = [\chi c_t^{1-\frac{1}{\upsilon}} + (1-\chi)(\frac{m_t}{P_t})^{1-\frac{1}{\upsilon}}]^{\frac{\upsilon}{\upsilon-1}}.$$

Shifts in preferences are allowed through variations in θ_t . An increase in θ_t represents an increase in importance of purchased inputs relative to time in producing effective

consumption. Goods and real money balances combine through a CES function with substitution elasticity v.

The distinguishing feature of our model is that the effective amount of labor supplied to the market and to home consumption depends not only on how hours are split between market and home, but also on levels of exertion or effort. Suppose the consumer spends an amount of time n_t in the market and 1- n_t at home for consuming. Let ϕ_t and $\tilde{\phi}_t$ represent the effort levels he exerts at work and in the activity of consuming. Then we treat effective labor in the market l_t and effective time in consumption \tilde{l}_t as

$$l_t = n_t \phi_t^{\gamma}$$
$$\widetilde{l_t} = (1 - n_t) \widetilde{\phi_t}^{\lambda},$$

where both γ and λ are ≥ 0 and < 1.

We impose a constraint on the available energy that a consumer can exert in market and non-market activity. The "energy constraint" is

(1)
$$\phi_t n_t + (1 - n_t) \widetilde{\phi}_t = 1.$$

This presents consumers with a tradeoff. If the consumer works more intensely in the market, he is left with less energy for non-market activities. (Becker, 1985, introduces such a constraint.) More generally, we can envision a number of ways in which consumers can potentially show themselves to be more desirable employees. For instance workers could reduce absenteeism at the cost of less flexibility to stay at home on days they deem that as attractive. Or workers could cut back on consumption activities that make them less productive and attractive as employees, such as carousing to late hours during the workweek.

The consumer spends his money income for purchases of consumption goods c_t , investment i_t , and money holdings m_t . Income includes labor income, rental income and a cash transfer from the government. Given the nominal wage rate W_t , rental rate R_t , price of goods P_t , and money transfer from government T_t , the budget constraints are

(2)
$$c_t + \frac{m_t}{P_t} + i_t \le \frac{W_t}{P_t} n_t + \frac{R_t}{P_t} k_t + \frac{m_{t-1}}{P_t} + \frac{T_t}{P_t}$$

(3)
$$k_{t+1} = i_t + (1 - \delta_K)k_t$$

The money transfer from the government reflects the income from money creation. $T_t = M_t - M_{t-1} = (\mu_t - 1)M_{t-1}$, where $\mu_t = \frac{M_t}{M_{t-1}}$. Capital depreciates at rate δ .

The effective labor of a worker is $n_t \phi_t^{\gamma}$. The wage is related to hourly effort ϕ_t by

(4)
$$\frac{W_t}{P_t} = \Omega_t \phi_t^{\gamma}.$$

 Ω_t is the market's valuation of labor, determined in general equilibrium as described below. Equation (4) has two separate interpretations depending on whether wages are flexible or sticky. Under flexible wages it represents the ability of a worker to earn a higher wage by exerting greater effort. An individual worker treats the marginal value of labor, Ω_t , as given with respect to his actions. Therefore, he views each 1 percent expansion in effort ϕ_t to result in a γ percent real wage increase. Under sticky wages the worker takes not only Ω_t but also the real wage as given. Therefore, to be employed, the worker has to provide an effort dictated by

$$(4') \qquad \phi_t = \left(\frac{W_t}{P_t}/\mathcal{Q}_t\right)^{1/\gamma}.$$

Under flexible wages, consumer maximization yields two static first-order conditions for choosing effort and hours worked and two dynamic first-order conditions for choosing investment in capital and investment in real money balances.

(5)
$$\phi_t; \quad \frac{\lambda \phi_t}{1 - n_t \phi_t} = \frac{\gamma \theta_t}{1 - \theta_t} \frac{W_t}{P_t \widetilde{c}_t}$$

(6)
$$n_t; \quad \frac{1-\lambda}{1-n_t} + \frac{\lambda\phi_t}{1-n_t\phi_t} = \frac{\theta_t}{1-\theta_t} \frac{W_t}{P_t\widetilde{c}_t}$$

(7)
$$k_{t+1}; \quad \beta \frac{\widetilde{c}_t}{\theta_t} E_t [\frac{R_{t+1}/P_{t+1} + 1 - \delta}{\widetilde{c}_{t+1}/\theta_{t+1}}] = 1$$

(8)
$$m_t; \quad \frac{1-\chi}{\chi} (\frac{m_t}{P_t \widetilde{c}_t})^{-\frac{1}{\upsilon}} = 1 - \beta E_t [\frac{\theta_{t+1} P_t \widetilde{c}_t}{\theta_t P_{t+1} \widetilde{c}_{t+1}}]$$

where $\tilde{c}_t = c_t \left[1 + \frac{1-\chi}{\chi} \left(\frac{m_t}{P_t c_t}\right)^{1-\frac{1}{\nu}}\right]$ is consumption magnified by a factor equal to one plus the foregone interest cost of real balances held per unit of consumption.

With flexible wages equations (1), (5), and (6) yield the relative time devoted to market work and the relative rates of exertion in market and home activity.

$$\frac{n_t}{1-n_t} = \frac{1-\gamma}{1-\lambda} \frac{\theta_t}{1-\theta_t} \frac{W_t}{P_t \tilde{c}_t} - 1$$
$$\frac{\phi_t}{\tilde{\phi}_t} = \frac{\gamma(1-\lambda)}{\lambda(1-\gamma)}$$

Along a steady-state path with common growth in consumption and real wages, as we will have below, hours supplied to the market are constant. Exertion in market work relative to at home is constant at all times. If the parameters γ and λ are equal then $\frac{\phi_i}{\tilde{\phi_i}}$ equals one; furthermore, neither ϕ_i nor $\tilde{\phi_i}$ varies cyclically. If $\gamma > \lambda$, then $\frac{\phi_i}{\tilde{\phi_i}}$ is greater than one. This further implies that both ϕ_i and $\tilde{\phi_i}$ will vary opposite fluctuations in market hours.

If the wage is predetermined then workers are not free ex-post to choose effort. First-order condition (5) becomes irrelevant, with ϕ_i instead determined by the constraint in (4'). In a typical sticky wage model, if the real wage is too high ex-post, hours are reduced to drive up the marginal product of labor. Here by working harder workers maintain the choice to work longer hours. In fact, even though the wage is sticky the labor market continues to clear. (Recall Figure 1.)

