The Generalized Multinomial Logit Model

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Abstract: The so-called "mixed" or "heterogeneous" multinomial logit (MIXL) model has become popular in a number of fields, especially Marketing, Health Economics and Industrial Organization. In most applications of the model, the vector of consumer utility weights on product attributes is assumed to have a multivariate normal (MVN) distribution in the population. Thus, some consumers care more about some attributes than others, and the IIA property of multinomial logit (MNL) is avoided (i.e., segments of consumers will tend to switch among the subset of brands that possess their most valued attributes). The MIXL model is also appealing because it is relatively easy to estimate. But recently Louviere et al (1999, 2008) have argued that the MVN is a poor choice for modelling taste heterogeneity. They argue that much of the heterogeneity in attribute weights is accounted for by a pure scale effect (i.e., across consumers, all attribute weights are scaled up or down in tandem). This implies that choice behaviour is simply more random for some consumers than others (i.e., holding attribute coefficients fixed, the scale of their error term is greater). This leads to what we call a "scale heterogeneity" MNL model (or S-MNL). Here, we develop a "generalized" multinomial logit model (G-MNL) that nests S-MNL and MIXL. By estimating the S-MNL, MIXL and G-MNL models on ten datasets, we provide evidence on their relative performance. We find that models that account for scale heterogeneity (i.e., G-MNL or S-MNL) are preferred to MIXL by the Bayes and consistent Akaike information criteria in all ten data sets. Accounting for scale heterogeneity enables one to account for "extreme" consumers who exhibit nearly lexicographic preferences, as well as consumers who exhibit very "random" behaviour (in a sense we formalize below).

Keywords: Choice models, Mixture models, Consumer heterogeneity, Choice experiments

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I. Introduction

It is well known that consumer choice behaviour exhibits substantial heterogeneity. In choice modelling, adequate modelling of heterogeneity is important for many reasons. Most obviously, estimates of own and cross price elasticities of demand may be severely biased if one does not properly account for taste heterogeneity. More subtle and interesting, perhaps, are issues that arise with respect to new product development (NPD), product positioning and advertising, optimal price discrimination strategies, the development of menus of product offerings, and considerations of product image and/or brand equity.

For example, in NPD, the estimation of only average preferences, as in a simple multinomial logit model – or, more generally, the mis-specification of the heterogeneity distribution – may lead a researcher to miss the fact that a significant subset of the population would have great demand for a product with particular attributes. Similarly, correct welfare analysis requires correct modelling of taste distributions. Or, failure to properly understand the nature of taste heterogeneity may lead to failure to optimally target advertising that stresses certain product features to groups that favour those features. Also, there are many instances where one cares at least as much about the composition of buyers by type as about market share (e.g., any insurance or usage fee based product where profits/revenues depend on subsequent usage, not just on purchase). Many more examples could be provided.

For at least 25 years there has been a large ongoing research program in marketing on alternative ways to model consumer heterogeneity. As Keane (1997a, b) discusses, the traditional multinomial logit (MNL) of McFadden (1974) and multinomial probit (MNP) of Thurstone (1927) have an asymmetric heterogeneity structure, as they can be motivated by assuming consumers have heterogeneous tastes for the *unobserved* (or unmeasured or intangible) attributes of products, but common tastes for the *observed* attributes. Much recent work has focussed on extending these models to also allow for heterogeneous tastes over observed attributes as well.

For example, the heterogeneous or "mixed" logit (MIXL) model is currently quite popular (see, e.g., Ben-Akiva and McFadden et al (1997), McFadden and Train (2000), Dube, Chintagunta, et al. (2002)). MIXL extends MNL to allow for random coefficients on the observed attributes, while continuing to assume the "idiosyncratic" error is iid extreme value. While the researcher has great latitude in specifying distributions for the random attribute coefficients, the multivariate normal is used in most applications of which we are aware. [An exception is the price coefficient, which is often modelled as log normal to impose the constraint that it be negative.] Indeed, it is common in the literature to call the MNL with a

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normal heterogeneity distribution <u>the</u> mixed logit (MIXL) model (see, e.g. Dube, Chintagunta et al. (2002), p. 210). Even when other distributions have been considered, computational problems often led researchers to revert back to an assumption of normality (see, e.g. Bartels et al 2006) and Small et al (2005)).

Of course, one can also estimate multinomial probit (MNP) models with normally distributed attribute weights, using the GHK simulator to evaluate the choice probabilities (see Keane (1994, 1997b)). However, the popularity of the MIXL stems from its greater ease of use (i.e., GHK is harder to program, and MIXL procedures are now available in standard estimation software packages). Thus, the use of MNP has been mostly limited to more sophisticated academic users, while various logit models are widely used by practitioners.

One could also specify a discrete distribution for heterogeneity in either the MNL or MNP. This leads to what is known as the "latent class" (LC) model (see, e,g., Kamakura and Russell (1989)). Most applications of LC have used MNL as the base model, again based on ease of use. LC models typically generate a few discrete "types" of consumers. Part of the appeal of this approach is that one can "name" the types (e.g., couch potatoes, trend setters) leading to easier interpretation of market segments (see, e.g., Wedel and Kamakura (1998)). On the other hand, work by Elrod and Keane (1995) and Allenby and Rossi (1998) suggests that latent class models understate the extent of heterogeneity in choice data.

Other ways of capturing heterogeneity have been proposed, such as Harris and Keane (1999), who extended the heterogeneous logit model to allow the means of the random coefficients to depend on observed characteristics of consumers – in particular, attitudinal questions about how much they value the different attributes. They found this led to dramatic improvements in model fit (i.e., doubling of pseudo R-squared). In general, however, it would seem that choice modellers have favored models that rely largely or exclusively on unobserved heterogeneity, largely abandoning attempts to explain heterogeneous tastes using observables. To be fair, this is partly due to the rather limited set of consumer characteristics recorded in most data sets used in choice modelling.

Recently, Louviere et al (1999), Louviere, Carson, et al (2002), Louviere and Eagle (2006), Meyer and Louviere (2007) and Louviere et al (2008) have argued that the normal mixing distribution commonly used in the MIXL model is seriously mis-specified. Instead, they argue that much of the taste heterogeneity in most choice contexts can be better described as "scale" heterogeneity – meaning that for some consumers the scale of the idiosyncratic error component is greater than for others. However, the "scale" or standard deviation of the idiosyncratic error is not identified in discrete choice data – a problem that is

typically resolved by normalizing the standard deviation of the idiosyncratic error component to a constant. Thus, the statement that all heterogeneity is in the scale of the error term is observationally equivalent to the statement that heterogeneity takes the form of the vector of utility weights being scaled up or down proportionately as one "looks" across consumers.

It is important to note that the scale heterogeneity model is <u>not</u> nested within the heterogeneous logit with normal mixing. It might appear that the scale model is a limiting case of MIXL in which the attribute weights are perfectly correlated. However, the scale parameter must be positive for all consumers, so, while attribute weights may vary in the population, for all consumers they must have the same sign. A normal mixture model with perfectly correlated errors does not impose this constraint. What is clear is that MIXL with *independent* normal mixing is likely to be a poor approximation to the data generating process if scale heterogeneity is important. MIXL with correlated random coefficients may or may not provide a better approximation – an empirical question we address below.

Consider then the more general case in which there is <u>both</u> scale heterogeneity and residual normally distributed taste heterogeneity that is independent of the variation induced by scale. In that case, the heterogeneous logit model with normal mixing is clearly mis-specified. For example, suppose the utility weight on attribute k, $k=1,…,K$, for person n, $n=1,…N$, is given by $\beta_{nk} = \sigma_n \beta_k + \varepsilon_{nk}$ where β_k is the population mean utility weight on attribute k, σ_n is the person n specific scaling parameter, which for illustration we assume is distributed log normally, and ε_{nk} is what we will call "<u>residual" heterogeneity</u> not explained by scale heterogeneity. Assume that ε_{nk} is distributed normally. Then, if one writes $\beta_{nk} = \beta_k + \upsilon_{nk}$ as in the conventional MIXL model, the error term $\upsilon_{nk} = \beta_k(\sigma_n - 1) + \varepsilon_{nk}$ is itself a complex mixture of normal and lognormal errors (with the nature of the mixing depending on the unknown mean parameter vector β_k). Thus, the normal mixing model is mis-specified.[1]

There are a number of possible responses to this problem. Some researchers have argued for the estimation of individual level models, which circumvent the need to specify a heterogeneity distribution (see Louviere et al (2008), Louviere and Eagle (2006), Meyer and Louviere (2007)). However, this approach makes stringent requirements of the data. In revealed preference data one rarely has enough observations per individual to estimate individual level models. But, as shown by Louviere et al (2008), it is possible to estimate

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[1] McFadden and Train (2000) show heterogeneous logit can approximate any random utility model arbitrarily well. But this result relies on the investigator using the correct mixing distribution – which needs to be specified *a priori*. Unfortunately, their result seems to be widely misinterpreted among practitioners to mean that the heterogeneous logit with <u>normal</u> mixing can approximate any random utility model, which is certainly not true. Indeed, the correct mixing distribution only happens to be multivariate normal in the case of the MNP model.

individual level models from stated preference data obtained using efficient experimental designs. Their results suggest that distributions of preference weights generally depart substantially from normality. Nevertheless, models are by definition only approximations to "reality," so if estimation of individual models is not feasible, it remains an empirical matter whether assuming normality for preference weights is or is not a good modelling choice.

The hierarchical Bayes (HB) approach to choice modelling has also become popular recently, in part because advances in simulation methods (MCMC) made it computationally practical (see Allenby and Rossi (1998), Geweke and Keane (2001)). In the HB approach, the ease of use advantage for MIXL vanishes, so both MNP and MIXL are widely used.[2] An appeal of HB is that, by specifying weak priors that individual level parameters are normally distributed, one can allow considerable flexibility in their *posterior* distribution. However, as Allenby and Rossi (1998) note, HB procedures "shrink" individual level estimates toward the prior. And as Rossi, Allenby and McCulloch (2005 p. 142) note, "the thin tails of the normal model tend to shrink outlying units greatly toward the center of the data." Thus, if one shrinks toward a normal prior, when the "true" heterogeneity distribution departs substantially from normality, it may result in unreliable inferences about the heterogeneity. A very large amount of data per person may be necessary before the data "overwhelms" the prior and gives reliable inferences about individual level parameters and the shape of their distribution.

In response to this problem, a literature has emerged on using mixtures-of-normal distributions to generate flexible priors that can potentially accommodate a wide range of non-normal posterior distributions. This approach, known as "Bayesian non-parametrics," originated with Ferguson (1973) for density estimation. It has been extended to probit models by Geweke and Keane (1999, 2001), and to MIXL models by Rossi, Allenby and McCulloch (2005) and Burda, Harding and Hausman (2008).[3] Figure 5.7 in Rossi et al (2005) provides a nice illustration of how much more flexible the distribution of household posterior means can

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[2] Indeed, as noted in Train (2003, p. 316), MNP is actually somewhat computationally easier, because it has the same distribution (normal) for both the attribute weights and the idiosyncratic errors.

[3] In mixture-of-normals models there is probability of drawing from each class in the mixture, and *one must put a prior on that probability vector*. Some authors have adopted the Dirichlet process prior (DPP), which says there may be a countably infinite number of classes, but which is typically specified to put more prior mass on models with fewer classes. This is the approach invented by Ferguson (1973), and recently extended to MIXL models by Burda et al (2008). A second approach is to assume a fixed number of classes, and put a Dirichlet (i.e., multivariate Beta) distribution on the vector of type probabilities. This is the approach adopted in Geweke and Keane (1999, 2001) and Rossi et al (2005). In practice there is no fundamental difference between these approaches. This is true because (i) in the second method one can consider models with different numbers of classes and compare them based on the marginal likelihood or posterior odds, and (ii) in the first approach inference invariably puts essentially all mass on a fairly small number of types anyway. The two kinds of prior on the hyper-parameters of the Dirichlet distribution thus in practice produce essentially identical results, and the real point of this literature is the use of the mixture-of-normals specification.

become in a mixture-of-normals model.[4] Of course, one can also adopt a mixture-of-normals specification for the heterogeneity distribution within the classical framework.

Here, we propose an alternative approach to modelling heterogeneity that stays within the classical framework and retains the simplicity of use of MIXL, while extending it to accommodate both scale and "residual" taste heterogeneity. We show how to nest the MIXL model and the MNL model with scale heterogeneity (S-MNL) within a single framework. We refer to this new model as the "generalized multinomial logit model," or G-MNL. Estimating the G-MNL model allows one to assess whether including scale heterogeneity leads to a significant improvement in fit over the conventional MIXL model in any given data set.

Although not immediately obvious, G-MNL is closely related to mixture-of-normals models. The relation becomes clear if we adopt an "approximate Bayesian" perspective and use our estimated model to calculate person specific parameters *a posteriori* (see Train (2003), chapter 11). Then, the estimated heterogeneity distribution plays the same role as the prior in the Bayesian framework. One can interpret our model as allowing a more flexible prior on the distribution of individual level parameters than does a normal model, but via a different means than the standard discrete mixtures-of-normals approach. Specifically, G-MNL implies the attribute coefficients are a continuous mixture of scaled normals.

We apply G-MNL to data from ten different stated preference choice experiments. The experiments cover several different types of choices: choices about medical procedures, mobile phones, food delivery services, holiday packages and charge cards. We also estimate MIXL and S-MNL on each data set, and compare the performance of the three models using three information criteria: the Akaike criteria (AIC), Bayes criterion (BIC) and consistent Akaike criterion (CAIC), all of which penalize models with more parameters.

Our main finding is that models that include scale heterogeneity are preferred over MIXL by both BIC and CAIC in all ten data sets: G-MNL in 7 and S-MNL in 3. The MIXL model is only (very slightly) preferred by the AIC for the two charge card data sets. But our Monte Carlo results indicate that BIC and CAIC are more reliable measures for determining if scale heterogeneity is present.[5] Interestingly, among practitioners the MIXL model with

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[4] Recently, Geweke and Keane (2007) introduced the "smoothly mixing regression" (SMR) model in which the class probabilities in a mixture-of-normals model are determined by a multinomial probit. The key advantage of this approach is it allows class probabilities to depend on covariates, which is critical for modelling nonstationary processes. SMR is closely related to what are known as "mixture of experts" models in statistics (see Jiang and Tanner (1999), Villani, M., R. Kohn and P. Giordani (2007)).

[5] We find the following difference among the information criteria: in all 7 cases where G-MNL is preferred by all three, AIC prefers the full G-MNL model that includes correlated errors (i.e., correlated residual taste heterogeneity). But in 5 of these 7 cases the BIC and CAIC, which impose larger penalties for adding parameters, prefer a more parsimonious version of G-MNL with uncorrelated errors. We present Monte Carlo

uncorrelated errors is very widely used (see Train (2007)).[6] But we find this model is dominated by either G-MNL or S-MNL in all ten data sets, and in some cases by both.

Of course, it is also important to assess <u>why</u> the scale heterogeneity models fit better, in terms of what behavioural patterns they capture better than MIXL. We show that G-MNL can account for "extreme" consumers who exhibit nearly lexicographic preferences, while MIXL is not able to account for such behaviour. We also show that G-MNL is better able to explain consumers who exhibit very "random" behaviour (in a sense we formalize below). Both of these advantages follow directly from the fact that the G-MNL model allows for much greater flexibility in the shape of posterior distribution of person specific parameters than does the MIXL model, even when the amount of data per person is large.

A comparison of our results across datasets revealed two other interesting patterns. First, we can assess the importance of heterogeneity *in general* (both scale and residual) by looking at the percentage log-likelihood improvement in going from simple MNL to the G-MNL model. By this metric, heterogeneity is roughly *twice* as important in the data sets that involve medical decisions as in those that involve product choices. We speculate that this may be because medical decisions involve more complex emotions/greater involvement and/or higher brain functions than do consumer purchase decisions. But regardless of the reason, the result has important implications for the study of medical decision-making.

Second, we lack a formal metric for assessing relative importance of scale vs. residual taste heterogeneity in a given data set, because log-likelihood improvements from including them are not additive. But, as a heuristic, we look at the fraction of the overall likelihood improvement from including all forms of heterogeneity that is attained by including scale heterogeneity alone. This fraction is far greater in the four data sets that involve medical decisions or cell phones than in the six involving choice of pizza delivery, holiday packages or charge cards. This finding is consistent with a hypothesis that scale heterogeneity is more important in contexts involving more complex choice objects (medical tests or high-tech goods vs. consumer goods). But research on sources of heterogeneity is in its infancy (see, e.g., Louviere, Carson, et al (2002), Cameron (2002)),[7] so this hypothesis is only preliminary.

