

**Question A:** Imagine a world with the aggregate production function

$$y = \kappa k^\alpha l^{1-\alpha}.$$

There is one unit of labor in economy. Let the *quarterly* rate of time preference be 0.01. Similarly, take the *quarterly* rate of depreciation to be 0.015. The stock of labor in the economy is one.

1. Assume that the economy is in a steady state. Compute the capital stock.
2. Take the time period to be *one year*. Redo the above calculation. Is your capital stock the same? (Assume that  $(1 + x)^n = 1 + nx$  for small  $n$  and  $x$ .)
3. What is the issue here?

**Question B:** Consider the following optimization problem:

$$V(y) = \max_{k_1, k_2} \{\ln c + \beta V(y')\},$$

subject to

$$c + k'_1 + k'_2 = y,$$

and

$$y' = x(k'_1)^\alpha + z(k'_2)^\alpha,$$

where  $x$  is a constant and  $0 < \alpha, \beta < 1$ . The random variable  $z \in \{z^l, z^h\} \subset \mathcal{R}_+$  is distributed as follows:

$$\Pr[z = z^i] = 1/2 \text{ for } i = l, h.$$

Characterize the solution for the decision rules for  $k'_1$  and  $k'_2$ . What is the solution for consumption? How does income evolve over time?