In addition to choosing current market hours, workers' wage rates must be specified a period in advance—this is the source of wage stickiness. The first-order condition for this choice can be written as:

(9)
$$W_{t+1}; W_{t+1}E_t[\frac{\theta_{t+1}n_{t+1}}{P_{t+1}\tilde{c}_{t+1}}] = \frac{1-\lambda}{1-\gamma}E_t[\frac{(1-\theta_{t+1})n_{t+1}}{1-n_{t+1}}]$$

Firms:

There are a large number of identical firms operating under constant returns to scale in capital and effective labor. The representative firm hires capital and labor each period to maximize profits $(P_tY_t - W_tN_t - R_tK_t)$ subject to the production function

(10)
$$Y_t \equiv F(K_t, N_t, \boldsymbol{\Phi}_t; A_t, \boldsymbol{Q}_t) \equiv A_t K_t^{1-\alpha} (\boldsymbol{Q}_t N_t \boldsymbol{\Phi}_t^{\gamma})^{\alpha}.$$

 Φ_t represents aggregate effort level; A_t reflects temporary productivity shifts, whereas Q_t reflects a deterministic trend of technology that grows at rate g. The first order conditions for capital and labor are

(11)
$$\frac{R_t}{P_t} = MPK_t = (1-\alpha)A_tK_t^{-\alpha}(Q_tN_t\Phi_t^{\gamma})^{\alpha}$$

(12)
$$\frac{W_t}{P_t} = MPN_t = \alpha A_t K_t^{1-\alpha} Q_t^{\alpha} N_t^{\alpha-1} \Phi_t^{\gamma \alpha}.$$

The first-order condition for labor yields a wage rate per efficiency unit of labor equal to $\Omega_t = \alpha A_t Q_t^{\alpha} \left(\frac{K_t}{N_t \phi_t^{\gamma}}\right)^{1-\alpha}$.

Rational Expectations Equilibrium:

The markets for goods, labor, and money clear each period. A rational expectations equilibrium is a set of stochastic processes for the endogenous variables $\{Y_t, K_t, N_t, \phi_t, c_t, m_t, P_t, W_t, R_t\}$ that satisfies (3), (4'), (6)-(8), (10)-(12), and market clearing for exogenous processes $\{A_t, \theta_t, \mu_t, Q_t\}$. The model is solved numerically using a log-linear approximation of the system of first order conditions and constraints of the stationary economy around the steady state as in King, Plosser and Rebelo (1988.)²

3. Calibration of Model Parameters and Shocks

In our model the labor market clears, despite short-run wage stickiness, thanks to fluctuations in market effort. Consequently, the model's predictions for fluctuations in hours and output depend not only on the conventional elasticity of labor supply, but also on how desired hours are affected by these fluctuations in effort. That, in turn, depends on the parameters γ and λ . As an example, in the limit as γ and λ approach one hours and effort are perfect substitutes. Consider a nominal shock that drives up the real wage and effort by one percent. Workers' hours simply decrease by one percent, holding output (and welfare) constant. In fact, provided γ equals λ , though not one, to a first-order approximation there will be offsetting movements in productivity and hours, leaving effective production and consumption constant. More generally, however, the increase in real wage and effort leads to a lesser decrease in hours, an increase in output, and a fall in effective leisure $\tilde{l_t}$.

 $^{^{2}}$ Given the existence of trends in technology and the money supply, we need to transform the economy so that it admits a stationary solution. We can do so by dividing real variables by the technology index and

Calibrating the Elasticity of Labor Supply:

Let ξ denote the elasticity response of hours to the real wage, holding current consumption expenditures constant. The model implies an elasticity of one for (1-n) with respect to the wage. (See equation (5).) Therefore it implies a value of approximately $\frac{1-n}{n}$ for ξ . We set the compensated elasticity of labor supply, ξ , equal to one. This value is much lower than what is typically employed in simulations of real business cycles, but is quite large relative to most estimates from cross-sectional and panel data (Ghez and Becker, 1975, MaCurdy, 1981, and Altonji, 1986).³

Calibrating $\frac{\phi}{\widetilde{\phi}}$:

As discussed above, the optimal ratio of effort in market work relative to that in consumption is $\frac{\phi}{\tilde{\phi}} = \frac{\gamma(1-\lambda)}{\lambda(1-\gamma)}$. Thus knowing $\frac{\phi}{\tilde{\phi}}$ is sufficient to determine a relationship between the parameters λ and γ . Quantifying $\frac{\phi}{\tilde{\phi}}$ exactly is not feasible. We start from a presumption that $\frac{\phi}{\tilde{\phi}}$ is greater than (or equal to) one. Studies of exertion and energy use have focused largely on activities in developing countries, where calorie intake is a more primary concern. Fogel and Floud (1991) examine caloric energy requirements for a number of activities. These are described in Appendix A. Fogel and Floud also discuss the total energy requirements for work versus discretionary activities (leisure). Their calculations suggest greater exertion at work except for particularly sedentary occupations. In addition to physical and caloric considerations, most leisure and

nominal variables by the previous period's money stock. (To save on notation, we use the same variables for the transformed stationary variables.)

³ Several studies have examined how time is divided between market and non-market pursuits based on time use diaries. (Examples include Hill, 1983, Juster and Stafford, 1985, 1991.) From Juster and Stafford (1991), a sample of men in the United States in 1981 report spending 48 hours per week in market work, including commuting, and 42 hours in social entertainment and various sorts of passive and active leisure. For women the comparable number of hours are respectively 26 and 42. These numbers suggest a value for $\frac{1-n}{n}$ of one or perhaps somewhat larger. Our primary interest is to explore the cyclical implications of the

model-so we do not want to employ an implausibly large value for ξ for the sake of matching crude measures of $\frac{1-n}{n}$.

consumption activities are presumably less tiresome mentally than typical market work. Based on these considerations, we set the ratio $\frac{\phi}{\phi}$ somewhat arbitrarily at $\frac{3}{2}$. (We explore the robustness of the results to this choice.) This implies λ is related to γ as $\lambda = \frac{2\gamma}{3-\gamma}$.

Calibrating γ from WWII experiences:

How desired hours respond to exogenous changes in effort reflects parameter γ . But we do not see a practical way to estimate this response. As a result of World War II, many workers in manufacturing faced dramatic changes in their workweeks. The U.S. Bureau of Labor Statistics (BLS) took advantage of these variations to study the impact of hours of work on efficiency and absenteeism. The results of these studies are reported in *Studies of the Effects of Long Working Hours*, BLS (1944) and *Hours of Work and Output*, BLS (1947). By measuring how workers vary effort in response to an enforced change in hours, this provides an alternative way to judge to what extent hours and effort are substitutes.

Productivity, output per hour, equals ϕ_t^{γ} . From equation (5)

$$\phi_t n_t = \frac{1}{1 + \frac{\lambda(1-\theta)}{\gamma \theta} \frac{P_t \widetilde{c}_t}{W_t n_t}}.$$

If consumption expenditures move one-for-one with earnings then $\phi_t n_t$ is constant. This implies changes in productivity per hour are related to changes in hours according to

$$\Delta \ln(\frac{y_t}{n_t}) = \gamma \Delta \ln(\phi_t) = -\gamma \Delta \ln(n_t) \,.$$

Thus the response of productivity to the wartime changes in hours yields a value for γ .

More generally, the ratio of consumption to earnings will vary with the large changes in hours. Given that wartime changes in hours were transitory and restrictions were placed on consumer purchases during the war, workers probably devoted some of the extra earnings from longer hours to savings. As an extreme, suppose that consumption was not affected by the wartime changes in hours. Then changes in productivity are related to changes in hours by

$$\Delta \ln(\frac{y_t}{n_t}) = \gamma \Delta \ln(\phi_t) \approx -\gamma \Delta \ln(n_t) \left[\frac{1}{1 + \frac{\lambda(1-\gamma)(1-\theta)}{\gamma \theta}}\right] = -(\frac{\gamma}{2-\gamma}) \Delta \ln(n_t),$$

where \approx reflects a first-order approximation. The last equality follows from substituting values for λ and θ to be consistent with the calibrations above. Productivity falls less if consumption does not vary. We first use the war data to observe how much productivity declined in response to an expansion in hours. We then use that response to calibrate two extreme values for γ based on consumption varying one-for-one with earnings or being unaffected.