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results showing that BIC and CAIC are reliable for assessing if scale heterogeneity is present, but that they tend to prefer models with uncorrelated errors even when correlation is present.
[6] Presumably a key reason is the ready availability of Ken Train's program for MIXL. The classical version of his program imposes uncorrelated errors (although the Bayesian version has an option to allow correlation).
[7] This prior work has examined complexity as a source of scale heterogeneity, defining "complexity" to be the amount of information subjects must process to make choices. Factors examined as contributors to "complexity" include number of attributes, number of alternatives, number of attributes that differ among alternatives, number of scenarios. But complexity may also derive from the nature of attributes themselves (i.e., attributes of high-tech goods may be intrinsically harder to evaluate than those of simple consumer goods). There may also be

II. The Generalized Multinomial Logit Model (G-MNL)

In the simple multinomial logit (MNL) model the utility to person n from choosing alternative j on purchase occasion (or in choice scenario) t is given by:

$$U_{njt} = \beta x_{njt} + \varepsilon_{njt} \qquad n = 1,...,N; \quad j = 1,...,J; \quad t = 1,...,T, \qquad (1)$$

where x_{njt} is a vector of observed attributes of alternative j, β is a vector of utility weights (homogenous across consumers) and $\varepsilon_{njt} \sim$ iid extreme value is the "idiosyncratic" error. As emphasized by Keane (1997b), the idiosyncratic error can be motivated as consumer heterogeneity in tastes for unobserved (or intangible or latent) product attributes. The x_{njt} for $j=1,...,J$ may include alternative specific constants (ASCs), which capture persistence in the unobserved attributes (for each option j) over choice occasions. If the average consumer views option j as having desirable unmeasured attributes, it will have a positive ASC.

Of course, the great popularity of the MNL stems from the fact that it generates simple closed form expressions for the choice probabilities:

$$P(j \mid X_{nt}) = \exp(\beta x_{njt}) \Big/ \sum_{k=1}^{J} \exp(\beta x_{nkt}), \qquad (2)$$

where X_{nt} is the vector of attributes of all alternatives $j=1,...J$. However, due to the restrictive assumptions that (i) the ε_{njt} are iid extreme value and (ii) tastes for observed attribute are homogenous, MNL imposes a very special structure on how changes in elements of x_{njt} can affect choice probabilities. For instance, from (2) we see the restrictive IIA property:

$$P(j \mid X_{nt}) / P(k \mid X_{nt}) = \exp(\beta x_{njt} - \beta x_{nkt})$$

which says that the ratio of choice probabilities for alternatives j and k depends only on the attributes of j and k. Thus, changes in the attributes of any product l, or the introduction of a new product into the choice set, cannot alter the relative probabilities of j and k. This is obviously unrealistic in cases where product l is much more similar to j than to k.

One model that avoids IIA is the MIXL model. In MIXL the utility to person n from choosing alternative j on purchase occasion (or in choice scenario) t is given by:

$$U_{njt} = (\beta + \eta_n) x_{njt} + \varepsilon_{njt} \qquad n = 1,...,N; \quad j = 1,...,J; \quad t = 1,...,T, \qquad (3)$$

Here, β is the vector of <u>mean</u> attribute utility weights in the population, while η_n is the person n specific deviation from the mean. The "idiosyncratic" error component ε_{njt} is still assumed

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individual differences in ability to deal with complexity, arising due to literacy differences, age differences, etc. For example, Fang et al (2006) find that ability to choose among insurance options differs by level of cognitive ability. Response times also can be used as indirect measures of task complexity (i.e., more complex tasks exhibit longer response times). In behavioural economics, de Palma et al. (1994) develop a theoretical model where consumers differ in ability to choose, but have identical preferences. Their assumptions suggest that as complexity increases, some consumers who have less ability to choose should make more mistakes.

to be iid extreme value. The investigator may specify any distribution for the η vector, but in most applications it is assumed to be multivariate normal, MVN(0, Σ). However, the price coefficient is sometimes assumed to be log-normal to impose the proper sign restriction.

Many MIXL applications have assumed Σ is diagonal. This rules out that consumers who like a certain attribute will also tend to like (dislike) some other attribute. That is, it rules out correlation in tastes across attributes, but not correlation in tastes across alternatives.[8]

A major appeal of MIXL is ease of use. It relaxes IIA yet it is still quite simple to program.[9] The reason MIXL is simple to program can be seen by examining the expression for the choice probabilities and how they are simulated:

$$P(j \mid X_{nt}) = \frac{1}{D} \sum_{d=1}^{D} \frac{\exp[(\beta + \eta^d)x_{njt}]}{\sum_{k=1}^{J} \exp[(\beta + \eta^d)x_{nkt}]} \tag{4}$$

Thus, given D draws $\{\eta^d\}_{d=1,\dots,D}$ from the multivariate normal MVN(0, Σ), one obtains simulated choice probabilities just by averaging simple logit expressions over these draws.[10]

The scale heterogeneity model (S-MNL) can be understood by recognizing that the idiosyncratic error in both (1) and (3) has a scale or variance that has been implicitly normalized (to that of the standard extreme value distribution) to achieve identification. To proceed, let us write out the simple logit model with the scale of the error made explicit:

$$U_{njt} = \beta x_{njt} + \varepsilon_{njt}/\sigma \qquad n = 1,\dots,N; \quad j = 1,\dots,J; \quad t = 1,\dots,T, \tag{5}$$

Here, σ is the scale of the error term. Obviously, it is not possible to identify both β and σ, so it is standard practice to normalize σ to 1, which is equivalent to multiplying (5) through by σ.

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[8] It is important to emphasize that the assumption that Σ is diagonal does not rule out correlation across alternatives or within alternatives over time. Note that (3) can be rewritten:

$$U_{njt} = \beta x_{njt} + (\eta_n x_{njt} + \varepsilon_{njt}) = \beta x_{njt} + v_{njt}$$

The composite error term $v_{njt} = (\eta_n x_{njt} + \varepsilon_{njt})$ will be positively (negatively) correlated across alternatives j that have similar (dissimilar) attributes, which is indeed the essential idea of the MIXL model. Thus, MIXL with diagonal Σ does avoid IIA. It also allows for correlation over time, as a person who places high utility weights on certain attributes will persist in preferring brands with high levels of those attributes over time.
[9] Another model that avoids IIA and allows a more flexible pattern of substitution across alternatives is the multinomial probit (MNP). This model assumes that the idiosyncratic errors have a multivariate normal distribution. MNP can also be extended to allow the β vector to be normally distributed in the population. However, MNP generates choice probabilities that are J-1 dimensional integrals with no closed form. Thus, estimation beyond the J=2 case was precluded for many years by computational limits. But the development of the GHK probability simulator in the late 1980s (see Keane (1994, 1997b)) made MNP estimation feasible. While MNP algorithms are now readily available in popular packages such as SAS and STATA, these packaged programs remain limited because they allow only correlation across alternatives, not across choice occasions as would be appropriate in many stated and revealed preference applications. Geweke, Keane and Runkle (1997) provide extensive discussion of the MNP with correlation across alternatives and over choice occasions. As is clear from their discussion, the programming required to implement MNP in this case is much more involved.
[10] Furthermore, with panel data or multiple choice occasions per subject, the simulated choice probabilities are obtained simply by taking the products of period-by-period logit expressions, and averaging them over draws d.

Now, suppose that σ is heterogeneous in the population, and denote its value for person n by σ_n. Then, multiplying (5) through by σ_n we obtain the S-MNL model:

$$U_{njt} = (\beta\sigma_n)x_{njt} + \varepsilon_{njt} \qquad n = 1,...,N; \quad j = 1,...,J; \quad t = 1,...,T, \qquad (6)$$

Notice that heterogeneity in scale is observationally equivalent to a particular type of heterogeneity in the utility weights. That is, equation (6) implies that the vector of utility weights β is scaled up or down proportionately across consumers n by the scaling factor σ_n.[11]

Note that, if valid, the S-MNL model provides a much more parsimonious description of the data than MIXL. This is because $\beta\sigma_n$ is a much simpler object than $(\beta + \eta_n)$. For example, say there are 10 observed attributes. Then η_n is a 10-vector of normals, with a 10 by 10 covariance matrix containing 55 unique elements to be estimated. In contrast, σ_n is a scalar random variable, and only the parameters of its distribution need be estimated. For example, if σ_n is assumed to be log normal, we need estimate only its variance – a single parameter – as the mean must be constrained for identification reasons (see below).

Recently, Louviere et al (2008) have criticized the MIXL model in (3). Based on the distributions of utility weights obtained from individual level estimations, they have argued that: (1) distributions do not appear very close to being normal, as assumed in most MIXL applications, and (2), when comparing coefficient vectors across consumers, something close to the scaling property implied by (6) seems to hold. Thus, they have argued that much of the heterogeneity in discrete models would be better captured by S-MNL than by MIXL.

In an attempt to shed light on this issue, Keane (2006) noted that MIXL and S-MNL could be nested, to obtain a "generalized multinomial logit" model (G-MNL). Estimation of G-MNL would shed light on whether heterogeneity is better described by scale heterogeneity, normal mixing, or some combination of the two. In the G-MNL model the utility to person n from choosing alternative j on purchase occasion (or in choice scenario) t is given by:

$$U_{njt} = [\sigma_n\beta + \gamma\eta_n + (1-\gamma)\sigma_n\eta_n]x_{njt} + \varepsilon_{njt} \qquad (7)$$

where γ is a parameter between 0 and 1. Figure 1 describes how G-MNL nests MIXL, S-MNL and MNL, as well as two other models we call G-MNL-I and G-MNL-II. To obtain MIXL one sets the scale parameter $\sigma_n=\sigma=1$. To obtain the S-MNL model one sets $Var(\eta_n)=0$, meaning the variance-covariance matrix of η_n, denoted Σ, is degenerate.

The parameter γ does not arise in either the MIXL or S-MNL special cases. It is only present in the G-MNL model, and its interpretation is more subtle than either σ_n or Σ. The

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[11] A common misconception is that random coefficient and scale heterogeneity models are fundamentally different. In fact, they are just different ways of specifying the distribution of coefficient heterogeneity.

parameter γ governs how the variance of residual taste heterogeneity varies with scale, in a model that includes both. To see this, note that there are two equally sensible ways to nest MIXL and S-MNL. One might simply combine (3) and (6) to obtain what we call G-MNL-I:

$$U_{njt} = (\beta\sigma_n + \eta_n)x_{njt} + \varepsilon_{njt} \qquad n = 1,...,N; \quad j = 1,...,J; \quad t = 1,...,T, \tag{8}$$

Alternatively, one might start with (3) and make the scale parameter explicit:

$$U_{njt} = (\beta + \eta_n)x_{njt} + \varepsilon_{njt}/\sigma_n \qquad n = 1,...,N; \quad j = 1,...,J; \quad t = 1,...,T,$$

Then, multiplying through by σ_n we obtain G-MNL-II:

$$U_{njt} = \sigma_n(\beta + \eta_n)x_{njt} + \varepsilon_{njt} \qquad n = 1,...,N; \quad j = 1,...,J; \quad t = 1,...,T, \tag{9}$$

Note that, in either model (8) or (9), we can write the vector of utility weights as:

$$\beta_n = \sigma_n\beta + \eta_n^*$$

In our terminology, the random variable σ_n captures scale heterogeneity while the random variable η_n^* captures "residual" taste heterogeneity. The difference between G-MNL-I and G-MNL-II is that, in G-MNL-I, the standard deviation of residual taste heterogeneity is independent of the scaling of β. But in G-MNL-II the standard deviation of η_n^* is proportional to σ_n. As noted in Figure 1, G-MNL approaches G-MNL-I as $\gamma \to 1$, and approaches G-MNL-II as $\gamma \to 0$. In the full G-MNL model γ can take on any value between 0 and 1.

To enhance intuition, it is useful to consider the use of an estimated G-MNL model to calculate the posterior means of individual level parameters. G-MNL-I adopts the prior that they are a mixture-of-normals with different means but equal variances. G-MNL-II adopts the prior that they are a mixture-of-normals with proportionally different means <u>and</u> standard deviations. The full G-MNL model allows for differential scaling of β and η_n^*.

In order to impose the restriction that γ must lie between 0 and 1 in estimation, we use a logistic transform $\gamma = \exp(\gamma^*)/[1 + \exp(\gamma^*)]$ and estimate the parameter γ^*. Thus, G-MNL approaches G-MNL-I as $\gamma^* \to \infty$, and approaches G-MNL-II as $\gamma^* \to -\infty$.

To complete the specification of G-MNL we must specify the distribution of σ_n. The spirit of the model is that σ_n is positive, as it represents the person specific standard deviation of the idiosyncratic error term. Thus, we specify that σ_n has a log normal distribution with mean 1 and standard deviation τ, or $LN(1, \tau^2)$. Thus, τ is the key parameter that indicates if scale heterogeneity is present in the data. As $\tau \to 0$, G-MNL approaches MIXL. If $\tau > 0$ then G-MNL approaches S-MNL as the diagonal elements of Σ approach zero. If both τ and Σ go to zero we approach the simple MNL model.

III. Computation and Estimation

Here we discuss the details of computation and estimation for the G-MNL model. In order to constrain the scale parameter σ_n to be positive we use an exponential transformation:

$$\sigma_n = \exp(\bar{\sigma} + \tau \varepsilon_{0n}) \quad where \quad \varepsilon_{0n} \sim N(0,1).$$

Thus, as the parameter τ increases, the degree of scale heterogeneity increases.

Obviously, as σ_n and β only enter the model as a product $\sigma_n \beta$, some normalization on σ_n is necessary to identify β. The natural normalization is to set the mean of σ_n equal to 1, so that β is interpretable as the mean vector of utility weights. In order to achieve this, it is necessary that the parameter $\bar{\sigma}$ be a decreasing function τ. Note that:

$$E\sigma_n = \exp(\bar{\sigma} + \tau^2 / 2)$$

Thus, to set $E\,\sigma_n = 1$ we should set $\bar{\sigma} = -\tau^2 / 2$.

Then, the simulated choice probabilities in the G-MNL model take the form:

$$P(j \mid X_{nt}) = \frac{1}{D} \sum_{d=1}^{D} \frac{\exp(\sigma^d \beta + \gamma \eta^d + (1-\gamma)\sigma^d \eta^d) X_{njt}}{\sum_{k=1}^{J} \exp(\sigma^d \beta + \gamma \eta^d + (1-\gamma)\sigma^d \eta^d) X_{nkt}} \tag{10}$$

where:

$$\sigma^d = \exp(\bar{\sigma} + \tau \varepsilon_0^d)$$

Note that η^d is a multivariate normal K-vector, where K is the number of elements of β, while ε_0^d is simply a scalar. The simulation involves drawing the multivariate normal vectors $\{\eta^d\}$ for $d=1,\ldots,D$, and the standard normal random variables $\{\varepsilon_0^d\}$ for $d=1,\ldots,D$. It is notable that the computation in (10) is no more difficult than that for the MIXL model in (4).

Now suppose we have either panel data or multiple choice tasks per subject. Let $y_{njt}=1$ if person n chooses option j at time t, and 0 otherwise. Then, the simulated probability of observing person n choosing a sequence of choices $\{y_{njt}\}_{t=1}^{T}$ is given by:

$$\hat{P}_n = \frac{1}{D} \sum_{d=1}^{D} \prod_{t} \prod_{j} \left(P(j \mid X_{nt}, \sigma^d, \eta^d) \right)^{y_{njt}} = \frac{1}{D} \sum_{d=1}^{D} \prod_{t} \prod_{j} \left(\frac{\exp(\sigma^d \beta + \gamma \eta^d + (1-\gamma)\sigma^d \eta^d) X_{njt}}{\sum_{k=1}^{J} \exp(\sigma^d \beta + \gamma \eta^d + (1-\gamma)\sigma^d \eta^d) X_{nkt}} \right)^{y_{njt}}$$

which strings together period specific probabilities like that inside the summation in (10).[12]

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[12] Empirical applications of MIXL, S-MNL and G-MNL will almost always involve multiple observations per subject. While the MIXL model is formally identified given only one observation per subject (simply because the mixture of normal and extreme value errors may provide a slightly better fit to the data than extreme value alone), Harris and Keane (1999) showed that the likelihood surface is extremely flat without multiple

In practice, we found the numerical performance of the algorithm is substantially improved by adopting two slight modifications to the above specification. First, we set the mean of σ_n equal to one in the simulated data, not merely in expectation. This means setting:

$$\bar{\sigma} = -\ln\left[\frac{1}{N}\sum_{n=1}^{N}\exp(\tau\varepsilon_0^{d(n)})\right]$$

where the notation $\varepsilon_0^{d(n)}$ means the dth draw for the nth person (we use a different set of D draws for each person). Second, if τ is too large, it causes numerical problems (i.e., overflows and underflows in exponentiation) for extreme draws of ε_0. To avoid this, we draw ε_0 from a truncated normal with truncation at ± 2.

In addition, we also discovered that the S-MNL model performs poorly empirically when alternative specific constants (ASCs) are scaled. By this we mean: (1) the estimates often "blow up," with τ taking on very large values and the standard errors of the elements of β becoming very large, and (2) the model always produces a substantially worse fit than a model where only the utility weights on observed attributes are scaled, while the ASCs are assumed homogenous in the population. Mechanically, it seems that these problems arise because data sets typically contain a set of individuals who always (or almost always) chose the same option, regardless of the elements of X_{nt}. If the ASCs are scaled, then the model can explain this phenomenon by making τ very large so that ASCs can vary substantially across individuals. The estimation algorithm usually decides to take this route.

On a more conceptual level, note that ASCs are fundamentally different from most observed attributes. For instance, for attributes like price or indicators of quality, it makes sense to think that all consumers have utility weights of the same sign, but that these weights are scaled up or down across consumers (e.g., all consumers value quality, but some value it more than others). In contrast, ASCs tend to measure intangible aspects of products. Thus, it is very likely that the ASCs consumers assign to products will differ in sign. A model that imposes that all consumers have ASCs of the same sign, and that these are merely scaled, is very unlikely to explain key patterns observed in choice behaviour, such as the high degree of persistence in choices or the "loyalty" that consumers often exhibit for specific brands.

Thus, in models that have ASCs, we decided to specify the S-MNL in one of two ways. In one version, we assume the ASCs are homogenous in the population and do not scale them. In another version we treat the ASCs as random effects. We assume these have a

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observations per subject. This is completely intuitive: We cannot expect to identify parameters that characterize systematic heterogeneity in individual choice behaviour if we only see each person once.

MVN distribution which we estimate. We treat the ASCs in the G-MNL model in exactly the same way. Thus, we can rewrite (7) as:

$$U_{njt} = (\beta_{0j} + \eta_{0nj}) + [\sigma_n \beta + \gamma \eta_n + (1-\gamma)\sigma_n \eta_n] x_{njt} + \varepsilon_{njt} \qquad (11)$$

where x_{njt} is now interpreted to include only observed attributes and not ASCs, and $\beta_{0j} + \eta_{0nj}$ is the ASC for alternative j, which consists of the component β_{0j} which is constant across people, and the component η_{0nj} which is heterogeneous across people. Then, we can write that $(\beta_0 + \eta_{0n})$ is a vector of ASCs, with β_0 being the mean vector and η_{0n} being the stochastic component. We assume that the entire vector $\{\eta_{0n}, \eta_n\}$ has a MVN distribution.

Finally, in an effort to explain why scale differs across people, or even across choice occasions for the same person, we can let σ_n be a function of characteristics of people or of choice occasions. For instance, we could write:

$$\sigma_{nt} = \exp(\bar{\sigma} + \theta z_{nt} + \tau \varepsilon_0) \qquad (12)$$

where z_{nt} is a vector of attributes of person i and choice occasion t. For instance, one might let z_{nt} contain demographics, or some measure of the "entropy" of the choice occasion (e.g., how similar or dissimilar the choices are; see Swait and Adamowicz, 2001; DeShazo and Fermo, 2002). Similarly, in the equation for γ we could let the parameter γ^* depend on z_{nt} as well.

IV. Monte Carlo Results

In this section we present two Monte-Carlo experiments to evaluate the properties of G-MNL model estimates. Of particular interest is whether the model can accurately assess the extent of scale heterogeneity (captured by τ) vs. "residual taste heterogeneity" captured by Σ. In order to make the Monte Carlo experiments realistic, we constructed simulated data sets based on two of the empirical data sets that we will analyse in Section V. The first is a data set where women choose whether to have a pap smear exam, and the second is a data set where people choose between holiday locations (the "Holiday A" data set).

In each experiment, we use the actual Xs from the empirical data sets. The "true" parameters are obtained by estimating the G-MNL model on the empirical data sets. We generate 20 artificial data sets based on each empirical data set. We then estimate the G-MNL model on these 20 Monte Carlo data sets. In these estimations, as in our empirical work in Section V, we use D=500 draws to simulate the likelihood.

The results of estimating G-MNL on the 20 data sets based on the pap smear data are reported in Table 1. The pap smear data sets contain five attributes (see Table 5), including doctor attributes, test cost and contextual variables (i.e., whether the test is recommended), as well as an ASC for the "Yes" option. Each has 79 hypothetical respondents and 32 choice

occasions per respondent. In Table 1 we report the true parameter values used to generate the data sets, the mean estimates across the 20 replications, the empirical standard deviation of the estimates across data sets, and the mean of the asymptotic standard errors. An asterisk indicates that the bias in an estimated parameter is significant at the 5% level.

The results in Table 1 show evidence of significant bias for only a handful of parameters. Of the six elements of the β vector, only β_5 exhibits significant bias. But the magnitude of the bias is less than 2/3 of an empirical standard deviation.[13] The standard deviations of residual taste heterogeneity are also rather precisely estimated, except for that on attribute 6, where it is upward biased.[14] Most importantly, the scale heterogeneity parameter τ is estimated quite precisely: its true value is .890 and the mean estimate is .891.

In these datasets the true value of the parameter γ is almost 0, but our mean estimate is .156. This is significantly greater than zero but still quantitatively small. In addition, the median estimate of γ is .08 (it exceeds .50 in only one out of 20 datasets). Thus, the model does a reasonable job of uncovering the fact that the true γ is small. For the most part the empirical standard errors and mean asymptotic standard errors are close, suggesting the asymptotic theory is a good guide to the variability of the estimates.

The results of estimating the G-MNL model on the 20 artificial data sets based on the Holiday A data set are reported in Table 2. These data sets contain 8 attributes, as described in Table 5. There are 331 hypothetical respondents and 16 choice occasions per respondent.

Of the eight elements of the β vector, only β_1 exhibits significant bias. And the magnitude of the bias is only 1/2 of an empirical standard deviation. The scale heterogeneity parameter τ is again estimated quite precisely: its true value is 1.0 and the mean estimate is .968. However, the standard deviations of residual taste heterogeneity show a tendency to be upward biased, and this bias is significant for 6 out of 8 parameters.

We would argue that this upward bias in the error variances is not a great cause for concern. The largest bias, which is for σ_8, is only 80% of an empirical standard deviation, and other significant biases are about 2/3 of a standard deviation. Biases of this magnitude are not surprising, in light of prior work showing it is often difficult to pin down error variance-covariance parameters in discrete choice models (e.g., Geweke, Keane and Runkle (1994)).

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[13] Of course, the reader should always bear in mind that ML estimators are only consistent – they are not unbiased in finite samples. This is why in Monte Carlo work it is generally argued that modest biases are to be expected and are not a major concern. Only quantitatively large biases that would substantially alter the interpretation of results would be a major concern.

[14] The estimates of the correlations among the errors (i.e., the residual taste heterogeneity) fall reasonably well in line with the true values, although significant biases show up in 6 out of 15 cases.

The true value of the parameter γ is 0.20, and the mean estimate is .137. This downward bias is significant, but again the model does a reasonable job of uncovering the fact that the true γ is small. The greatest cause for concern in Table 2 is that the asymptotic standard errors are systematically smaller than the empirical standard errors. This was not the case in Table 1. We suspect that this difference arises because we attempt to estimate a larger number of variance-covariance parameters in Table 2 (i.e., 36 vs. 21).

In Section V we use AIC, BIC and CAIC to choose between the G-MNL, MIXL and S-MNL models. So it is important to consider if these criteria can reliably distinguish among them. To address this issue, we perform a 3 by 6 factorial experiment where we: (i) simulate data where the true model is S-MNL, MIXL or G-MNL (both with correlated errors), and (ii) estimate the MNL, S-MNL, MIXL and G-MNL models (both with and without correlated errors) on those data sets. As in Tables 1 and 2, this was done using data sets constructed to look like the pap smear and Holiday A data.[15] We then counted the number of times that AIC, BIC and CAIC preferred each model in each case. The results are reported in Table 3.

Consider first the case where G-MNL with correlated errors is the true model. In the pap smear data sets the AIC correctly picks it in 9/20 cases. But in 11/20 cases AIC chooses instead the more parsimonious G-MNL with uncorrelated errors. In contrast, for the Holiday A data sets, AIC correctly picks G-MNL with correlated errors in all 20 cases. Now consider BIC and CAIC (which have larger penalties for adding parameters). In both data sets, these criteria tend to pick the more parsimonious G-MNL with uncorrelated errors, even though errors are correlated. Indeed, they occasionally even pick MIXL with uncorrelated errors.

Next consider the case where MIXL with correlated errors is the true model. In this case BIC and CAIC correctly pick MIXL as the true model in the large majority of cases. But they always choose the more parsimonious version with uncorrelated errors. The performance of AIC in this case is poor, as it chooses G-MNL in 12/20 cases in the pap smear data set and 7/20 cases in the Holiday A data sets.

Finally, when S-MNL is the true model it is correctly identified by all three information criteria in all 40 cases. The reason for this success is that MIXL and G-MNL both involve a large increase in number of parameters over S-MNL. In summary, while the results for the case when S-MNL is the true model are clear cut, those for the cases where MIXL or G-MNL are the true model appear more ambiguous.

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[15] For example, we fit the S-MNL model to the Papsmear data set, and use those estimates to generate the data where S-MNL is the true model. We fit MIXL with correlated errors to the Papsmear data set, and use those estimates to generate the data where MIXL is the true model. Finally, we fit G-MNL with correlated errors to the Papsmear data set, and use those estimates to generate the data where G-MNL is the true model.

How can we make sense of these results? The bottom panel of Table 3 provides a useful summary. Here we look only at the cases where MIXL or G-MNL is the true model, ignore the distinction between correlated and uncorrelated errors, and combine the results from the two data generating processes. We simply ask how reliably the three information criteria determine if the true model contains scale heterogeneity. Note that BIC makes the correct determination in 68/80 cases. It wrongly concludes the true model is MIXL in 7/80 cases, and it only gives a false positive for scale heterogeneity in 5/80 cases. The results for CAIC are similar. In contrast, AIC has a bias towards accepting scale heterogeneity when it is not present (19/80 cases). This is not surprising, as the AIC has a smaller penalty for adding parameters, and G-MNL has only two more parameters than MIXL.

Given these results, we would argue that both BIC and CAIC provide accurate guides for whether scale heterogeneity is present – that is, for distinguishing between MIXL and G-MNL. But they are biased toward rejecting the presence of error correlations. This is not surprising because error correlations add many parameters, which these criteria penalize heavily. On the other hand, AIC correctly picks models where errors are correlated in 69/80 cases. Thus, we would recommend using the information criteria in conjunction: Using BIC and/or CAIC as reliable measures of whether scale heterogeneity is present (i.e., MIXL vs. G-MNL or S-MNL) and then using AIC to evaluate whether error correlations are important.

V. Empirical Results
V.A. Estimation Results

Our empirical results are based on data from ten stated preference choice experiments described in Table 4. The datasets differ widely along several dimensions, including the object of choice (i.e., medical tests, mobile phones, pizza delivery services, holiday packages and charge cards), the number of attributes (6 to 18), the number of choices (2 to 4), and the number of choice occasions (or choice sets) that each person faced in the experiment (4 to 32). All datasets are fairly large, but the number of observations also varies substantially (from 2,528 to 21,856). Table 5 lists all attributes and how they are coded in each dataset.

Tables 6-15 present estimation results for the 10 datasets. We only discuss the results for dataset 1 in detail, giving an overview of results for the other datasets in Sections V.B and V.D. In dataset one, participants were asked whether they would chose to receive diagnostic tests for Tay Sachs disease, cystic fibrosis, both or neither, giving four alternatives. The attributes that vary across choice scenarios are the cost of the tests, whether the person's doctor recommends the tests, the chance that the test is inaccurate, how the results of the tests

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will be communicated, and what the person is told about the probability that they are a carrier for each disease. The members of the sample in dataset one are Ashkenazi Jews, who are a population of interest as they have a relatively high probability of carrying Tay Sachs.

The estimation results are presented in Table 6. The first column presents results for a simple MNL model. All attribute coefficients are significant with expected signs (except for how the result is communicated, which is not significant). Cost has a negative effect, doctor recommendation and risk factors have positive effects, and inaccuracy has a negative effect.

The next column contains results for the S-MNL model with homogeneous ASCs. The scale parameter τ is 1.14 with a standard error of 0.09, implying substantial scale heterogeneity in the data. Allowing for scale heterogeneity leads to a dramatic improvement in the likelihood over MNL, from -3717 to -3223, which is 494 points or 13%. As this model adds only a single parameter, it leads to substantial improvements in all three information criteria (AIC, BIC and CAIC).

In the 3rd column we report results of the S-MNL model with heterogeneity in the ASCs. Allowing for such heterogeneity leads to a further substantial improvement in fit (e.g., 408 points in the likelihood, or 11%). Notice that the scale heterogeneity parameter τ falls from 1.22 to 0.64, but remains highly significant with a standard error of 0.06.

The next two columns of the table present results from MIXL and the G-MNL model that nests MIXL and S-MNL. Two aspects of the results are notable. First, while the S-MNL model does provide dramatic improvement in fit compared to simple MNL, the improvement achieved by MIXL is, at least in this data set, considerably greater. MIXL achieves a log-likelihood of -2500 vs. -3717 for MNL. This is a 33% improvement, compared to the 24% improvement achieved by S-MNL (with random ASCs). Of course, this is not too surprising, as MIXL adds 66 parameters, while S-MNL adds only 7.

Second, G-MNL provides a better fit than either MIXL or S-MNL alone. By adding two parameters, it achieves a log-likelihood improvement of 20 points over MIXL, and it beats MIXL on all three information criteria (AIC, BIC, CAIC).

Note that the G-MNL estimate of the scale parameter τ is 0.45 with a standard error of 0.08. Thus, the estimates imply a substantial degree of scale heterogeneity in the data, even after allowing for correlated normal random coefficients. As $\sigma_n = \exp(-\tau^2/2 + \tau\varepsilon_{0n})$, the estimates imply a person at the 90th percentile of the scale parameter would have his/her vector of utility weights scaled up by 57%, while a person at the 10th percentile would have his/her vector of utility weights scaled down by 46%.

The estimate of γ is 0.11, which implies the data is closer to the G-MNL-II model (see equation (9)), where the variance of residual taste heterogeneity increases with scale, than the G-MNL-I model (see equation (8)), where it is invariant to scale.

Finally, the last two columns of Table 6 report estimates of restricted versions of MIXL and G-MNL with *uncorrelated* residual taste heterogeneity. This is of interest in part because MIXL with independent normal taste heterogeneity is popular among practitioners. Note that restricting residual taste heterogeneity to be independent across attributes leads to a substantial deterioration of the log-likelihood – by over 250 points for both MIXL and G-MNL.[16] The AIC, BIC and CAIC all prefer the G-MNL model with correlated taste heterogeneity over that without. This is a bit surprising, in light of our Monte Carlo result that BIC and CAIC tend to prefer the uncorrelated model even if correlation is present.

With the above discussion as a guide, the interested reader should be able to follow the empirical results in Tables 7-15. Rather than describe each of these in detail, we turn to a discussion of general patterns that emerge across data sets.

V.B. Comparing Model Fit across Data Sets

Table 16 compares the fit of our 7 alternative models (simple MNL, S-MNL, MIXL, G-MNL and the latter two with uncorrelated taste heterogeneity) across the 10 datasets. Recall that our Monte Carlo results in Section IV indicated that BIC and CAIC were the most reliable criteria for determining whether scale heterogeneity is present. According to BIC and CAIC, G-MNL is the preferred model in 7 out of 10 data sets. And the S-MNL (with a random intercept) is preferred in the remaining 3 data sets (mobile phones and charge cards A and B). Thus, models that include scale heterogeneity are preferred over MIXL in <u>all</u> cases.

That S-MNL is preferred in 3 cases is striking, given the great simplicity of this model relative to its competitors. For example, in the mobile phone dataset, S-MNL (with a random intercept) beats MIXL by 176 points on BIC, and beats G-MNL by 160 points. Yet it has only 17 parameters, compared to 45 for MIXL and 47 for G-MNL. Similarly, in the charge card A and B data sets, S-MNL beats MIXL by 176 and 159 points on BIC, respectively.

Among the 7 data sets where G-MNL is preferred by BIC and CAIC, the G-MNL model with correlated errors is preferred only in the two Tay Sachs datasets. The G-MNL model with uncorrelated residual taste heterogeneity is preferred in five datasets (Pap smear, Pizza A and B, and Holiday A and B). But this result should be interpreted with caution, in

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[16] *A priori*, one might have expected the deterioration in the likelihood to be less in the model with scale heterogeneity, because scale heterogeneity could "sop up" much of the positive correlation among the attribute weights. However, when we look at the estimated correlation matrix (not reported but available on request), we find that at least half of the correlations among attribute weights in this data set are negative.

light of our Monte Carlo results in Section IV showing that BIC and CAIC tend to prefer simpler models without correlation even when error correlations are present.

In the 7 cases where BIC and AIC prefer the G-MNL model, the AIC, which imposes a smaller penalty for additional parameters, always prefers the full version of G-MNL with correlated errors. This is not too surprising, as our Monte Carlo results suggest that AIC is more likely to prefer models with correlated errors when correlation is in fact present.

The AIC results regarding the preferred model contradict BIC and CAIC for three data sets. For mobile phones, AIC prefers G-MNL with correlated errors while BIC and CAIC both prefer S-MNL. Also, in the two credit card data sets, AIC slightly prefers MIXL with correlated errors, although the advantage over G-MNL and S-MNL is very small.