The BLS examined 78 case studies covering 3,105 workers in 34 plants across a variety of industries. Each case included anywhere from 1 to 5 changes in hours.⁴ In order to estimate the response of effort to changes in hours workers must be choosing their level of effort. We are concerned that this may not be true for workers paid at an hourly rate. Therefore we restrict our attention to cases involving piece rate workers.⁵ We further restrict attention to cases where the pace of work is described as dictated by the worker, as opposed to by machine. We also required that terms of compensation were essentially unaltered across the changes in hours. We are left with 27 groups of workers and 62 hours changes.⁶

⁴ The BLS visited over 800 plants; but most did not meet the requirements of the study. From Bulletin 917: "In order to permit the effects of various schedules of hours to emerge clearly, it was necessary to rule out all other variables. A plant, therefore, could not be studied if, during the various periods to be surveyed, hours were not maintained consistently at fairly fixed and definite schedules. During these periods, the operations performed by the workers to be studied had to remain essentially unchanged, and the number of identical workers involved had to be reasonably large."

⁵ The study was heavily weighted toward groups paid by piece-rate, as this made it easier to measure workers' output. Bulletin 917 reports that, on average, workers on hourly rates maintained greater efficiency in response to an increase in hours than did those on piece rates.

⁶ One case corresponds to 150 workers. All others correspond to a number of workers between 8 and 48. 11 of these changes occur prior to the war. 16 represent increases in hours from before to after Pearl

Implicit in this calculation is that productivity is not affected by an increase in hours worked per week except through effort. If an expansion in hours is associated with a decrease in capital per worker this could lower productivity. We do not believe this was the case here. Adding work on Saturdays or Sundays or lengthening a shift should not reduce capital per worker. Furthermore, the study selected groups of workers where the number and mix of workers in the group did not change too significantly.

Many of the large increases in hours are associated with the United States' entry into the war. Conversely, many of the large decreases reflect the end of the war. Entry into war may have provided a strong psychological stimulus to productivity, particularly for workers producing munitions and other goods directly related to the war effort. For the case of 18 workers involved in machining metal parts BLS (1947) states, "*It is pertinent to an analysis of the findings in this plant that workers became aware of the demand for company's products in the war effort* ..." For this reason, we introduce a control variable, ΔWar , that equals 1 for periods reflecting entry into the war, equals -1 for periods reflecting the end of the war, and equals 0 otherwise.

Results are presented in Table 1. The first column regresses the reported percent change in efficiency solely on the percent change in hours. (The change in hours is net of any change in absenteeism.) The estimated impact on efficiency, though negative, is fairly small and only marginally significant. The regression in Column 2 controls for ΔWar . The war is associated with a very significant positive impact on productivity of 5.6 percent. Productivity now shows an estimated elasticity of –.26 with respect to hours (with a standard error of .07). Lastly, Column 3 interacts Δ War with a zero/one dummy variable, that equals one for the 42 hours changes that are for workers producing goods directly related to the war effort. The impact of the war on productivity is about 8.0 percent for these workers.⁷ The impact of hours on productivity is estimated fairly precisely at an elasticity of –.25 (standard error of .06).

Harbor. 18 are changes during the war. 16 represent changes from before to after VJ Day. 1 occurred entirely after the war.

⁷ Examples of products not directly related to war are dental equipment, tobacco products, candles, and cough drops. The variable Δ War is not significant for these workers.

We take the estimated impact on productivity as a .25 percent decrease for each percent increase in hours. If consumption varies one for one with earnings this implies a value for γ of .25. If consumption is not varying this implies a value for γ of .40. For our benchmark case we choose a value in the middle of this range, setting γ equal to $\frac{1}{3}$. We explore robustness to a wider range of values.

Calibrating Money Demand:

First-order conditions (7) and (8) imply that money demand is proportional to consumption and has an interest rate (i_t) elasticity of -v. There is a very large empirical literature estimating v. We take v = 0.2 as a value in the middle of the range of estimates (e.g., Laidler, 1985). We set the parameter χ equal to .9999. For a value of 0.2 for v and a nominal interest rate of 8 percent this implies a real balance-consumption ratio, $\frac{m_t}{P_t c_t}$, of 0.27. For the United States for 1954 to 1996 the observed ratio for $\frac{m_t}{P_t c_t}$ is 0.24 using M2 and .07 using M1. The small value of $\frac{m_t}{P_t c_t}$ renders the effect of real balances on consumption demand nearly zero.

Table 2 summarizes the parameter values we have discussed in this section. It also lists parameters we have calibrated at values common in the literature, such as labor's share α and the depreciation rate δ .

Estimating the Shocks:

We consider three disturbances to the economy: disturbances to technology A_t , to preferences θ_t , and to the rate of money growth μ_t . We denote a variable's percentage deviation from its steady-state value by adding a circumflex [e.g. $\hat{A}_t = \log(A_t / A)$]. We assume that $S_t = [\hat{A}_t \ \hat{\theta}_t \ \hat{\mu}_t]$ reflects a stationary stochastic process,

(13)
$$S_{t}' = \rho S_{t-1}' + \varepsilon_{t}', \quad \rho = \begin{bmatrix} \rho_{A} & 0 & 0 \\ 0 & \rho_{\theta} & 0 \\ 0 & 0 & \rho_{\mu} \end{bmatrix}, \quad \rho_{A}, \rho_{\theta}, \rho_{\mu} < 1, \quad \varepsilon_{t} = [\varepsilon_{At} \ \varepsilon_{\theta t} \ \varepsilon_{\mu t}]$$

(14)
$$\Theta = E \varepsilon_{t}' \varepsilon_{t}.$$

We estimate this process three ways to be consistent first with a model with flexible wages and constant effort, then with a model with sticky wages and constant effort, and finally with a model with sticky wages with an effort response.

With constant effort we can measure shifts in productivity \hat{A}_t in a conventional manner using the Solow residual. But more generally the Solow residual reflects variations in effort

$$\hat{Y}_t - (1 - \alpha)\hat{K}_t - \alpha\hat{N}_t = \hat{A}_t + \alpha\gamma\hat{\phi}_t$$
.

With flexible wages $\hat{\phi}_t$ is directly related to \hat{n}_t through equations (1), (5), and (6). Under sticky wages, similarly, $E_{t-1}\hat{\phi}_t$ can be directly related to $E_{t-1}\hat{n}_t$ given the wage setting in equation (9). After subtracting $\alpha\gamma E_{t-1}[\hat{\phi}_t]$ from the Solow residual for t, we project what remains on lagged and predetermined variables to construct the variable $E_t\hat{A}_t$. (This is described in greater detail in Appendix B.) Then, given that $E_{t-1}\hat{A}_t$ has the same autocorrelation as \hat{A}_t , we use the series for $E_{t-1}\hat{A}_t$ to estimate ρ_A .

If wages are flexible, preference shifts can be related to observed variables using equations (5) and (6) as $\frac{\theta_t}{1-\theta_t} = \frac{1-\lambda}{1-\gamma} \frac{P_t \tilde{c}_t}{W_t} \frac{1}{1-n_t}$. This parallels Hall (1986), Parkin (1988), and Baxter and King's (1991) use of the static first-order condition to measure preference shocks. If wages are sticky, then this relationship holds in expectation as of *t*-1. As in the treatment of \hat{A}_t , we first use this relationship to construct $E_{t-1}\hat{\theta}_t$, then estimate ρ_{θ} from its autocorrelation.

Lastly, growth rates of the monetary base are used to estimate parameter ρ_{μ} .

The estimation of the three shocks, with results, is described in greater detail in Appendix B. Allowing for sticky wages and variable effort results in slightly smaller, but more persistent, shocks to technology than under flexible wages and constant effort.

4. Results for Cyclical Fluctuations

The cyclical behavior of hours and productivity

We contrast three models with respect to their predictions for how output, consumption, investment, productivity, and prices respond to shocks. The models being: a standard flexible wage model, a model with sticky nominal wages and rationing in the labor market, and the model we have introduced with sticky nominal wages where the labor market clears through endogenous effort. First, however, we examine the behavior of these variables for the U.S. economy with a particular emphasis on the cyclical behavior of productivity.

Table 3 presents the standard deviations, first-order autocorrelations, and contemporaneous correlations with real GDP for the eight series real GDP, consumption, investment, hours, prices, real wage, labor productivity, and the Solow residual (TFP) for the U.S. economy. The series are annual Hodrick-Prescott filtered data for 1954-1996. Prices and the real wage reflect the GDP deflator. The hours series are from the Bureau of Labor Statistics and reflect a correction for changes in the composition of the workforce by age and education.⁸ The series for the real wage, labor productivity, and TFP are corrected in a consistent manner. As has been often documented, variability of hours is nearly as large as that in output, with the standard deviation in the real wage and labor productivity less than half that of hours. Note that fluctuations in hours are actually more persistent than fluctuations in labor productivity or TFP, in contrast to typical

⁸ The adjustments for labor force composition are described in detail in BLS (1993). Without correcting the standard deviation of hours is 2.19 percent instead of 2.01 percent. Without correcting the correlations of labor productivity with output and hours equal .30 and -.21, rather than the corresponding values in Table 3 of .48 and .06.

results for models that have been calibrated. Prices are very countercyclical for the period 1954 to 1996, with a correlation of -.57 with output.

Table 4 presents correlations of the real wage, labor productivity, and the Solow residual with hours, contemporaneously as well as for leads and lags of up to 3 years. Real wages and TFP exhibit contemporaneously correlations of .43 and .45 with hours, but labor productivity and hours are largely uncorrelated. Fluctuations in all three variables dramatically lead fluctuations in hours. For both labor productivity and TFP the correlation at a lead of 2 years is over .5.

Impulse responses for the models

We examine impulse responses to technology, preference and monetary shocks for each of the three models.⁹ First consider a technology shock of one percent. The responses of the flexible wage model with constant effort are given in Figure 2a. These responses are standard. Investment responds much more than consumption and output, with consumption's response being humped shape. The real wage (and labor productivity) responds much more, and much more persistently, than hours.¹⁰

Now consider the response, Figure 2b, for a sticky-wage model with no response in effort ($\gamma = 0$). For the first year, during which the nominal wage is predetermined, the impact on the real wage is simply the opposite of the response of the price level. The price level falls by about 2/3 of a percent. The induced increase in the real wage of 2/3 of a percent is somewhat smaller than the real wage increase under flexible wages of about 0.9 percent. Because employment is demand determined, this leads to a somewhat larger increase in employment and output in the first year.

The response of the model with sticky wages but endogenous effort – Figure 2c – is intermediate to the flexible-wage and standard sticky-wage results. The path for the real wage looks much like the simple sticky wage model. The sticky nominal wage

⁹ Recall that for each model, the persistence of shocks corresponds to the autocorrelation of the shocks estimated from that model. In practice, the differences in persistence of shocks across models is very similar; so this has little impact on the appearance of the impulse responses.

¹⁰ We also examined a flexible-wage model with endogenous effort. Effort moves very little. Bils and Cho (1994) and Burnside, Eichenbaum, and Rebelo (1993) achieve greater movements in effort under flexible wages by adding adjustment costs for hours.

causes the real wage to increase by less than its flexible wage counterpart. This leads to a reduction in the productivity of effort (ϕ_t^{γ}) by 1/4 percent. Hours increase by about 0.6 percent, which is greater than the response of 1/3 percent under flexible wages and smaller than the response of 1 percent under the standard sticky model. Overall, the expansions in output, consumption, and investment look very much like that under completely flexible wages.

Next we examine the responses of these economies to a preference shock reflecting a one-percent increase in θ_i . The responses of the flexible wage economy are given in Figure 3a. The preference shock causes both consumption and investment to expand, with the increase in consumption modestly larger. Output expands about 3/4 percent the first year, declining gradually to be about 0.4 percent above trend in the fifth year. Prices and real wages are countercyclical. Prices fall by 1/2 percent in the first year. Real wages fall by about 1/3 percent initially, but only slightly by the fifth year.

The response of the standard sticky-wage model to the preference shock, an increase in consumption demand, is quite perverse. Looking at Figure 3b, the increase in consumption drives up the demand for real balances causing prices to drop. This, in turn, increases the real wage by about 1/4 percent in the first year. Because the level of technology and the capital stock are unaffected in the first year, this increase in the real wage necessarily generates a fall in employment and output. So an increase in demand for consumption actually results in a contraction in output in the first year, with the increase in consumption more than offset by a drop in investment. As nominal wages adjust investment and output subsequently increase.

Again the response of the sticky wage model with effort – Figure 3c - isintermediate to the other two models. The real wage rises initially, similarly to the simple sticky wage model. But this induces an increase in productive effort at work that increases marginal product of labor. This increase in effort exceeds the increase in real wage and results in an expansion in hours. The increase in hours in the first year is substantially less than for the flexible wage model. But thanks to the increase in effort, output expands nearly as much as under flexible wages. Note that hours and output both peak in the second year of the shock, with hours in particular showing a very strong humped shape response. Furthermore, real wages (and labor productivity) and TFP clearly lead the expansion in hours and output. By the time hours peak TFP is back to normal and the real wage and labor productivity are below trend. The response of the model with sticky wages and endogenous effort to a preference shock is the only example of an impulse response, among the three models and three shocks we consider, that generates productivity leading hours. From Table 3, this is a striking feature of the data.

Lastly we examine responses to a shock of one percent to the monetary growth rate. The impact on the economy with flexible wages is extremely small (no real variable departs as much as .001 percent from its steady-state value), so we skip to the two sticky wage models. Results for the sticky wage model without effort response appear in Figure 4a. The impact on hours and output is very dramatic. The decline in real wages from unexpected money growth creates a transitory increase in hours of about 4 percent and in output of nearly 3 percent. The expansion is almost entirely through investment spending, which increases by about 8 percent. The monetary shock creates a persistent expansion in consumption, but not in output.

With endogenous effort, Figure 4b, the impact of the monetary shock is almost neutralized by the decrease in effort brought about by the decrease in the real wage. Hours still expand significantly by about 2 percent, as opposed to 4 percent. But this increase in hours is largely offset by a decline in effort so that the increase of effective labor in the market is very small. The impact on consumption, investment, and output is also quite small relative to the case of sticky wages with no effort response.

Cyclical moments for the models

In Appendix C we present moments for time series generated from each of the three models. The shocks to the models consist of the technology, preference, and monetary shocks as described in Section 3 and Appendix B. Summarizing the findings there, both the flexible-wage model and the sticky-wage model with varying effort do substantially better matching the data than does the simple sticky-wage model. The sticky-wage with effort model outperforms the flexible wage model in a couple of respects – hours variability and TFP leading the cycle, but is also outperformed in a

couple of dimensions – persistence of hours movements and the contemporaneous correlation of hours and labor productivity.