In summary, models with scale heterogeneity (G-MNL or S-MNL) are preferred by all three information criteria in 8 out of 10 cases. In the other two cases, AIC picks MIXL while BIC and CAIC pick S-MNL. Thus, there is clear evidence that scale heterogeneity is important in 8 data sets, and substantial evidence it is important in the other two.[17]

A final notable result is that MIXL with uncorrelated errors, which is very widely used (see Train (2007)), is never preferred. According to BIC and CAIC it is beaten by G-MNL with uncorrelated errors in every data set except mobile phones. It is beaten by S-MNL in mobile phones, as well as the Tay Sachs general population data, and the two charge card data sets. It is beaten by MIXL with correlated errors in the Tay Sachs and charge card data. According to BIC and CAIC, it is beaten by G-MNL with correlated errors in those four data sets plus Pizza B and Holiday B, and under AIC it is beaten by G-MNL with correlated errors in every data set. The only case where it comes even close to being the preferred model is the pap smear data. Thus, the data offer no empirical support for MIXL with uncorrelated errors.

V.C. Why Do Models with Scale Heterogeneity Fit Better than MIXL?

We have shown that models with scale heterogeneity (either G-MNL or S-MNL) are preferred by BIC and CAIC in all ten data sets, and preferred by AIC in 8 out of 10. Thus, we have strong evidence that models with scale heterogeneity provide a better fit to a wide range of data sets than do models like MIXL that rely on residual taste heterogeneity alone. In this section we ask "Why do models with scale heterogeneity fit better? That is, what behavioural patterns can they explain better than the MIXL model?" And "What substantive behavioural predictions differ between the G-MNL model and simpler nested models like MIXL?"

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[17] Among the 10 data sets, γ ran off to zero – and had to be pegged near 0 – in five cases, and it ran off to one in another. Only in four cases (the Tay Sachs datasets, mobile phones and charge card A) do we find intermediate values of γ. Usually γ was small, implying the G-MNL-II model is often a reasonable description of the data.

These key questions are addressed in Figures 2 to 5. These look specifically at the Pizza B data, although we could have shown similar figures for other data sets. In Figure 2, we order the 328 individuals from the person with least negative log-likelihood contribution in the MIXL model (i.e., the person the model fits best) to the person with the most negative log-likelihood contribution (i.e., the person the model fits worst). We then plot these people from left to right (the dark circles). We also plot each person's log-likelihood contribution according to the G-MNL model (the light crosses). The horizontal line is the log-likelihood of the naïve model that assumes equal choice probabilities for both alternatives. We also divide the sample into thirds: the "Type I" people on the left that MIXL fits best, the Type IIs in the middle, and the Type IIIs on the right (for whom the fit is often worse than the naïve model).

The key result of Figure 2 is that G-MNL generally fits Type I and Type III people better than MIXL, while the fit for Type II people is about the same. What does this mean? It turns out the Type Is are "extreme" people whose preferences are close to lexicographic. For instance, of these 109 people, 22 always choose the pizza with fresher ingredients on all choice occasions, regardless of other attributes, 18 always choose the pizza with the lower price, etc..[18] The G-MNL model is better able to explain such extreme behaviour, by saying that: (i) some people have a very small scale for the error term (or, conversely, very large attribute weights), so there is little randomness in their behaviour, and (ii) as attribute weights are random, for some people one (or a few) attributes are much more important than others, so that one (or few) attributes almost entirely drive choices.

Turning to Type IIIs, these are people whose behaviour is highly random. That is, their behaviour is largely driven by the idiosyncratic error term ε_{njt} and is little affected by attributes. Indeed, the naïve model that assumes equal choice probabilities regardless of attribute settings generally fits their behaviour better than MIXL. G-MNL still has trouble fitting the behaviour of such people, but it gives a clear improvement over MIXL. G-MNL is better able to explain "random" people because it can say that some people have a very large scale of the error term (or, conversely, very small attribute weights).[19]

Some further insight is gained by looking at the bottom panel of Figure 2. Here, we fit simple MNL models to the Type I, II and III groups separately. Note that for the Type III people we obtain very small attribute weights. Thus, choices of the Type IIIs are largely driven by the error terms. In this sense they are highly random. In contrast, for Type Is we

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[18] There are 32 choice occasions, but each attribute only differs between the two options on 16 occasions.
[19] Note that, in principle, the MIXL model can also generate some people for whom all attribute weights are small. But in a model with several attributes, this would be a very unlikely event.

estimate very large attribute weights. This makes their choices very sensitive to attribute settings. The Type IIs are in the middle. One can clearly see a general scaling up of the attribute weights as one moves from Type IIIs to Type IIs to Type Is.

Having isolated why G-MNL fits better than MIXL, we turn to the question of how its substantive predictions differ. In Figure 3, the four graphs correspond to MNL, S-MNL, MIXL and G-MNL. Each graph shows the distribution of people in terms of their probability of choosing between the two Pizza delivery services.[20] The distribution is shown under two scenarios: a baseline where services A and B have identical attributes and a scenario where service A improves ingredient quality (to all fresh) while also raising price by $4.

Of course, under the baseline, each model says that 100% of the people have a 50% probability of choosing A. After the policy change, MNL (which assumes homogeneous preferences) predicts that all people have a 52% chance of choosing A. In contrast, S-MNL predicts heterogeneity in consumer responses. 41% of consumers continue to have a roughly 50% chance of choosing A, while for 43% the probability of choosing A increases to about 55%, and for 17% of the probability of choosing A increases into the 60-75% range.

The more interesting comparison is between MIXL and G-MNL. G-MNL predicts that, after the policy change, 14% of consumers still have a 50% chance of choosing A. Strikingly, 8% of consumers would have essentially a 100% chance of choosing A (these are the types who put great weight on fresh ingredients) while 5% would have essentially a 0% chance of choosing A (these are the types who care primarily about price). As we would expect based on the Figure 2 results, MIXL predicts that fewer people stay indifferent, and also that fewer people have extreme reactions. Specifically, MIXL predicts that only 8% of consumers stay at roughly a 50% chance of choosing A, while essentially no consumers have their choice probabilities move all the way to 100% or 0%.

In the actual Pizza B data, there are 24/328 = 7.3% of subjects who choose the fresh ingredient Pizza on all choice occasions regardless of other attribute settings, while there are 27/328 = 8.2% who always choose the less expensive Pizza. *The Figure 3 results show that G-MNL can generate such extreme (or lexicographic) behaviour, while MIXL cannot.*

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[20] Note that here we adopt the mathematical psychology view that choice is random for an individual across choice occasions. In the economist's view, the randomness in choice exists solely from the point of view of the analyst, who does not observe a consumer's preference type or all the relevant product attributes. In this view, a consumer faced with the same choice situation on two occasions should make the same choice. But this view is hard to reconcile with behaviour in choice experiments where consumers make repeated choices (e.g., 32 in the Pizza B data set). Inevitably one sees cases where, when presented with A vs. B, a person chooses A, and then later, in a situation that is identical except that an attribute of A is improved, the person chooses B. Randomness across choice occasions *at the individual level* is necessary to explain this. Such randomness is present in choice models applied to experimental data whenever one lets the stochastic terms differ across choice occasions.

To gain additional insight into why the behavioural predictions of G-MNL and MIXL differ, we report for each model the posterior means of the person level coefficients on fresh ingredients and price. To do this we condition on the estimated model parameters and the 32 observed choices of each person, using the algorithm in Train (2003) p. 266. Distributions of the posterior means of the person specific parameters are reported in Figure 4.[21]

The differences in the posteriors generated from the MIXL and G-MNL model are striking. The MIXL posteriors depart modestly from normality, but the strong influence of the normal prior, and in particular its tendency to pull in tail observations, is evident. In contrast, the G-MNL posteriors are multi-modal, with considerable mass in the tails. In particular, the G-MNL posterior for the price coefficient clearly shows a substantial mass of people in the left tail who care tremendously about price. And the G-MNL posterior for the coefficient on fresh ingredients clearly shows a substantial mass of people in the right tail who greatly value freshness. This example clearly illustrates the flexibility of the continuous mixture of scaled normals prior for individual level coefficients in the G-MNL model.

Finally, Figure 5 shows that the pattern shown in Figure 3 emerges not just for fresh ingredients but for other attributes as well. Each panel plots the distribution of consumer choice probabilities under an experiment where one attribute of Pizza delivery service A is improved, and price is also increased by $4. The first panel repeats the fresh ingredients experiment from Figure 3. But now the probability distributions of the G-MNL and MIXL models are plotted side-by-side, making the differences easier to see. As is clear, the G-MNL model puts more mass near the center of the distribution of choice probabilities (i.e., close to 50%) and more mass in the tails (close to 0% or 100%). The same basic pattern holds in experiments where firm A offers gourmet pizza, steaming hot pizza or a vegetarian option.

What are the managerial implications of these results? Unlike the situation in the Pizza B choice experiment, in the real world pizza delivery firms do not offer a single type of pizza (or a small range of options) at a single price. They offer a wide range of pizzas with different attributes at different prices. In order to determine the optimal menu of offerings, a firm needs to know the entire distribution of demand. It is beyond the scope of this paper to design optimal menus. But it is clear that optimal price discrimination strategies would differ between a market where a significant fraction of consumers have essentially lexicographic preferences vs. a market where attribute weights differs less markedly across consumers.

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[21] Allenby and Rossi (1999) call this an "approximate Bayesian" approach. We tried integrating over uncertainty in the estimated model parameters, as well as uncertainty in calculating the posterior means. This made little difference, presumably because (i) the model coefficients are estimated quite precisely, and (ii) with 32 observations per person, the posterior means are also estimated rather precisely.

In summary, these results make clear why models with scale heterogeneity (either G-MNL or S-MNL) fit better than MIXL in every data set we examine. The models with scale heterogeneity are able to generate the sort of extreme (or lexicographic) behaviour that is common in these choice experiments, while MIXL cannot. It is also able to capture "random" choice behaviour (i.e., low responsiveness to attribute settings) better than MIXL. The reason for both advantages is transparent. Models that include scale can generate random behaviour by setting scale large, and can generate lexicographic behaviour by setting scale small (while also letting one attribute have a large idiosyncratic component of its preference weight).

V.D. Comparing the Importance of Heterogeneity across Data Sets

Table 17 summarizes results across the ten data sets.[22] One interesting pattern is the extent to which the inclusion of heterogeneity of <u>all</u> types leads to improvement in model fit. That is, what is the percentage improvement in the log-likelihood when we go from the simple MNL model to the full-fledged G-MNL model? Strikingly, this differs greatly by dataset, ranging from only 12% to 16% in the mobile phone, pizza B and holiday B data sets, to as much as 33% to 40% in the Tay Sachs and Pap smear datasets. Another metric (not in the table) is the improvement in pseudo-R^2 when heterogeneity is included. This ranges from .27 to .35 in the three medical datasets, but from only .10 to .17 in the other datasets.[23]

Thus, the extent of preference heterogeneity in the three datasets involving medical decisions is roughly <u>twice</u> as great as in those for consumption goods (phones, pizza delivery, holidays, charge cards). There are a number of possible explanations for this pattern. People may have stronger feelings about medical procedures than the more mundane attributes of consumer products. People may have very different attitudes towards risk. Perhaps medical decision-making is a more complex or higher involvement task, and taste heterogeneity in general (and perhaps scale heterogeneity in particular) increases with task complexity. [24, 25]

A second interesting pattern is how the importance of scale heterogeneity differs across datasets. We do not have a formal measure of the fraction of heterogeneity due to scale heterogeneity, because the improvement in the likelihood when we include scale and residual

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[22] The Mobile Phone, Pizza B, Holiday B, and Charge Card data sets contained very many attributes (16 to 18), so it was not feasible to estimate a full variance-covariance matrix in these cases. Instead, we restricted them to have a one-factor structure. Such an approach may be worth pursuing as a compromise between the two extreme options commonly applied in practice: imposing no correlation or estimating full variance-covariance matrix.

[23] Pseudo-R^2 for a discrete choice model is defined as 1-LL(m)/LL(0) where LL(m) is the log-likelihood of the model, and LL(0) is that of a "null" model that assigns equal probability to each choice.

[24] Medical decisions are also relatively "unfamiliar" tasks compared to choice among common consumer goods. It is plausible that choice in such unfamiliar contexts is more difficult.

[25] Also, it may simply be that taste heterogeneity is more important in datasets with ASCs. But, this is contradicted by the mobile phone and credit card data sets, which contain ASCs but exhibit a relatively low degree of heterogeneity.

heterogeneity is not additive. But we can get a sense of the importance of scale heterogeneity by asking: "Of the total improvement in the likelihood achieved by adding all forms of heterogeneity, what fraction can be attained just by adding scale heterogeneity?" Table 17 reports this figure for the S-MNL models with and without random ASCs. The more relevant figure is that for models with fixed ASCs, as the likelihood improvement from adding random intercepts is more appropriately ascribed to residual taste heterogeneity.

Differences in results across datasets are striking. For mobile phones, 71% of the log-likelihood improvement that can be achieved by introducing all heterogeneity is achieved by introducing scale heterogeneity <u>alone</u>. For the three medical tests (Pap smear, Tay Sachs) the figures range from 40% to 66%. But in the other datasets scale heterogeneity appears to be less important. In the Pizza delivery and Holiday destination datasets the fraction of the total log-likelihood improvement that can be achieved just by introducing scale is only 13% to 23%, and, in the two Charge Card choice experiments, the figures are only 21% to 22%.

Another way to gauge the importance of scale heterogeneity is by the improvement in pseudo-R^2 when it is added to the model. This ranges from .07 to .23 in the medical and mobile phone data sets,[26] but from only .02 to .05 in the other data sets.

Thus, by this metric, scale heterogeneity appears to be much more important in the medical test and mobile phone data sets than in the pizza, holiday and charge card data sets. What accounts for this contrast? One hypothesis is that scale heterogeneity increases with task complexity. It is intuitive that choices about medical tests are complex, as they involve making decisions about risks/probabilities, which humans have difficultly understanding. Similarly, mobile phones are high-tech goods with attributes like WiFi connectivity, voice commands, USB connections, etc., which consumers may also find difficult to assess. In contrast, attributes of simple consumer goods like pizza and holidays (e.g., thick crust, quality of hotels) may be easier to evaluate. Thus, the results appear consistent with a view that scale heterogeneity is more important in more complex choice contexts.

In summary, we find that two hypotheses seem at least consistent with the observed patterns across datasets. First, heterogeneity (in general) is more important in data sets that involve high involvement decisions (e.g., medical tests). Second, scale heterogeneity is more important in data sets that involve more complex choice objects (i.e., objects with more complex attributes). Of course, we view both of these hypotheses as merely preliminary, but they suggest interesting avenues for future work.

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[26] The low end of this range (.07) comes from the mobile phone dataset. But this improvement appears more substantial when one considers that heterogeneity in general only improves pseudo-R^2 by .10 for mobile phones.

Finally, we tried using observed covariates to explain differences in scale across subjects, as in equation (12). But we had little success and hence do not report the results. Our limited data on subject characteristics did not help to explain scale, nor did our measures of task complexity (number of attributes, number of alternatives, number of attributes that differ among alternatives, number of scenarios). Clearly, more work is needed on this topic.

V.E. Comparing Willingness to Pay Calculations in the MIXL and G-MNL Models

An important issue that arises in choice modelling is the calculation of consumer willingness to pay (WTP) for changes in product attributes. How best to do this in random coefficient models has recently been an active area of research (see, e.g., Sonnier, Ainslie and Otter (2007)). To understand the issue, consider a general model with heterogeneity in (i) the attribute weights, (ii) the price coefficient and (iii) the scale parameter:

$$U_{njt} = \beta_n x_{njt} - \phi_n p_{njt} + \varepsilon_{njt} / \sigma_n \qquad n = 1,...,N; \quad j = 1,...,J; \quad t = 1,...,T, \qquad (14)$$

This model is not identified, and the most common normalization is, of course, to set the scale parameter $\sigma_n=1$ for all n. This gives what is called a model in "utility space." But an alternative is to normalize the price coefficient $\phi_n =1$ for all n. This gives what is called a model in "WTP space." It is useful to write out the two models explicitly:

$$U_{njt} = \beta_n x_{njt} - \phi_n p_{njt} + \varepsilon_{njt} \qquad \qquad \text{"Utility Space"}$$

$$U_{njt}^* = \beta_n^* x_{njt} - p_{njt} + \varepsilon_{njt} / \sigma_n \qquad \qquad \text{"WTP Space"}$$

In the model in "Utility space," WTP for an additional unit of attribute k is β_{nk}/ϕ_n, while for the model in "WTP space" it is simply β_n^*.[27] These two models will give identical fits to the data, and identical estimates of WTP, provided the specification and estimation methods maintain the restrictions that $\beta_n^* = \beta_n / \sigma_n$ and $\phi_n = \sigma_n$.

Practitioners have reported however, that the two models give very different estimates of WTP, and in particular that estimates obtained in "utility space" are often unreasonably large. The source of these differences is that, in practice, it is difficult (or inconvenient) to specify the "Utility space" and "WTP space" models in such a way that they are equivalent.[28] This does not mean however, that the two models are not equivalent if properly specified.

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[27] Analogously, in contingent valuation data, Hanemann (1984) estimated WTP as the ratio of the intercept (representing the hypothetical program) to the price coefficient, while Cameron (1988) uses the expenditure function to estimate WTP directly.

[28] In the utility space model it is common to assume β_n is normal, and that the price coefficient ϕ_n is normal or log normal (to keep it positive). Regardless, the distribution of WTP for attribute k is the ratio (β_{nk}/ϕ_n), where the numerator is normal and the denominator normal or log normal. In contrast, in the WTP space model, the WTP distribution is simply that of β_{nk}^*, which is typically specified as normal (see, e.g., Sonnier et al (2007)). Hence,

It is interesting to examine the issue of estimating WTP in the context of the G-MNL and S-MNL models. Rewriting (7) so the price coefficient is explicit, we have:

$$U_{njt} = [\sigma_n \beta + \gamma \eta_n + (1-\gamma)\sigma_n \eta_n] x_{njt} - [\sigma_n \phi + \gamma \eta_{\phi n} + (1-\gamma)\sigma_n \eta_{\phi n}] p_{njt} + \varepsilon_{njt} \qquad (13)$$

where ϕ denotes the mean price coefficient in the population. If only scale heterogeneity matters, WTP for a unit of attribute k reduces to just (β_k / ϕ), where β_k denotes the kth element of the β vector. This illustrates a strong property of the S-MNL model – there is heterogeneity in coefficients, but not in WTP.[29] However, this does not mean there is no heterogeneity in price sensitivity. For example, in the pure S-MNL model the derivative of the choice probability with respect to price is $\partial P_n(j \mid X_{nt}) / \partial p_{njt} = -P_n(j \mid X_{nt})[1 - P_n(j \mid X_{nt})] \cdot \sigma_n \cdot \phi$. Thus, as $\sigma_n \rightarrow 0$, only unobserved attributes ε matter for choice, and price sensitivity goes to zero.

This illustrates an odd aspect of the "willingness to pay" concept in choice models. A consumer's WTP for an attribute increase is defined as the price increase which, combined with the attribute increase, leaves the deterministic part of his utility for a brand unchanged – and hence the choice probability unchanged. However, consider the same unit increase in the attribute holding price fixed. Given heterogeneity, consumers with the same WTP for the attribute will not in general have the same increase in their choice probability for the brand (even given the same initial probability). Consumers with larger σ_n in the WTP space model, or larger $\beta_n = \beta_n^* \sigma_n$ in the utility space model, will have a larger increase in demand. In other words, it is perfectly compatible that some consumers have a large WTP for an attribute, but that introducing it leads to little increase in their probability of choosing the brand.

In general, WTP in the G-MNL model is given by the ratio:

$$[\sigma_n \beta_k + \gamma \eta_{kn} + (1-\gamma)\sigma_n \eta_{kn}] / [\sigma_n \phi + \gamma \eta_{\phi n} + (1-\gamma)\sigma_n \eta_{\phi n}]$$

While seemingly complicated, this is no more difficult to simulate than (β_{nk}/ϕ_n) in the MIXL model. To guarantee "reasonable" WTP estimates one must choose distributions for σ_n and $\eta_{\phi n}$ so the price coefficient $[\sigma_n \phi + \gamma \eta_{\phi n} + (1-\gamma)\sigma_n \eta_{\phi n}]$ is bounded away from zero. However, in light of our previous comments, we argue that WTP calculations are overemphasized, and that more emphasis should be placed on simulating demand. This will become clear below.

In Table 18, we compare demand and WTP predictions of the G-MNL and MIXL models, again focussing on the Pizza B data set. The top and bottom panels report results for

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it is not surprising that the two models – as typically specified – give very different answers, as there is no reason to expect (β_{nk}/ϕ_n) to be approximately normal. Furthermore, it is not surprising that, in a utility space model, WTP sometimes takes on extreme values; we are taking the ratio of two random variables, where the denominator is normal or log normal, and the ratio can "explode" because the denominator is close to zero.

[29] This is because people with larger attribute weights have a proportionately larger price coefficient.

MIXL and G-MNL, respectively. In the first row we consider an experiment where delivery service A switches from traditional to gourmet pizza, while raising price by \$4 (holding other attributes equal between the two services). Both MIXL and G-MNL predict that roughly 39% of consumer would choose service A under this experiment (as opposed to 50% under the baseline where all attributes are equal). Thus, the demand curves generated by both models imply that roughly 39% of consumers are willing to pay \$4 extra for gourmet pizza.

A similar pattern holds when we look (see the next three rows of each panel) at the demand predictions for fresh ingredients, guaranteed hot pizza, and vegetarian pizza. In each case, demand predictions from the G-MNL and MIXL models are almost identical. This pattern held across all data sets and a wide range of prediction scenarios: the aggregate demand predictions from G-MNL and MIXL are almost identical. The key point is that the difference between the two models arises not from their predictions about aggregate demand, but in their predictions about the distribution of demand across individual types of people.

We turn next to the distribution of WTP implied by each model. For both G-MNL and MIXL this is simulated in the conventional way, as described above. At the 50th percentile, the WTP for gourmet pizza is close to zero according to both models. At the 75th percentile it is about \$3 according to MIXL and \$2.40 according to G-MNL. Thus, given the simulated WTP distributions, both models imply less than 25% of consumers are willing to pay \$4 extra for gourmet pizza. Here we see immediately how WTP distributions generated by both models (calculated in the conventional way) seriously contradict the demand predictions, as we have already seen that both models predict that roughly 39% of consumers would be willing to pay \$4 extra for the gourmet pizza. Indeed, based on the overall WTP distribution, the MIXL model implies that only 23% of consumers would buy the gourmet pizza at a \$4 price premium, and the G-MNL model implies that only 20% of consumers would do so.

VI. Conclusion

Consumer taste heterogeneity is of central importance for many issues in marketing and economics. For at least 25 years there has been a large ongoing research program on how best to model heterogeneity. This research program has produced a large number of alternative modelling approaches. One of the most popular is the so-called "mixed" or "heterogeneous" multinomial logit (MIXL) model. In most applications of MIXL, the vector of consumer utility weights is assumed to have a multivariate normal distribution in the population. But recently, Louviere et al (1999, 2008) have argued, based on estimation of individual level models, that much of the heterogeneity in attribute weights is better described

as a pure scale effect (i.e., across consumers, weights on all attributes are scaled up or down in tandem). This implies that choice behaviour is simply more random for some consumers than others (i.e., holding attribute coefficients fixed, the scale of their error term is greater). This leads to what we have called a "scale heterogeneity" MNL model (S-MNL).

In this paper we have developing a "generalized" multinomial logit model (G-MNL) that nests S-MNL and MIXL. By estimating the G-MNL model on ten datasets, we provide empirical evidence on the importance of scale heterogeneity, and on the relative ability of the MIXL, S-MNL and G-MNL models to fit the data. Our main results show that, based on BIC and CAIC, the G-MNL model is preferred in 7 data sets while the S-MNL model is preferred in the other three. This is striking evidence of the importance of scale heterogeneity – and of the ability of models that include scale heterogeneity to outperform MIXL.

We also show why G-MNL fits better than MIXL. Specifically, it can better explain the behaviour of "extreme" consumers who exhibit near lexicographic preferences (i.e., consumers who nearly always choose the option with a particular attribute, such as lowest price or highest quality, regardless of the attributes of other alternatives). G-MNL is also better able to explain highly "random" consumers whose choices are relatively insensitive to product attributes (i.e., consumer with a large scale of the idiosyncratic error terms).

We went on to show that the G-MNL model allows more flexibility in the posterior distribution of individual level parameters than does MIXL. From an "approximate Bayesian" perspective, the MIXL model with a normal heterogeneity distribution imposes a normal prior on the distribution of individual level parameters. But G-MNL imposes a much more flexible continuous mixture of scaled normals prior. Thus, even given a large amount of data per person, MIXL posteriors depart only modestly from normality. But G-MNL posteriors exhibit sharp departures. These include both multi-modality with spikes in the tails (people who care greatly about particular attributes) and excess kurtosis (people who have small attribute weights or, conversely, a large scale of the error term).

An important avenue for future research is to compare G-MNL with alternative models that also allow a more flexible distribution of individual level parameters, such as mixture-of-normals logit and probit models. The potential advantage of G-MNL is that it achieves a flexible distribution while adding only two parameters to the normal model.

Our analysis also yielded two interesting empirical findings: First, taste heterogeneity in general was far more important for medical decisions than for consumer goods. Second, scale heterogeneity was more important in datasets that involve more complex choice objects. Of course, these empirical findings are quite preliminary, as they involve only ten datasets.

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Figure 1: The G-MNL Model & Its Special Cases

G-MNL
$$\beta_n = \sigma_n \beta + \gamma \eta_n + (1-\gamma)\sigma_n \eta_n$$

$\gamma = 1$ $\gamma = 0$

G-MNL - I
$$\beta_n = \sigma_n \beta + \eta_n$$

G-MNL - II
$$\beta_n = \sigma_n(\beta + \eta_n)$$

$\text{var}(\eta_n) = 0$ $\sigma_n = \sigma = 1$

S-MNL
$$\beta_n = \sigma_n \beta$$

MIXL
$$\beta_n = \beta + \eta_n$$

$\sigma_n = \sigma = 1$ $\text{var}(\eta_n) = 0$

MNL
$$\beta_n = \beta$$
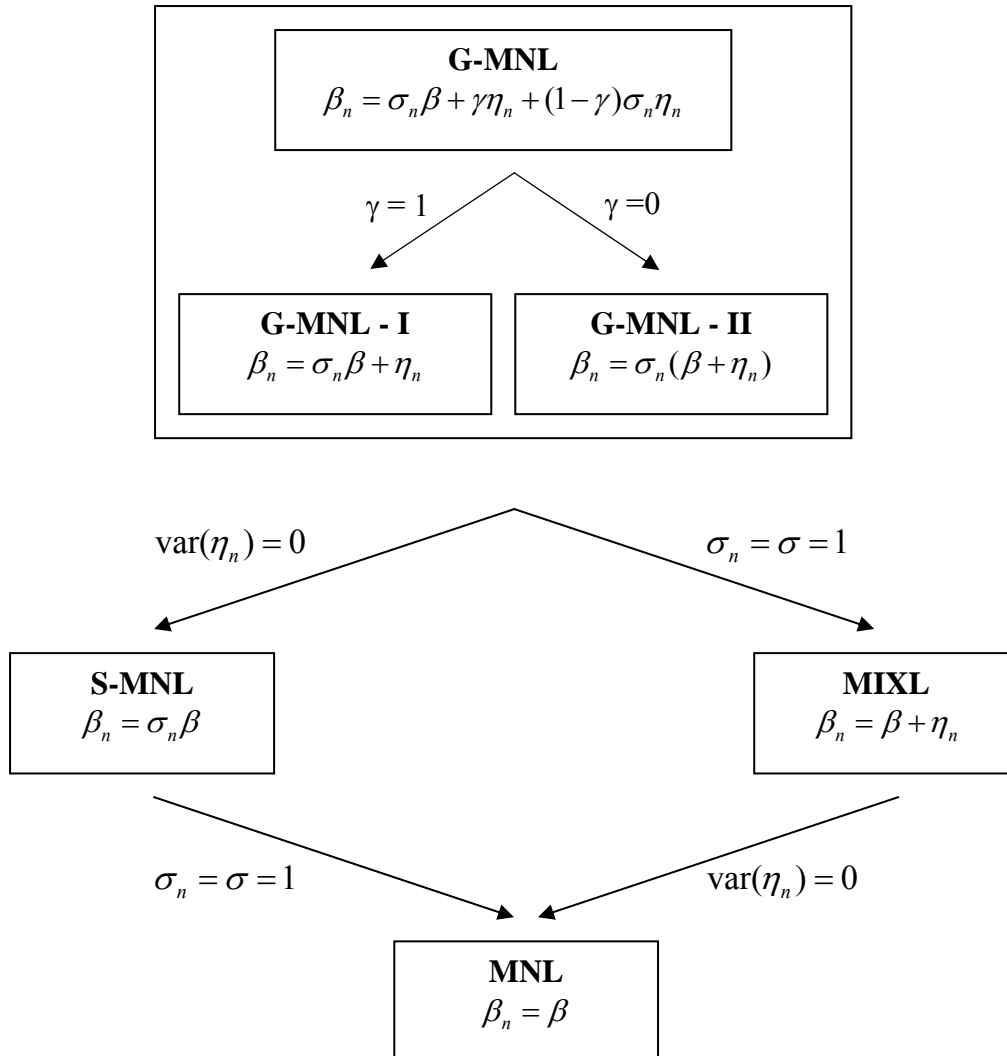
Figure 2: Individuals' log-likelihood from Pizza B data set (N = 328; T = 32; binary choice)

Type 1
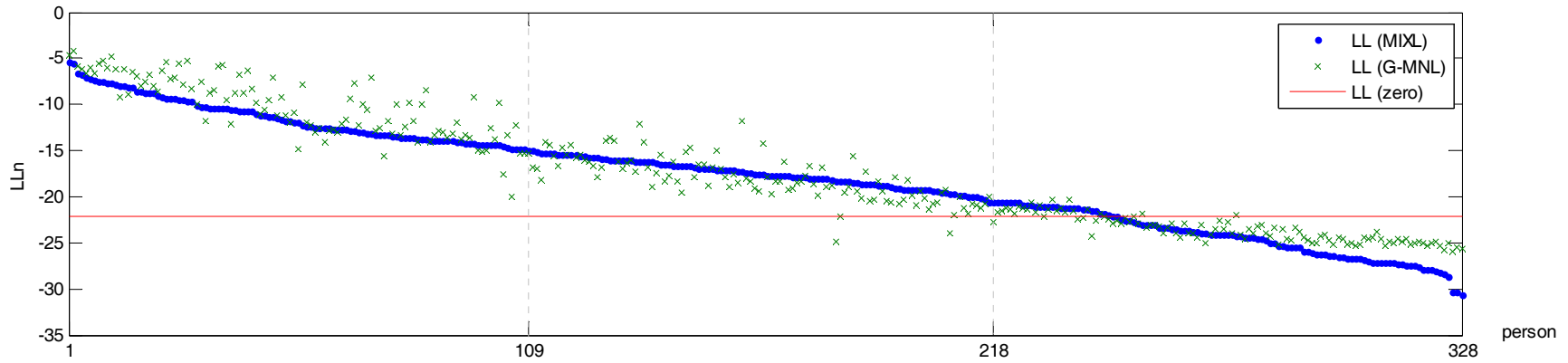
"Extremely persistent" type
22 people – fresh ingredients only
18 people – low price only
14 people – steaming hot only
 8 people – vegetarian only (small overlapped)