Welfare costs of wage stickiness

The behavior of consumption expenditure and effective leisure is very similar for our model with sticky wages and variable effort to that under flexible wages. This suggests that the welfare consequences of wage stickiness are far lower for our model than in a standard sticky-wage model. We illustrate for the case of nominal shocks to μ_t . We set ρ_{μ} equal to .68 based on the time series for the monetary base. We set the standard deviation of shocks equal to .46 percent. This is roughly consistent with observed price variability for all the models we consider. (See Appendix B.) Under sticky wages and constant effort, the cost to welfare of the wage rigidity is equivalent to a loss of 0.71 percent of steady-state consumption. (Details on calculating welfare costs are contained in Appendix D.) This is consistent with estimates in Cho, Cooley, and Phaneuf (1997), which range from .05 to 1.2 percent of steady-state output.

For our base model with endogenous effort, with $\gamma = \frac{1}{3}$ and steady-state $\frac{\phi}{\tilde{\phi}}$ equal

to $\frac{3}{2}$, the welfare cost of nominal shocks is only 0.0063 percent of steady-state consumption. Thus the cost is reduced by two orders of magnitude.¹¹ For annual consumption of \$30,000 this translates into a cost of only \$2 per year. It is a longstanding puzzle why wage agreements do not build in more indexing and flexibility. Our model, by allowing an effort response, suggests the cost of wage stickiness may be extremely small. Thus it may require only very small costs of writing wage flexibility into labor arrangements to rationalize sticky wages in practice.

We examined several other parameterizations of the model with endogenous effort. We first let marginal variations in effort be less productive by setting $\gamma = \frac{1}{10}$, while maintaining $\frac{\phi}{\tilde{\phi}}$ equal to $\frac{3}{2}$ (implying $\lambda = .069$). This increases the welfare cost of wage

¹¹ If we do not scale down the monetary disturbances the welfare costs of sticky wages are 6.37 percent of consumption with constant effort, but only 0.06 percent with the effort response.

rigidity to .011 percent of steady-state consumption. The steady-state ratio of $\frac{\phi}{\tilde{\phi}}$ affects the cost of fluctuations in effort. If we make $\frac{\phi}{\tilde{\phi}}$ equal to one, by setting both γ and λ equal to $\frac{1}{3}$, then sticky wages create essentially a zero welfare cost. ("Effective" time in production and consumption are unaffected by sticky wages to a first-order approximation if γ equals λ .) Conversely, holding γ equal to $\frac{1}{3}$, but reducing λ to make $\frac{\phi}{\tilde{\phi}}$ equal to 3 increases the welfare cost to .038 percent of steady-state consumption.

5. Conclusions

We examine the impact of wage stickiness when employment has an effort as well as hours dimension. Despite wages being predetermined, the labor market clears through the effort margin. Sticky wages do create inefficient fluctuations in exertion at work relative to at home. But the consumption-leisure margin is much less distorted than if no response in effort is allowed.

We compare our model quantitatively to two models without an effort margin, one with flexible wages and one with sticky wages. Movements in real wages for our model behave very much like real wages in the typical sticky wage setting. Fluctuations in hours worked are intermediate to their behavior in the standard flexible-wage and sticky-wage models. Finally, output and consumption behave much like in the flexible-wage economy. Consequently, welfare costs of wage stickiness appear to be much smaller, by two orders of magnitude, if one allows an effort dimension. This result may help explain the apparent lack of short-run flexibility in actual wage practices.

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Appendix A: Energy requirements for activities

Table A1, reproduced from Fogel and Floud (1991), presents energy requirements for a number of activities. The calorie requirements for an activity are measured by its impact on a basal metabolic rate (BMR). They are expressed relative to the BMR for sleeping. The BMR is the amount of energy (calories) required to maintain the body while at rest in terms of body temperature and the functioning of organs. It is probably reasonable to assume that exertion for most leisure activities fall in the range of standing quietly and strolling. These two activities have respective BMR impacts of 1.4 and 2.5. Most of the work activities in Table A1 generate larger energy requirements. Some of the work activities have far higher energy requirements, though these (felling trees, collecting and spreading manure) may not be that relevant for the postwar U.S. economy.

Appendix B: Estimating the Models' Shocks:

The three disturbances to technology, preferences, and the rate of money growth are described by equations (13) and (14) of the text.

As discussed in the text, with variable effort the Solow residual reflects variations in effort as well as technology \hat{A}_t ,

$$\hat{Y}_t - (1 - \alpha)\hat{K}_t - \alpha\hat{N}_t = \hat{A}_t + \alpha\gamma\hat{\phi}_t \quad .$$

Under sticky wages, optimal wage setting in equation (9) yields an implied value for $E_t \hat{\phi}_{t+1}$. Intuitively, W_{t+1} is set such that the expectation of $\frac{\phi_{t+1}}{\tilde{\phi}_{t+1}}$ reflects its flexible wage counterpart of $\frac{\gamma(1-\lambda)}{\lambda(1-\gamma)}$. For $\gamma \neq \lambda$ this implies small movements in $E_t \hat{\phi}_{t+1}$ to satisfy energy constraint (1). We subtract $\alpha \gamma E_t \hat{\phi}_{t+1}$ from the Solow residual at time t+1 to yield a variable with expectation at time t equal to $E_t \hat{A}_{t+1} = \rho_A \hat{A}_t$. We construct the expectation of the corrected t+1 Solow residual based on a projection on variables $\{\hat{Y}_t, \hat{Y}_{t-1}, \hat{N}_t, \hat{N}_{t-1}, \hat{K}_{t+1}, \hat{K}_t, \hat{K}_{t-1}, (\frac{\hat{W}_{t+1}}{W_t}), (\frac{\hat{W}_t}{W_{t-1}})\}$ to obtain $E_t \hat{A}_{t+1}$. We then estimate $\hat{\rho}_A$ from the first-order autocorrelation of $E_t \hat{A}_{t+1}$, which equals the autocorrelation of \hat{A}_t . Finally, we divide $E_t \hat{A}_{t+1} (= \rho_A \hat{A}_t)$ by $\hat{\rho}_A$ to obtain our time series for \hat{A}_t . Under flexible wages, first order conditions (5) and (6) reveal the preference shifts θ_t as $\frac{\theta_t}{1-\theta_t} = \frac{1-\lambda}{1-\gamma} \frac{P_t \tilde{e}_t}{W_t} \frac{1}{1-\theta_{t+1}} = \frac{1-\lambda}{1-\gamma} \frac{P_{t+1} \tilde{e}_{t+1}}{W_{t+1}} = \frac{1-\lambda}{1-\gamma} \frac{P_{t+1} \tilde{e}_{t+1}}{W_{t+1}}$

$$E_t \hat{\theta}_{t+1} = (1-\theta) E_t \left[\frac{n}{1-n} \hat{n}_{t+1} + \hat{\tilde{c}}_{t+1} - (\frac{\hat{W}}{P})_{t+1} \right].$$

Note $E_t[\hat{\theta}_{t+1}]$ has the same autocorrelation as $\hat{\theta}_t = \rho_{\theta}^{-1} E_t[\hat{\theta}_{t+1}]$. We use predicted values from regressing $\hat{\theta}_{t+1}$ on $\{\hat{n}_t, \hat{n}_{t-1}, \hat{c}_t, \hat{c}_{t-1}, (\frac{\hat{W}}{P})_t, (\frac{\hat{W}}{P})_{t-1}, \hat{K}_{t+1}, \hat{K}_t, \hat{K}_{t-1}, (\frac{\hat{W}_{t+1}}{W_t}), (\frac{\hat{W}_t}{W_{t-1}})\}$ to obtain $E_t[\hat{\theta}_{t+1}]$. Similarly to the treatment of \hat{A}_t , we use the first-order autocorrelation of $E_t[\hat{\theta}_{t+1}]$ to estimate ρ_{θ} , then divide $E_t[\hat{\theta}_{t+1}]$ by ρ_{θ} to obtain a series for $\hat{\theta}_t$. (We proceed in a similar manner for the model with sticky wages but no effort choice.)