Type II

Type III

"More random" type
Utility weights are close to zero.
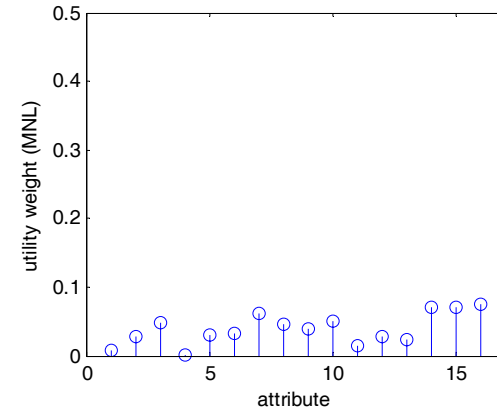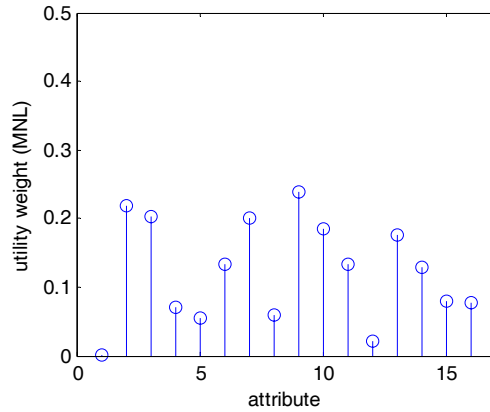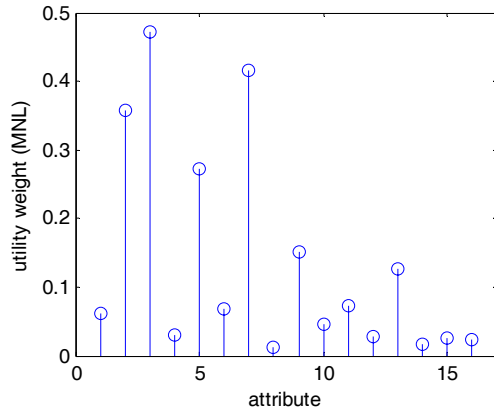
Figure 3: Predicted distribution of probability of choosing firm A from MNL, S-MNL, MIXL and G-MNL models when firm A improves ingredient quality and increases price $4
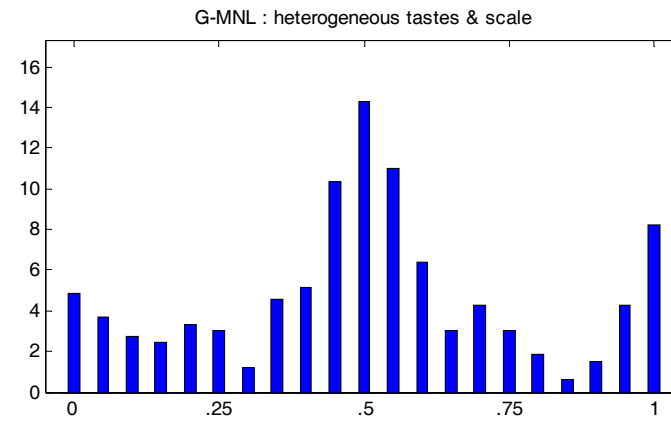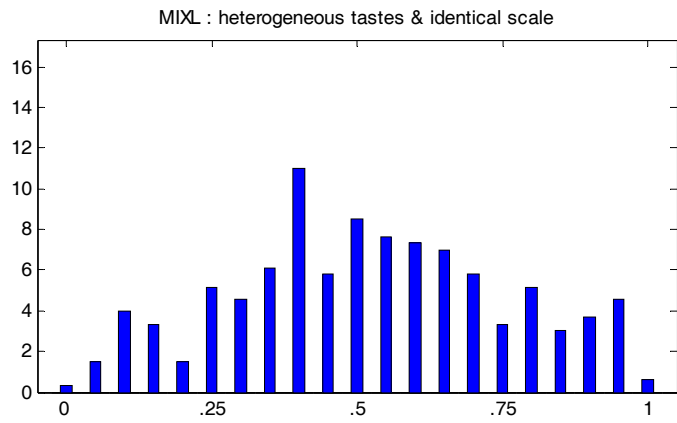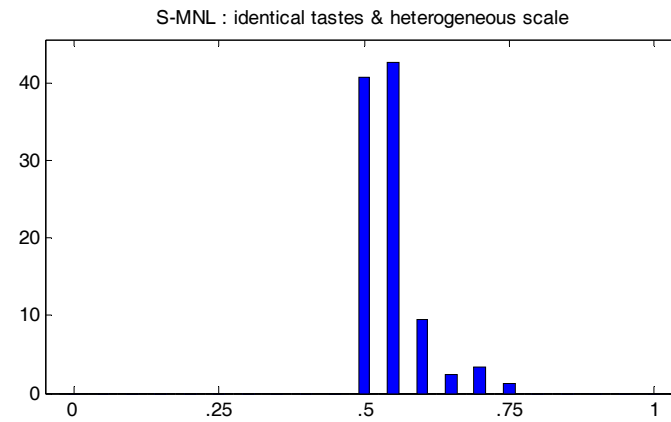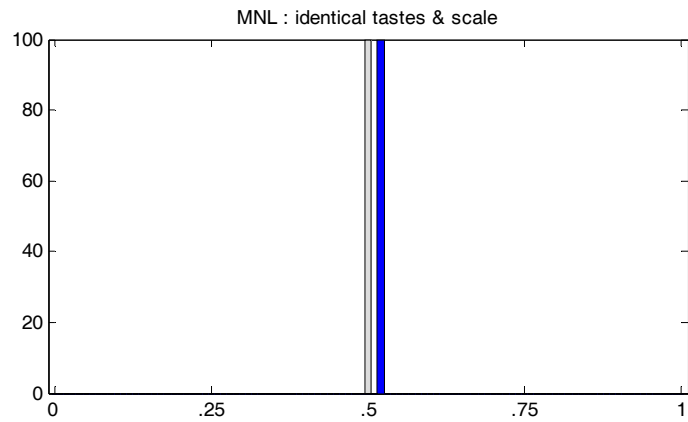
Figure 4: Posterior distribution of individual-level parameters: MIXL vs. G-MNL
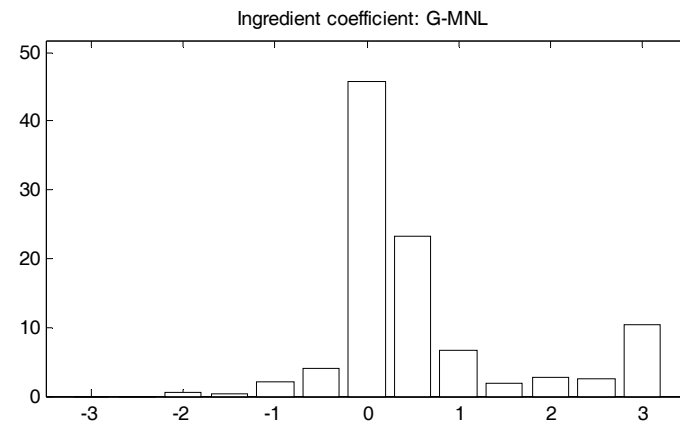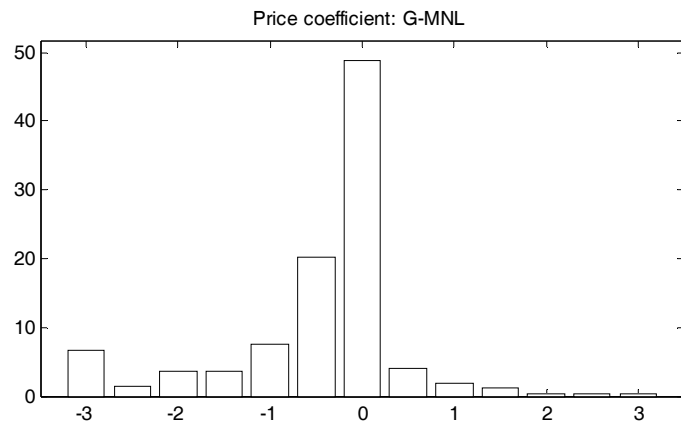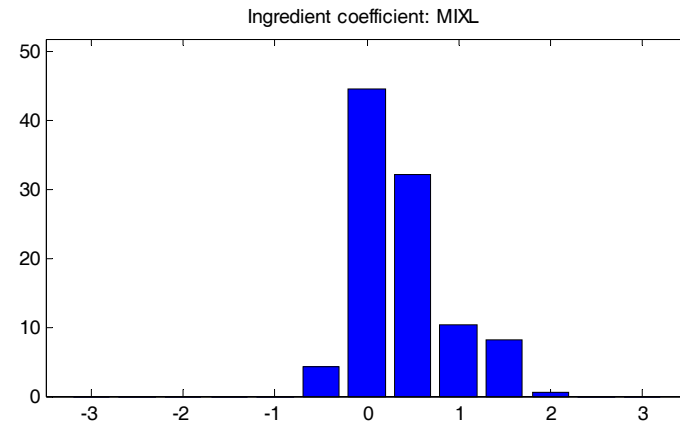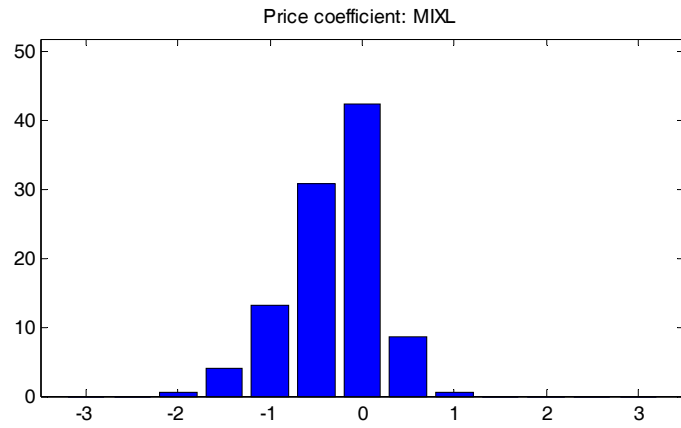
Figure 5: Predicted distribution of probability of choosing firm A from MIXL and G-MNL models when firm A improves one attribute and increases price $4 (Note: attribute scenarios clock-wise are fresh/canned ingredients, gourmet/traditional, hot/warm, vegetarian availability)
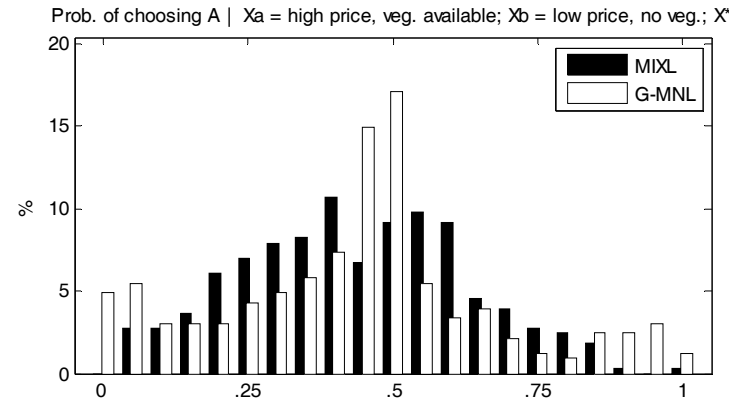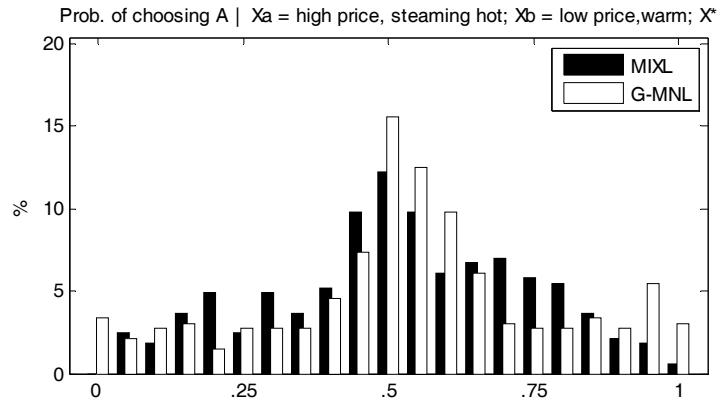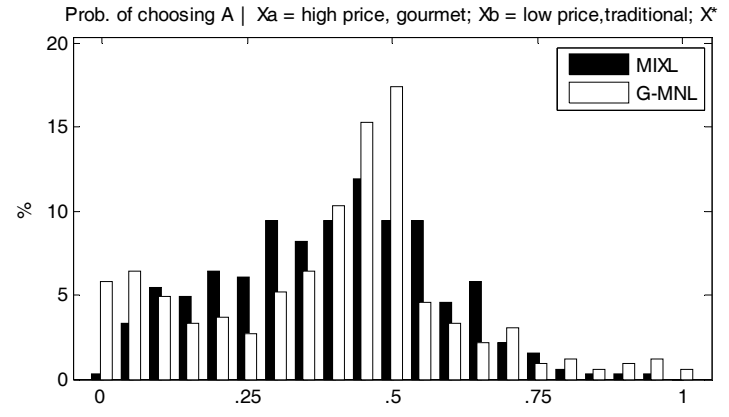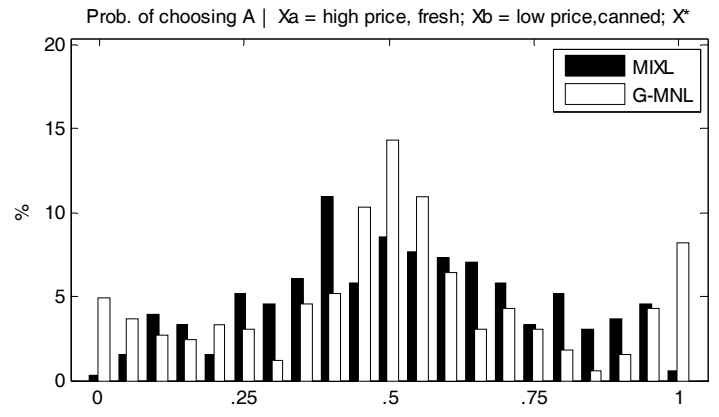
Table 1: Monte Carlo Simulation Results – Papsmear test configuration

No. of draws = 500

	True	$\bar\theta$	s.d.	$\overline{\mathrm{ASE}}$		True	$\bar\theta$	s.d.	$\overline{\mathrm{ASE}}$
β_1	-1.201	-1.192	0.742	0.542	ρ_{12}	-0.392	-0.271	0.377	0.308
β_2	0.466	0.525	0.405	0.444	ρ_{23}	-0.116	-0.031	0.270	0.281
β_3	-1.475	-1.458	0.818	0.601	ρ_{34}	-0.182	-0.186	0.170	0.216
β_4	3.563	3.983	1.045	0.908	ρ_{45}	-0.120	-0.016	0.265	0.406
β_5	1.657	1.928	0.408*	0.551	ρ_{56}	0.398	0.175	0.346*	0.565
β_6	-0.215	-0.241	0.123	0.192	ρ_{13}	0.075	0.211	0.287*	0.245
					ρ_{24}	0.073	0.030	0.319	0.233
σ_1	4.036	4.107	0.704	0.786	ρ_{35}	0.280	0.249	0.237	0.386
σ_2	1.631	1.768	0.469	0.555	ρ_{46}	-0.115	-0.169	0.355	0.497
σ_3	2.454	2.685	0.781	0.724	ρ_{14}	-0.385	-0.231	0.275*	0.233
σ_4	2.992	3.436	0.959	0.782	ρ_{25}	-0.418	-0.494	0.257	0.322
σ_5	1.506	1.787	0.674	0.640	ρ_{36}	-0.483	-0.219	0.329*	0.474
σ_6	0.226	0.490	0.175*	0.254	ρ_{15}	0.132	0.262	0.262*	0.424
					ρ_{26}	0.110	-0.077	0.370*	0.478
					ρ_{16}	0.239	0.048	0.415	0.522
τ	0.890	0.891	0.328	0.214					
γ *	-5.000	-2.699	1.978*	16.215					
γ	0.007	0.156	0.198*	0.232					

The attributes and true values are constructed from the Papsmear data set (X_1 is ASC). The number of draws used in simulated maximum likelihood estimation is 500. We construct 20 artificial data sets (indexed by $m = 1,\ldots,20$) and compare the estimates to the true values. $\bar\theta = \dfrac{1}{20}\sum_{m=1}^{20}\theta_m$; s.d. $= \sqrt{\dfrac{1}{19}\sum_{m=1}^{20}(\theta_m - \bar\theta)^2}$; $\overline{\mathrm{ASE}} = \dfrac{1}{20}\sum_{m=1}^{20}\mathrm{ASE}_m$ where θ_m and ASE_m denote parameter estimates and asymptotic standard errors from each data set. An asterisk indicates the t-statistic for the estimated bias greater than the critical value at the 5% level, i.e., $|t|>2.09$ where $t = \sqrt{20}(\bar\theta - \theta_{true})s.d.^{-1}$. The true values are from Table 11.

Table 2 : Monte Carlo Simulation Results – Holiday A configuration

	True	$\overline{\theta}$	s.d.	$\overline{\text{ASE}}$		True	$\overline{\theta}$	s.d.	$\overline{\text{ASE}}$		True	$\overline{\theta}$	s.d.	$\overline{\text{ASE}}$
β_1	-0.905	-1.134	0.415*	0.242	ρ_{12}	0.216	0.092	0.219*	0.033	ρ_{47}	0.194	0.105	0.125*	0.119
β_2	1.012	1.214	0.619	0.277	ρ_{23}	0.012	0.045	0.303	0.180	ρ_{58}	0.113	0.193	0.156*	0.050
β_3	-0.189	-0.243	0.174	0.111	ρ_{34}	-0.092	-0.129	0.288	0.122	ρ_{15}	-0.065	-0.148	0.227	0.066
β_4	1.924	2.223	0.814	0.449	ρ_{45}	0.243	0.304	0.127*	0.067	ρ_{26}	-0.165	-0.157	0.197	0.113
β_5	1.771	2.032	0.733	0.413	ρ_{56}	0.225	0.255	0.185	0.102	ρ_{37}	-0.070	-0.011	0.294	0.164
β_6	0.860	0.885	0.299	0.209	ρ_{67}	0.094	0.173	0.186	0.143	ρ_{48}	-0.060	0.039	0.167*	0.050
β_7	0.262	0.232	0.180	0.120	ρ_{78}	-0.350	-0.201	0.196*	0.083	ρ_{16}	0.244	0.212	0.247	0.105
β_8	3.200	3.803	1.296	0.745	ρ_{13}	-0.043	-0.081	0.410	0.184	ρ_{27}	0.194	0.217	0.182	0.112
					ρ_{24}	0.446	0.453	0.129	0.050	ρ_{38}	0.106	0.018	0.254	0.076
σ_1	0.982	1.157	0.403	0.241	ρ_{35}	0.056	0.064	0.221	0.098	ρ_{17}	0.620	0.489	0.204*	0.106
σ_2	3.590	4.503	1.503*	0.854	ρ_{46}	0.182	0.162	0.198	0.104	ρ_{28}	0.015	0.035	0.139	0.048
σ_3	0.616	0.598	0.245	0.162	ρ_{57}	-0.358	-0.308	0.199	0.117	ρ_{18}	0.129	0.031	0.230	0.042
σ_4	1.891	2.451	0.785*	0.473	ρ_{68}	0.181	0.154	0.198	0.067					
σ_5	1.693	2.127	0.686*	0.414	ρ_{14}	0.007	-0.057	0.217	0.055					
σ_6	1.006	1.305	0.445*	0.283	ρ_{25}	0.072	0.087	0.126	0.070					
σ_7	0.877	1.119	0.407*	0.247	ρ_{36}	0.403	0.283	0.351	0.132					
σ_8	2.351	3.323	1.212*	0.638										
τ	1.000	0.968	0.344	0.138										
γ *	-1.380	-2.633	2.260*	10.379										
γ	0.200	0.137	0.254*	0.118										

The attributes and true values are constructed from the Holiday A data set. The number of draws used in simulated maximum likelihood estimation is 500. We construct 20 artificial data sets (indexed by m = 1,…,20) and compare the estimates to the true values. $\overline{\theta} = \frac{1}{20}\sum_{m=1}^{20}\theta_m$; s.d. $= \sqrt{\frac{1}{19}\sum_{m=1}^{20}(\theta_m - \overline{\theta})^2}$; $\overline{\text{ASE}} = \frac{1}{20}\sum_{m=1}^{20}\text{ASE}_m$ where θ_m and ASE_m denote parameter estimates and asymptotic standard errors from each data set. An asterisk indicates the t-statistic for the estimated bias greater than the critical value at the 5% level, i.e., |t|>2.09 where $t = \sqrt{20}(\overline{\theta} - \theta_{true})s.d.^{-1}$. The true values are from Table 10, except τ is reduced from 1.51 to 1.00 to make detection of scale heterogeneity more challenging. And γ is increased from 0 to 0.20 so to contrast with Table 1 where γ =0.

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Table 3: Monte Carlo Simulation Results

A. Papsmear test data configuration

True DGP is G-MNL

	MNL	S-MNL	Correlated error		Uncorrelated error	
			MIXL	G-MNL	MIXL	G-MNL
AIC	0	0	0	9	0	11
BIC	0	0	0	0	2	18
CAIC	0	0	0	0	4	16

True DGP is MIXL

	MNL	S-MNL	Correlated error		Uncorrelated error	
			MIXL	G-MNL	MIXL	G-MNL
AIC	0	0	8	10	0	2
BIC	0	0	0	0	19	1
CAIC	0	0	0	0	19	1

True DGP is S-MNL

	MNL	S-MNL	Correlated error		Uncorrelated error	
			MIXL	G-MNL	MIXL	G-MNL
AIC	0	20	0	0	0	0
BIC	0	20	0	0	0	0
CAIC	0	20	0	0	0	0

B. Holiday A data configuration

True DGP is G-MNL

	MNL	S-MNL	Correlated error		Uncorrelated error	
			MIXL	G-MNL	MIXL	G-MNL
AIC	0	0	0	20	0	0
BIC	0	0	0	1	5	14
CAIC	0	0	0	0	6	14

True DGP is MIXL

	MNL	S-MNL	Correlated error		Uncorrelated error	
			MIXL	G-MNL	MIXL	G-MNL
AIC	0	0	13	7	0	0
BIC	0	0	0	0	16	4
CAIC	0	0	0	0	17	3

True DGP is S-MNL

	MNL	S-MNL	Correlated error		Uncorrelated error	
			MIXL	G-MNL	MIXL	G-MNL
AIC	0	20	0	0	0	0
BIC	0	20	0	0	0	0
CAIC	0	20	0	0	0	0

G-MNL or MIXL

	Right	Wrong	
		MIXL	G-MNL
BIC	68	7	5
CAIC	66	10	4
AIC	61	0	19

Table 4: Empirical Data Sets

		No. of choices	No. of choice occasions	No. of respondents	No. of observations	No. of attributes	Products	Meaningful ASC	Complicated attributes	Variation in attributes	All consumers are likely to have same signs
1	Tay Sachs Disease & Cystic Fibrosis test Jewish sample (3 ASCs)	4	16	210	3360	11	Medical	Yes	Yes	High	Yes
2	Tay Sachs Disease & Cystic Fibrosis test General population sample (3 ASCs)	4	16	261	4176	11	Medical	Yes	Yes	High	Yes
3	Mobile phone (1 ASC)	4	8	493	3944	15	Consumption	No	Yes	High	Yes
4	Pizza A (no ASC)	2	16	178	2848	8	Consumption	No	No	Low	No
5	Holiday A (no ASC)	2	16	331	5296	8	Consumption	No	No	Low	No
6	Papsmear test (1 ASC)	2	32	79	2528	6	Medical	Yes	No	Medium	Yes
7	Pizza B (no ASC)	2	32	328	10496	16	Consumption	No	No	Low	No
8	Holiday B (no ASC)	2	32	683	21856	16	Consumption	No	No	Low	No
9	Charge card A (2 ASCs)	3	4	827*	3308	17	Consumption	Yes	No	High	Yes
	Charge card B (3 ASCs)	4	4	827*	3308	18	Consumption	Yes	No	High	Yes

Note: * The respondents in the two credit card data sets are the same. They first complete 4 tasks with 3 options and then answer 4 tasks with 4 options. Some data sets were used in previous research (see Hall et al (2006) for data sets 1 and 2, Fiebig and Hall (2005) for data set 6, and Louviere et al (2008) for data sets 4, 5, 7 and 8).

Table 5: Attributes and Levels

Tay Sachs disease (TS) & Cystic Fibrosis (CF) test: Jewish and General population

	Attributes	Levels
1	ASC for TS test	0,1
2	ASC for CF test	0,1
3	ASC for both tests	0,1
4	Cost to you of being tested for TS	(0,150,300,600)/1000
5	Cost to you of being tested for CF	(0,375,750,1500)/1000
6	Cost to you of being tested both TS and CF	(0,150,…,1800,2100)/1000
7	Whether your doctor recommends you have a test	-1(no),1(yes)
8	The chance that you are a carrier even if the test is negative	(15,30,45,60)/10
9	Whether you are told your carrier status as an individual or as a couple	-1(individual), 1(couple)
10	Risk of being a carrier for TS	log base 10 of (.004,.04,.4,4) x 10^3
11	Risk of being a carrier for CF	log base 10 of (.004,.04,.4,4) x 10^3

Papsmear test

	Attributes	Levels
1	ASC for test	0(no),1(yes)
2	Whether you know doctor	0(no),1(yes)
3	Whether doctor is male	0(no),1(yes)
4	Whether test is due	0(no),1(yes)
5	Whether doctor recommends	0(no),1(yes)
6	Test cost	{0,10,20,30}/10

Pizza A: attributes 1-8; Pizza B: attributes 1-16 (No ASC)

	Attributes	Levels
1	Gourmet	-1 (Traditional),1(Gourmet)
2	Price	-1 ($13),1 ($17)
3	Ingredient freshness	-1 (some canned),1(all fresh ingredients)
4	Delivery time	-1(45 mins),1(30 min)
5	Crust	-1(thin),1(thick)
6	Sizes	-1(single size),1(3 sizes)
7	Steaming hot	-1(warm),1(steaming hot)
8	Late open hours	-1(till 10 pm.), 1 (till 1 am.)
9	Free delivery charge	-1($2),1 (free)
10	Local store	-1(chain),1(local)
11	Baking Method	-1(traditional),1(wood fire)
12	Manners	-1(friendly),1(polite & friendly)
13	Vegetarian availability	-1(no),1(yes)
14	Delivery time guaranteed	-1(no),1(yes)
15	Distance to the outlet	-1(in other suburb),1(in own suburb)
16	Range/variety availability	-1(restricted menu),1(large menu)

Mobile phone

	Attributes	Levels
1	ASC for purchase (phone 1, phone 2 or phone 3)	0,1
	Voice Commands (omitted Text to voice or voice to text converter)	
2	(1) No	-1,0,1
3	(2) Voice dialling by number or name	-1,0,1
4	(3) Voice operating commands	-1,0,1
	Push to Communicate (omitted to share video)	
5	(1) No	-1,0,1
6	(2) to talk	-1,0,1
7	(3) to share pictures or video	-1,0,1
	Email Access (omitted email with attachments)	
8	(1) personal emails	-1,0,1
9	(2) corporate emails (VPN, RIM)	-1,0,1
10	(3) both personal & corporate emails on multiple accounts	-1,0,1
11	WiFi	-1(No), 1(Yes)
12	USB Cable or Cradle connection	-1(No), 1(Yes)
13	Thermometer	-1(No), 1(Yes)
14	Flashlight	-1(No), 1(Yes)
15	Price	(0,11.7,19.5,…,497.25, 563.55)/100 (36 unique values)

Holiday A: attributes 1-8; Holiday B: attributes 1-16 (No ASC)

	Attributes	Levels
1	Price	-1($999), 1 ($1200)
2	Overseas destination	-1(Australia), 1(Overseas)
3	Airline	-1(Qantas), 1(Virgin)
4	Length of stay	-1(7), 1(12)
5	Meal inclusion	-1(no), 1(yes)
6	Local tours availability	-1(no), 1(yes)
7	Peak season	-1(off-peak), 1(peak)
8	4-star Accommodation	-1(2-star), 1 (4-star)
9	Length of Trip	-1(3 hours), 1 (5 hours)
10	Cultural activities	-1(Historical sites), 1 (museum)
11	Distance from hotel to attractions	-1 (200m), 1 (5km)
12	Swimming pool avail.	-1(no), 1(yes)
13	Helpfulness	-1(helpful), 1(very helpful)
14	Individual tour	-1 (organized tour), 1 (individual)
15	Beach availability	-1(no), 1(yes)
16	Brand	-1(Jetset), 1 (Creative Holidays)

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Table 5 (continued)

Charge card A & B (no transaction option for Card A)

	Attributes	Levels
1	ASC for credit card	0,1
2	ASC for debit card	0,1
3	ASC for transaction card	0,1
4	Annual fee	(-70,-30,10,70)/10
5	Transaction fee	(-.5, -.3, .1, .5)*10
6	Permanent overdraft facility	
	credit:	0 (N/A)
	debit/trans:	-1(Available), 1(Not available)
7	overdraft interest free days (up to)	(-30, 5, 15, 30)/10
8	Interest charged on outstanding credit/overdraft	(-.075, -.035, .015, .075)*100
9	Interest earned on positive balance	
	credit:	(-.025, .025)*100
	debit/trans:	0.015*100
10	Cash advance interest rate	
	credit:	(-.035, -.005, .015, .035)*100
	debit/trans:	0.015*100
	Location and shop access (omitted EFTPOS + telephone + internet + mail, use world wide)	
11	(1) Nowhere else, use Australia wide	-1,0,1
12	(2) EFTPOS + telephone + internet + mail, use Australia wide	-1,0,1
13	(3) Nowhere else, use world wide	-1,0,1
14	Loyalty scheme	0(None), 1(Frequent Flyer/Fly Buys and other rewards)
15	Loyalty scheme annual fees	(-40,40)/10 if Loyalty scheme = 1; 0 if Loyalty scheme = 0
16	Loyalty scheme points earning	-1(points on outstanding balance interest paid on), 1(points on purchases only)
17	Merchant surcharge for using card	(-.03, -.01, .01, .03)*100
18	Surcharge for transactions at other banks ATM	
	credit:	-1.5
	debit/trans:	(-1.5, -.5, .5, 1.5)

Table 6: Tay Sachs Disease (TS) and Cystic Fibrosis (CF) test: Jewish sample (3 ASCs)

	MNL		Scale heterogeneity S-MNL		Random Effects S-MNL		Correlated errors Mixed logit MIXL		G-MNL		Uncorrelated errors Mixed logit MIXL		G-MNL	
	est	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.
ASC for TS test	**-0.57**	0.14	**-2.24**	0.11	**-0.57**	0.20	-0.67	0.47	-0.17	0.41	**-1.07**	0.18	**-0.95**	0.17
ASC for CF test	**-0.82**	0.15	**-2.39**	0.13	**-0.88**	0.22	-0.74	0.42	-0.27	0.36	**-1.14**	0.20	**-1.15**	0.19
ASC for both tests	-0.08	0.15	**-3.01**	0.12	0.01	0.27	-0.38	0.52	0.01	0.45	-0.43	0.20	-0.32	0.18
TS cost	**-2.51**	0.24	**-2.87**	0.40	**-3.45**	0.34	**-4.75**	0.63	**-5.62**	0.78	**-4.24**	0.34	**-5.41**	0.49
CF cost	**-1.43**	0.13	**-1.38**	0.20	**-1.96**	0.20	**-3.24**	0.38	**-3.57**	0.42	**-3.07**	0.25	**-4.11**	0.35
Both cost	**-1.20**	0.07	**-0.95**	0.13	**-2.70**	0.17	**-3.65**	0.26	**-4.25**	0.37	**-3.13**	0.20	**-4.23**	0.24
Recommend	**0.33**	0.04	**0.66**	0.11	**0.56**	0.06	**0.95**	0.13	**1.00**	0.19	**0.64**	0.08	**0.81**	0.10
Inaccuracy	**-0.12**	0.02	**0.22**	0.04	**-0.15**	0.03	-0.14	0.09	**-0.36**	0.10	**-0.12**	0.04	**-0.19**	0.05
Form	0.07	0.04	0.13	0.08	0.12	0.05	0.28	0.16	0.15	0.19	**0.24**	0.08	0.24	0.10
Own risk of TS	**0.50**	0.03	**1.62**	0.17	**1.05**	0.08	**1.39**	0.12	**1.67**	0.18	**1.10**	0.07	**1.20**	0.09
Own risk of CF	**0.47**	0.04	**1.27**	0.14	**1.02**	0.07	**1.26**	0.12	**1.50**	0.18	**1.02**	0.07	**1.37**	0.10
τ	-		**1.14**	0.09	**0.64**	0.06	-		**0.45**	0.08	-		**0.52**	0.05
γ									0.11	0.15			0.01	0.02
No. of parameters	11		12		18		77		79		22		24	
LL	-3717		-3223		-2815		-2500		-2480		-2753		-2744	
AIC	7455		6469		5666		5154		**5118**		5550		5535	
BIC	7523		6543		5777		5626		**5601**		5684		5682	
CAIC	7534		6555		5795		5703		**5680**		5706		5706	

Note: Bold estimates are statistically significant at the 1% level.

Table 7: Tay Sachs Disease (TS) and Cystic Fibrosis (CF) test: General population sample (3 ASCs)

	MNL		Scale heterogeneity S-MNL		Random Effects S-MNL		Correlated errors Mixed logit MIXL		G-MNL		Uncorrelated errors Mixed logit MIXL		G-MNL	
	est	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.
ASC for TS test	**-2.18**	0.13	**-3.43**	0.11	**-3.14**	0.21	**-3.24**	0.32	**-3.29**	0.31	**-3.20**	0.18	**-3.36**	0.17
ASC for CF test	**-1.92**	0.12	**-3.18**	0.11	**-2.75**	0.20	**-2.61**	0.33	**-2.64**	0.29	**-2.61**	0.17	**-2.92**	0.15
ASC for both tests	**-1.49**	0.13	**-4.11**	0.11	**-3.23**	0.29	**-3.13**	0.44	**-3.73**	0.40	**-2.75**	0.20	**-3.03**	0.19
TS cost	**-1.12**	0.25	**-1.60**	0.40	**-1.55**	0.27	**-2.71**	0.50	**-2.99**	0.52	**-2.04**	0.32	**-1.62**	0.27
CF cost	**-0.73**	0.10	**-0.82**	0.17	**-0.99**	0.13	**-2.17**	0.30	**-2.56**	0.32	**-1.60**	0.15	**-1.24**	0.14
Both cost	**-0.51**	0.06	**-0.51**	0.12	**-1.21**	0.13	**-2.13**	0.23	**-2.27**	0.22	**-1.49**	0.14	**-1.37**	0.11
Recommend	**0.35**	0.03	**1.11**	0.15	**0.68**	0.06	**0.95**	0.12	**0.94**	0.12	**0.69**	0.07	**0.70**	0.08
Inaccuracy	0.02	0.02	**0.45**	0.06	**0.09**	0.03	0.10	0.07	0.02	0.06	-0.01	0.05	0.10	0.04
Form	0.06	0.03	**0.23**	0.07	0.09	0.05	0.25	0.10	0.21	0.13	**0.17**	0.06	**0.18**	0.06
Own risk of TS	**0.39**	0.03	**1.54**	0.19	**1.01**	0.08	**1.06**	0.11	**1.26**	0.13	**0.86**	0.06	**0.85**	0.06
Own risk of CF	**0.37**	0.03	**1.43**	0.18	**0.97**	0.08	**0.99**	0.10	**1.16**	0.10	**0.87**	0.06	**0.87**	0.06
τ	-		**1.53**	0.11	**0.97**	0.07	-		**0.56**	0.07	-		**0.64**	0.06
γ									**0.64**	0.08			**0.99**	0.02
No. of parameters	11		12		18		77		79		22		24	
LL	-4649		-3567		-3226		-2946		-2914		-3232		-3199	
AIC	9320		7158		6487		6047		**5986**		6507		6446	
BIC	9390		7234		6601		6535		**6487**		6646		6598	
CAIC	9401		7246		6619		6612		**6566**		6668		6622	

Note: Bold estimates are statistically significant at the 1% level.