Growth rates of the monetary base are used to estimate the stochastic process for $\hat{\mu}_t$. We find that for every model considered this leads to far more volatility in prices and inflation rates than we see in the data. For this reason, we scale down the monetary disturbances to one-third their estimated size.

Given the series for $\{\hat{A}_t, \hat{\theta}_t, \hat{\mu}_t\}$, the stochastic process (13)-(14) is estimated by OLS using annual data for the United States for 1954-1996. Linear time trends are included. Estimates for ρ and Θ are as follows (with the monetary innovation scaled to one third). Under flexible wages,

$$\hat{\rho} = \begin{bmatrix} .90 & & & \\ 0.06) & & & \\ 0 & .84 & & \\ 0 & (.09) & & \\ 0 & 0 & .68 \\ & & & (.15) \end{bmatrix}, \quad \hat{\Theta}^{1/2} = 10^{-2} \begin{bmatrix} 1.45 & .12 & .07 \\ .12 & 1.41 & -.06 \\ .07 & -.06 & .45 \end{bmatrix},$$

under sticky wages,

_

$$\hat{\rho} = \begin{bmatrix} .90 & & & \\ 0.06) & & & \\ 0 & .86 & & \\ 0 & (.09) & & \\ 0 & 0 & .68 \\ & & & (.15) \end{bmatrix}, \quad \hat{\Theta}^{1/2} = 10^{-2} \begin{bmatrix} 1.27 & .47 & .06 \\ .47 & 1.47 & .00 \\ .06 & .00 & .45 \end{bmatrix},$$

and under sticky wages with endogenous efforts,

$$\hat{\rho} = \begin{bmatrix} .93 & & & & 0 \\ (.06) & & & & \\ 0 & .86 & & & \\ & (.09) & & & \\ 0 & & & & .68 \\ & & & & (.15) \end{bmatrix}, \quad \hat{\Theta}^{1/2} = 10^{-2} \begin{bmatrix} 1.43 & .23 & .05 \\ .23 & 1.53 & .01 \\ .05 & .01 & .45 \end{bmatrix}.$$

Appendix C: Cyclical moments for the models

We now compare the moments for time series generated from each of the three models to those reported for U.S. data in Table 4. The generated series are also H-P filtered. The shocks to the models consist of the technology, preference, and monetary shocks estimated under each model, as described in Appendix B.

Results for the flexible wage model are contained in Tables A2 and A3. The model generates fluctuations in output and hours that are respectively .8 and .75 times the size of those observed in the data. Labor productivity, by contrast, is somewhat more volatile for the model than in actual data. The model generates persistent movements in real variables, though, with the exception of labor productivity, not as persistent as in the data. The model generates much less persistent movements in prices than we see in the data. This statement holds as well for the other two models we consider. From Table A3 we see that the model generates contemporaneous correlations of labor productivity and TFP with hours of respectively -.01 and .41. These are quite close to those estimated for U.S. data (.06 and .45). For the model movements in labor productivity and TFP modestly lag movements in hours. In the data, as discussed in the text, they very strongly lead hours.

Results for sticky wages with constant effort appear in Tables A4 and A5. Output and particularly hours are more variable for the model than in the data. The sticky-wage model, even augmented with technology and preference shocks, performs very poorly in terms of the persistence of the economic time series. This is particularly true for hours, which display a first-order correlation of .53 in the data but only .04 for the sticky wage model. (This problem is well known in the literature. For a recent discussion see Chari, et. al., 1996.) Turning to Table A5, the correlation between TFP and hours, .43, is very close to the correlation of .45 for the data. But unlike the data, hours and labor productivity are quite negatively correlated, with correlation of -.39 compared to .06 for the data. Also, in contrast to the data, fluctuations in labor productivity lag fluctuations in hours.

Finally, we present results for the model with sticky wages but varying effort in Tables A6 and A7. Broadly speaking, the time-series properties of this model are similar to those of the flexible wage model. Hours and output are somewhat more volatile than for the flexible wage model, and therefore are a little closer to the volatility depicted in Table 3 for the U.S. economy. Looking at Table A7, the model generates a contemporaneous correlation between hours and labor productivity of -.20 and between hours and TFP of .18 Both correlations fall below those for the flexible wage model and below those for the data. This model does generate fluctuations in labor productivity and, in particular, in TFP that lead those in hours worked. But this behavior is not as striking for the model as what we observe in the data. If we consider alternative parameters for the model that strengthen the importance of preference shocks, for example by reducing the elasticity response of labor supply, this creates a stronger leading pattern in labor productivity and TFP. But it also makes the contemporaneous correlation between hours and labor productivity more negative, in contradiction of the data.

Appendix D: Welfare costs of wage stickiness

Monetary disturbances are essentially neutral with respect to flexible-wage versions of the model. Therefore, for monetary disturbances, the welfare cost of sticky wages can be measured based on the economy's deviations from its steady state. Let \overline{U} denote the lifetime utility associated with consumption of goods, real balance, and leisure for the economy calculated at its steady-state level. Similarly, let U_s denotes lifetime utility for the realized economy under sticky wages. Then

$$\hat{U} = U_s - \overline{U} = \sum_{\tau=0}^{\infty} \beta^{\tau-t} E_t[\hat{u}_{\tau}]$$
, where \hat{u}_t is the utility cost incurred in t. Let D_s represent

the welfare cost from sticky wages in consumption units, so that $\log(x - D_s) - \log x = \hat{U}$. We can express D_s in terms relative to steady-state consumption as $\frac{D_s}{x} = 1 - e^{\hat{U}}$. Ignoring money balances, which are unimportant, the period *t* utility cost can be written

$$E[\hat{u}_t] = E[\theta \log c_t + (1-\theta)\log \tilde{l}_t] - [\theta \log c + (1-\theta)\log \tilde{l}],$$

where c and \tilde{l} are steady state values. Its second-order Taylor approximation is

$$E[\hat{u}_t] \approx \frac{\theta}{c} E(c_t - c) + \frac{1 - \theta}{\tilde{l}} E(\tilde{l}_t - \tilde{l}) - \frac{1}{2} \frac{\theta}{c^2} E(c_t - c)^2 - \frac{1}{2} \frac{1 - \theta}{\tilde{l}^2} E(\tilde{l}_t - \tilde{l})^2].$$

Generally speaking, $E[c_t] \neq c$ under sticky wages. We approximate $E[c_t]$ as follows (ignoring productivity shifts).

$$\begin{split} E[c_t] &\approx S_c E[y_t] = S_c E[L_t(\frac{K}{L})_t^{1-\alpha}] \\ &\approx S_c E[L(\frac{K}{L})^{1-\alpha} + (\frac{K}{L})^{1-\alpha}(L_t - L) + L(1-\alpha)(\frac{K}{L})^{-\alpha}((\frac{K}{L})_t - \frac{K}{L}) \\ &- \frac{1}{2}\alpha(1-\alpha)L(\frac{K}{L})^{-\alpha-1}((\frac{K}{L})_t - \frac{K}{L})^2 + (1-\alpha)(\frac{K}{L})^{-\alpha}((\frac{K}{L})_t - \frac{K}{L})(L_t - L)] \end{split}$$

where $L_t = N_t \Phi_t^{\gamma}$. Finally, \hat{u}_t can be expressed in terms of percentage deviations of variables from steady-state as

$$E[\hat{u}_t] \approx -\frac{1}{2} \theta E[\hat{c}_t]^2 - \frac{1}{2} (1-\theta) E[\hat{\tilde{l}}_t]^2 - \frac{1}{2} \theta S_c \alpha (1-\alpha) E[(\frac{\hat{K}}{L})_t]^2 + \theta S_c (1-\alpha) E[(\frac{\hat{K}}{L})_t \hat{L}_t].$$

	Column 1	Column 2	Column 3
Intercept	cept .047 (.011)		.042 (.008)
$\frac{\Delta Hours}{Hours}$	123 (.065)	264 (.069)	250 (.059)
∆War		.056 (.014)	
Δ War•War related			.080 (.015)
\overline{R}^2	.04	.22	.34
Ν	62	62	62

Table 1 – Response of Productivity to Hours Worked

Parameters	Description
$\alpha = 2/3$	Labor share in output
$\beta = 0.98$	Discount factor
$\delta = 0.1$	Depreciation rate
g = 0.02	Growth rate of technological progress
$\xi = 1$	Labor supply elasticity
n = 0.5	Steady-state hours of work
$\phi / \widetilde{\phi} = 3/2$	Ratio of effort in the market and home
$\gamma = 1/3$	Ability to substitute hours and effort in the market
$\lambda = 1/4$	Ability to substitute hours and effort at home
υ = .2	Interest rate elasticity of money demand
χ = .9999	Relative share of consumption in utility
$\theta = 0.5486$	Steady-state value in preference

Table 2 – Parameter Values for the Benchmark Case

Variable (x)	σ _x	σ_x / σ_{output}	$Cor(x_t, x_{t-1})$	Cor(x, output)
Output	2.29	1.00	.57	1.00
Consumption	1.32	.58	.67	.88
Investment	6.39	2.79	.41	.83
Hours	2.01	.88	.53	.91
Price	.97	.42	.81	57
Real wage	.94	.44	.48	.49
Labor productivity	.97	.42	.46	.48
Solow residual	1.29	.57	.45	.82

Table 3 – Volatility, persistence, and cyclicality: U.S. time series 1954-1996[#]

Table 4 – Lead and Lag correlations with hours at t.

Variable (x)	x(t-3)	x(t-2)	x(t-1)	x(t)	x(t+1)	x(t+2)	X(t+3)
Real wage				.43		36	28
Real wage Labor productivity	.14	.54	.65	.06	38	23	14
Solow residual	.16	.51	.76	.45	28	46	39

[#] Output: real GDP. Consumption: expenditure on non-durables and services. Investment: fixed investment. Hours: employed man-hours. Real wage: average hourly earning. Labor productivity: output divided by hours. Quantities are divided by population of age over 20. All variables are annual and H-P filtered with the weight parameter 100.

Activity	Men	Women
Sleeping	1.0	1.0
Standing quietly	1.4	1.5
Strolling	2.5	2.4
Walking at normal pace	3.2	3.4
Walking with 10-kg load	3.5	4.0
Walking uphill at normal pace	5.7	4.6
Sitting and sewing	1.5	1.4
Sitting and sharpening machete	2.2	_
Cooking	1.8	1.8
Tailoring	2.5	-
Carpentry	3.5	_
Common labor in building trades	5.2	_
Milking cows by hand	2.9	_
Hoeing	-	5.3-7.5
Collecting and spreading manure	6.4	_
Binding sheaves	5.4-7.5	3.3-5.4
Uprooting sweet potatoes	3.5	3.1
Weeding	2.5-5.0	2.9
Ploughing	4.6-6.8	2.2
Cleaning House	_	2.2
Child care	_	2.2
Threshing	-	4.2
Cutting grass with machete	_	5.0
Laundry work	_	3.4
Felling trees	7.5	_

Table A1 – Energy Requirements for Activities as a Multiple of the Basal Metabolic Rate, from Fogel and Floud (1991)

Sources are FAO/WHO (1985) and Durnin and Passmore (1967).

Variable (x)	ariable (x) $\sigma_x = \sigma_x / \sigma_{output}$		$Cor(x_t, x_{t-1})$	Cor(x, output)		
Output	1.88	1.00	.40	1.00		
Consumption	1.31	.70	.44	.93		
Investment	3.74	1.98	.36	.94		
Hours	1.50	.79	.36	.78		
Price	1.29	.69	.49	70		
Labor productivity	1.17	.62	.46	.59		
TFP	1.24	.65	.38	.86		

Table A2 – Volatility, persistence, and cyclicality: Flexible wages

Table A3 – Lead and lag correlations with hours at t: Flexible wages

	-								
Variable (x)	x(t-3)	x(t-2)	x(t-1)	X(t)	x(t+1)	X(t+2)	x(t+3)		
Labor productivity	13	15	12	01	.10	.16	.14		
TFP	15	09	.09	.41	.19	.07	.00		

Variable (x)	σ _x	σ_x / σ_{output}	$Cor(x_t, x_{t-1})$	Cor(x, output)		
Output	2.49	1.00	.27	1.00		
Consumption	1.43	.57	.48	.75		
Investment	6.39	2.56	.05	.93		
Hours	2.70	1.08	.04	.88		
Price	1.17	.47	.54	56		
Labor productivity	1.26	.51	.15	.07		
TFP	1.20	.48	.38	.77		

Table A4 – Volatility, persistence, and cyclicality: Sticky wages & constant effort

Table A5 – Lead and lag correlations with hours at t: Sticky wages & constant effort

Variable (x)	x(t-3)	x(t-2)	x(t-1)	X(t)	x(t+1)	x(t+2)	x(t+3)
Labor productivity	08	.02	.09	39	.26	.21	.09
TFP	11	.01	.23	.43	.19	.01	07

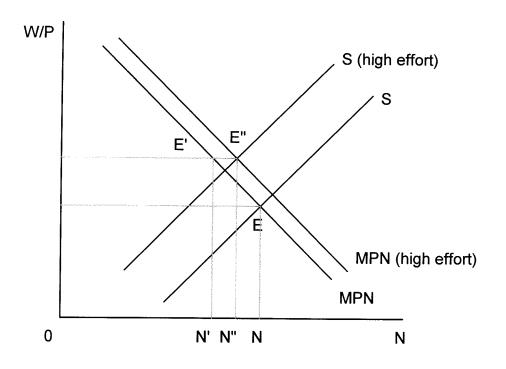
Variable (x)	iable (x) $\sigma_x = \sigma_x / \sigma_{output}$		$Cor(x_t, x_{t-1})$	Cor(x, output)
Output	2.09	1.00	.44	1.00
Consumption	1.53	.73	.48	.94
Investment	3.89	1.86	.38	.93
Hours	1.76	.85	.25	.68
Price	1.41	.67	.54	75
Labor productivity	1.54	.74	.18	.56
TFP	1.51	.72	.27	.82

Table A6 – Volatility, persistence, and cyclicality: Sticky wages & effort response

Table A7 – Lead and lag correlations with hours at *t*: Sticky wages & effort response

Variable (x)	x(t-3)	x(t-2)	x(t-1)	X(t)	X(t+1)	x(t+2)	x(t+3)
Labor productivity						.11	.08
TFP	05	.06	.31	.18	.14	.03	04

Figure 1 Labor market equilibrium: sticky wage with effort



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Figure 2a Impulse response to 1% increase in productivity shock: flexible wage

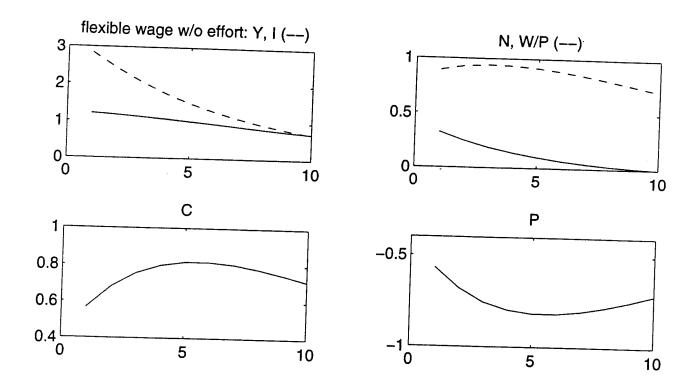
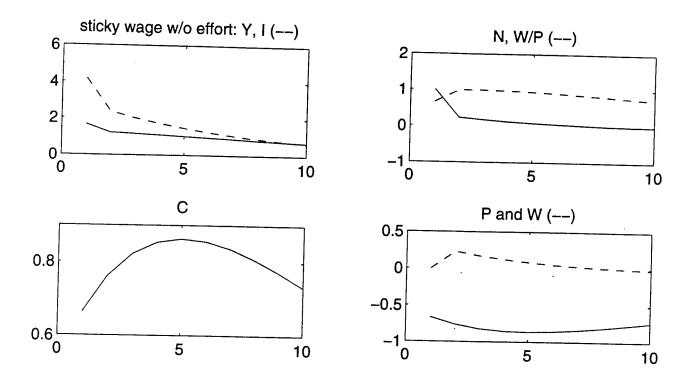
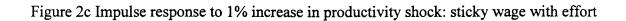


Figure 2b Impulse response to 1% increase in productivity shock: sticky wage





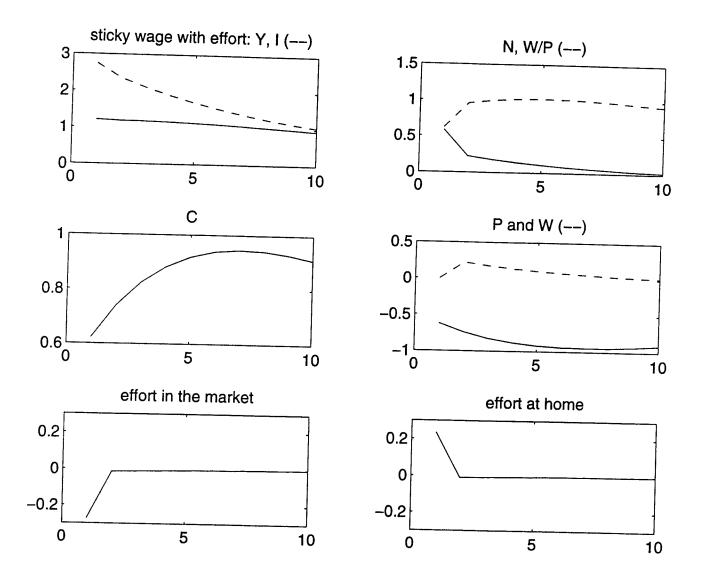


Figure 3a Impulse response to 1% increase in preference shock: flexible wage

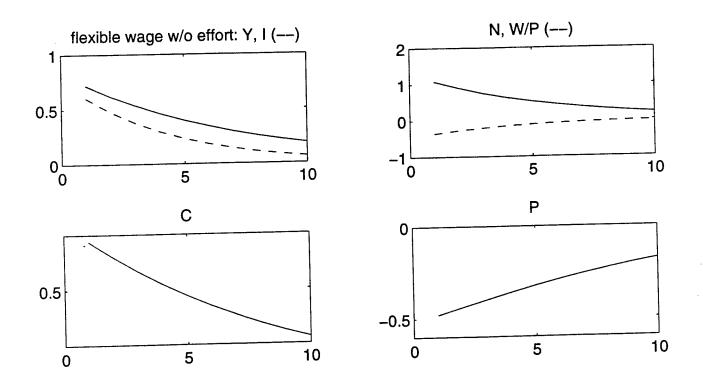


Figure 3b Impulse response to 1% increase in preference shock: sticky wage

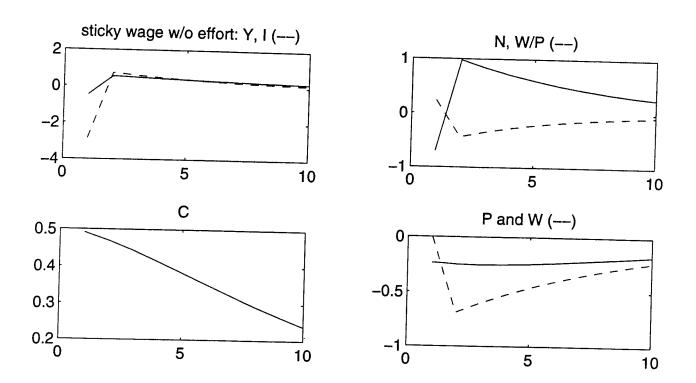


Figure 3c Impulse response to 1% increase in preference shock: sticky wage with effort

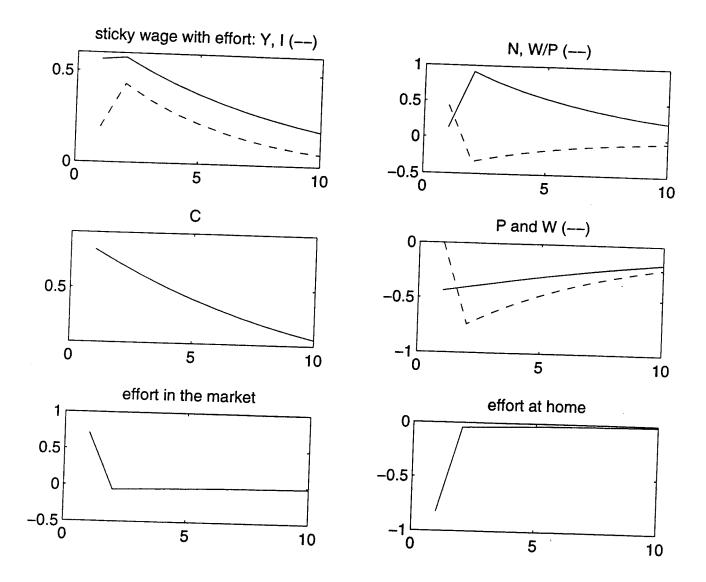


Figure 4a Impulse response to 1% increase in money growth: sticky wage