Table 8: Mobile phones (1 ASC)

	MNL		Scale heterogeneity S-MNL		Random Effects S-MNL		Correlated errors 1-Factor MIXL		Correlated errors 1-Factor G-MNL		Uncorrelated errors Mixed logit MIXL		Uncorrelated errors G-MNL	
	est	std. err.	est.	std.err.	est.	std.err.	est.	std.err.	est.	std.err.	est.	std.err.	est.	std.err.
ASC for purchase	**-0.80**	0.05	0.00	0.04	**-0.35**	0.12	**-0.54**	0.11	**-0.51**	0.13	**-0.50**	0.11	**-0.46**	0.12
No voice comm.	0.04	0.04	0.03	0.13	0.06	0.05	0.03	0.05	0.04	0.06	0.04	0.05	0.04	0.06
Voice dialing	**0.08**	0.04	0.20	0.14	0.05	0.06	0.03	0.06	0.07	0.06	**0.10**	0.05	0.09	0.06
Voice operation	**-0.12**	0.04	-0.22	0.17	-0.11	0.06	-0.10	0.06	-0.12	0.07	**-0.13**	0.05	**-0.12**	0.06
No push to com.	0.06	0.04	0.15	0.16	**0.12**	0.06	0.06	0.05	0.09	0.06	0.05	0.05	0.06	0.06
Push to talk	0.03	0.04	0.07	0.18	0.03	0.07	0.04	0.06	0.03	0.07	0.05	0.05	0.07	0.06
Push to share pics/video	-0.02	0.04	-0.14	0.19	-0.08	0.07	-0.04	0.06	-0.03	0.07	-0.02	0.05	-0.04	0.06
Personal e-mail	-0.07	0.04	-0.09	0.16	-0.04	0.06	-0.09	0.06	-0.11	0.07	-0.08	0.05	-0.07	0.06
Corporate e-mail	**0.09**	0.04	0.24	0.19	0.08	0.07	0.09	0.05	0.10	0.06	0.08	0.05	0.08	0.06
both e-mails	-0.05	0.04	-0.16	0.17	-0.08	0.06	-0.01	0.06	-0.003	0.06	-0.03	0.05	-0.04	0.06
WiFi	0.001	0.02	-0.03	0.09	-0.02	0.03	0.02	0.03	0.02	0.04	-0.002	0.03	-0.01	0.03
USB Cable/Cradle	**0.06**	0.03	0.02	0.09	**0.08**	0.04	**0.07**	0.03	**0.08**	0.04	**0.07**	0.03	**0.08**	0.03
Thermometer	**0.07**	0.03	0.02	0.08	0.05	0.03	**0.06**	0.03	0.06	0.04	**0.07**	0.03	**0.08**	0.03
Flashlight	0.05	0.03	0.07	0.08	0.01	0.03	0.05	0.03	**0.08**	0.04	0.05	0.03	0.04	0.03
Price/100	**-0.32**	0.02	**-3.07**	0.47	**-1.02**	0.16	**-0.76**	0.06	**-0.84**	0.10	**-0.76**	0.06	**-0.88**	0.10
τ	-		**2.14**	0.13	**1.45**	0.15	-		**0.77**	0.19	-		**0.66**	0.18
γ									0.28	0.24			0.01	0.49
No. of parameters	15		16		17		45		47		30		32	
LL	-4475		-4102		-3990		-3962		-3949		-3971		-3966	
AIC	8980		8236		8014		8014		**7986**		8002		7996	
BIC	9074		8336		**8121**		8297		8281		8190		8197	
CAIC	9089		8352		**8138**		8342		8328		8220		8229	

Note: Bold estimates are statistically significant at the 5% level.

Table 9: Pizza A (No ASC)

	MNL		Scale heterogeneity S-MNL		Correlated errors Mixed logit MIXL		G-MNL		Uncorrelated errors Mixed logit MIXL		G-MNL	
	est	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.
Gourmet	0.02	0.02	0.03	0.04	-0.01	0.06	0.16	0.45	0.03	0.05	**0.45**	0.22
Price	**-0.16**	0.02	**-0.19**	0.05	**-0.38**	0.06	-3.44	1.81	**-0.35**	0.06	**-1.67**	0.65
Ingredient freshness	**0.48**	0.03	**1.45**	0.29	**1.06**	0.10	**11.10**	5.46	**0.96**	0.08	**4.65**	1.69
Delivery time	**0.09**	0.03	**0.16**	0.08	**0.17**	0.07	1.24	0.72	**0.16**	0.05	**0.74**	0.35
Crust	0.02	0.03	0.01	0.04	0.08	0.08	0.70	0.70	0.02	0.06	0.42	0.26
Sizes	**0.09**	0.03	**0.12**	0.06	**0.17**	0.07	1.21	0.91	**0.20**	0.05	**0.81**	0.37
Steaming hot	**0.38**	0.03	**1.02**	0.24	**0.86**	0.11	**8.93**	4.32	**0.87**	0.08	**4.46**	1.64
Late open hours	**0.04**	0.02	0.08	0.06	0.07	0.06	0.39	0.55	0.07	0.05	0.29	0.17
τ	-		**1.69**	0.18	-		**2.00**	0.26	-		**1.79**	0.24
γ							0.02	0.01			0.01	0.01
No. of parameters	8		9		44		46		16		18	
LL	-1657		-1581		-1379		-1324		-1403		-1373	
AIC	3330		3179		2847		**2741**		2838		2782	
BIC	3378		3233		3109		3015		2933		**2889**	
CAIC	3386		3242		3153		3061		2949		**2907**	

Note: Bold estimates are statistically significant at the 5% level.

Table 10: Holiday A (No ASC)

	MNL		Scale heterogeneity S-MNL		Correlated errors Mixed logit MIXL		G-MNL		Uncorrelated errors Mixed logit MIXL		G-MNL	
	est	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.
Price	**-0.16**	0.02	**-0.17**	0.03	**-0.36**	0.04	**-0.91**	0.22	**-0.33**	0.04	**-0.74**	0.12
Overseas destination	**0.09**	0.02	**0.17**	0.02	**0.19**	0.07	**1.01**	0.26	**0.23**	0.06	**0.32**	0.11
Airline	-0.01	0.02	-0.05	0.02	-0.05	0.03	-0.19	0.11	-0.02	0.03	-0.1	0.06
Length of stay	**0.26**	0.02	**0.35**	0.04	**0.55**	0.05	**1.92**	0.42	**0.52**	0.04	**1.24**	0.19
Meal inclusion	**0.27**	0.02	**0.31**	0.03	**0.61**	0.05	**1.77**	0.39	**0.56**	0.04	**1.29**	0.2
Local tours availability	**0.09**	0.02	**0.09**	0.03	**0.23**	0.05	**0.86**	0.21	**0.19**	0.03	**0.45**	0.09
Peak season	0.03	0.02	0	0.03	0.08	0.05	0.26	0.12	0.06	0.03	0.14	0.07
4-star Accommodation	**0.44**	0.02	**0.65**	0.05	**0.92**	0.06	**3.2**	0.68	**0.86**	0.06	**1.99**	0.29
τ	-		**0.97**	0.08	-		**1.51**	0.14	-		**1.19**	0.10
γ							0.00	0.14			0.00	0.18
No. of parameters	8		9		44		46		16		18	
LL	-3066		-2967		-2504		-2469		-2553		-2519	
AIC	6149		5952		5097		**5031**		5139		5074	
BIC	6201		6011		5386		5333		5244		**5192**	
CAIC	6209		6020		5430		5379		5260		**5210**	

Note: Bold estimates are statistically significant at the 1% level.

Table 11: Papsmear test (1 ASC)

	MNL		Scale heterogeneity S-MNL		Random effects S-MNL		Correlated errors Mixed logit MIXL		G-MNL		Uncorrelated errors Mixed logit MIXL		G-MNL	
	est	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.
ASC for test	**-0.40**	0.14	**-1.93**	0.11	-0.60	0.37	**-1.93**	0.57	**-1.20**	0.45	**-1.26**	0.30	**-0.80**	0.31
If know doctor	**0.32**	0.09	**1.83**	0.45	**0.63**	0.14	**0.97**	0.29	0.47	0.30	**0.78**	0.18	**0.68**	0.21
If doctor is male	**-0.70**	0.09	**-0.97**	0.34	**-1.24**	0.16	-1.07	0.46	**-1.48**	0.53	**-1.39**	0.30	**-1.99**	0.32
If test is due	**1.23**	0.10	**5.35**	1.38	**2.74**	0.29	**3.33**	0.48	**3.56**	0.58	**3.26**	0.31	**3.35**	0.42
If doctor recommends	**0.51**	0.10	**2.68**	0.77	**0.74**	0.17	**1.31**	0.30	**1.66**	0.46	**1.33**	0.23	**1.65**	0.31
Test cost	**-0.08**	0.04	0.00	0.13	-0.17	0.07	-0.18	0.12	-0.22	0.16	-0.22	0.09	**-0.28**	0.09
τ	-		**1.45**	0.18	**0.81**	0.11	-		**0.89**	0.18	-		**1.00**	0.11
γ									0.00	0.42			0.01	0.38
No. of parameters	6		7		8		27		29		12		14	
LL	-1528		-1124		-1063		-923		-914		-945		-935	
AIC	3069		2262		2143		1899		**1887**		1914		1897	
BIC	3104		2303		2189		2057		2056		1984		**1979**	
CAIC	3110		2310		2197		2084		2085		1996		**1993**	

Note: Bold estimates are statistically significant at the 1% level.

Table 12: Pizza B (No ASC)

	MNL		Scale heterogeneity S-MNL		Correlated errors 1-Factor MIXL		Correlated errors 1-Factor G-MNL		Uncorrelated errors Mixed logit MIXL		Uncorrelated errors G-MNL	
	est	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.
Gourmet	0.01	0.01	**0.05**	0.01	0.01	0.02	0.06	0.03	0.01	0.02	0.03	0.03
Price	**-0.17**	0.01	**-0.25**	0.02	**-0.32**	0.03	**-0.54**	0.05	**-0.30**	0.03	**-0.79**	0.07
Ingredient freshness	**0.21**	0.01	**0.36**	0.03	**0.39**	0.03	**0.74**	0.06	**0.34**	0.03	**1.05**	0.08
Delivery time	**0.03**	0.01	0.04	0.02	0.05	0.02	**0.15**	0.04	0.05	0.02	**0.15**	0.04
Crust	**0.08**	0.01	**0.09**	0.01	**0.16**	0.03	**0.33**	0.05	**0.08**	0.03	**0.59**	0.06
Sizes	**0.07**	0.01	**0.08**	0.02	**0.10**	0.02	**0.17**	0.03	**0.11**	0.02	**0.23**	0.03
Steaming hot	**0.20**	0.01	**0.35**	0.03	**0.34**	0.03	**0.76**	0.05	**0.34**	0.02	**1.15**	0.09
Late open hours	**0.04**	0.01	0.02	0.02	**0.07**	0.02	**0.12**	0.03	**0.08**	0.02	0.08	0.04
Free delivery charge	**0.12**	0.01	**0.15**	0.02	**0.21**	0.02	**0.41**	0.04	**0.20**	0.02	**0.56**	0.06
Local store	**0.08**	0.01	**0.06**	0.02	**0.13**	0.02	**0.24**	0.04	**0.15**	0.02	**0.42**	0.05
Baking Method	**0.07**	0.01	**0.07**	0.02	**0.10**	0.02	**0.22**	0.03	**0.11**	0.02	**0.25**	0.04
Manners	0.01	0.01	-0.004	0.02	0.02	0.02	-0.07	0.04	0.02	0.02	0.01	0.04
Vegetarian availability	**0.09**	0.01	**0.06**	0.01	**0.11**	0.03	**0.21**	0.05	**0.13**	0.03	**0.34**	0.06
Delivery time guaranteed	**0.07**	0.01	**0.07**	0.02	**0.11**	0.02	**0.16**	0.03	**0.11**	0.02	**0.15**	0.04
Distance to the outlet	**0.06**	0.01	0.04	0.02	**0.09**	0.02	**0.12**	0.03	**0.09**	0.02	0.10	0.04
Range/variety availability	**0.06**	0.02	0.04	0.02	**0.09**	0.02	**0.12**	0.04	**0.09**	0.02	**0.14**	0.05
τ	-		**1.22**	0.08	-		**1.12**	0.06	-		**1.26**	0.06
γ							0.01	0.01			0.01	0.01
No. of parameters	16		17		48		50		32		34	
LL	-6747		-6607		-5857		-5668		-5892		-5689	
AIC	13525		13249		11810		**11436**		11849		11446	
BIC	13641		13372		12159		11799		12081		**11693**	
CAIC	13657		13389		12207		11849		12113		**11727**	

Note: Bold estimates are statistically significant different at the 1% level.

Table 13: Holiday B (No ASC)

	MNL		Scale heterogeneity S-MNL		Correlated errors 1-Factor MIXL		Correlated errors 1-Factor G-MNL		Uncorrelated errors Mixed logit MIXL		Uncorrelated errors G-MNL	
	est	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.	est.	s.e.
Price	**-0.16**	0.01	**-0.16**	0.01	**-0.25**	0.02	**-0.31**	0.02	**-0.25**	0.02	**-0.34**	0.02
Overseas destination	**0.08**	0.01	**0.12**	0.01	**0.17**	0.02	**0.21**	0.03	**0.12**	0.02	**0.24**	0.03
Airline	-0.02	0.01	-0.02	0.01	**-0.03**	0.01	-0.03	0.02	**-0.03**	0.01	-0.03	0.02
Length of stay	**0.18**	0.01	**0.19**	0.01	**0.30**	0.02	**0.40**	0.02	**0.29**	0.02	**0.40**	0.02
Meal inclusion	**0.20**	0.01	**0.24**	0.02	**0.33**	0.02	**0.45**	0.02	**0.34**	0.02	**0.46**	0.03
Local tours availability	**0.07**	0.01	**0.08**	0.01	**0.11**	0.01	**0.15**	0.02	**0.11**	0.01	**0.17**	0.02
Peak season	0.003	0.01	0.02	0.01	0.003	0.01	0.005	0.01	0.001	0.01	-0.01	0.02
4-star Accommodation	**0.34**	0.01	**0.54**	0.03	**0.51**	0.02	**0.65**	0.03	**0.50**	0.02	**0.69**	0.03
Length of Trip	-0.02	0.01	**-0.03**	0.01	**-0.04**	0.01	-0.03	0.01	**-0.03**	0.01	-0.03	0.02
Cultural activities	**-0.05**	0.01	**-0.05**	0.01	**-0.09**	0.01	**-0.11**	0.02	**-0.09**	0.01	**-0.12**	0.01
Distance from hotel to attractions	**-0.08**	0.01	**-0.07**	0.01	**-0.13**	0.01	**-0.17**	0.02	**-0.12**	0.01	**-0.17**	0.02
Swimming pool avail.	**0.09**	0.01	**0.09**	0.01	**0.15**	0.01	**0.19**	0.02	**0.15**	0.01	**0.23**	0.02
Helpfulness	**0.04**	0.01	**0.03**	0.01	**0.06**	0.01	**0.08**	0.02	**0.06**	0.01	**0.07**	0.02
Individual tour	**0.07**	0.01	**0.07**	0.01	**0.11**	0.02	**0.19**	0.02	**0.13**	0.02	**0.20**	0.02
Beach availability	**0.11**	0.01	**0.10**	0.01	**0.19**	0.01	**0.23**	0.02	**0.18**	0.01	**0.22**	0.02
Brand	0.001	0.01	-0.01	0.02	-0.004	0.02	0.01	0.02	0.003	0.02	0.004	0.02
τ	-		**1.13**	0.05	-		**0.67**	0.04	-		**0.72**	0.04
γ							0.01	0.02			0.01	0.02
No. of parameters	16		17		48		50		32		34	
LL	-13478		-13027		-11570		-11446		-11600		-11476	
AIC	26988		26088		23236		**22992**		23263		23019	
BIC	27116		26224		23619		23391		23519		**23291**	
CAIC	27132		26241		23667		23441		23551		**23325**	

Note: Bold estimates are statistically significant at the 1% level.

Table 14: Charge Card A (2 ASCs)

	MNL		Scale heterogeneity S-MNL		Random Effects S-MNL		Correlated errors 1-Factor MIXL		Correlated errors 1-Factor G-MNL		Uncorrelated errors Mixed logit MIXL		Uncorrelated errors G-MNL	
	est	s.e.	est	s.e.	est	s.e.	est	s.e.	est	s.e.	est	s.e.	est	s.e.
ASC for credit	**-0.85**	0.08	**-1.00**	0.05	**-0.90**	0.18	**-1.31**	0.27	**-1.31**	0.27	**-2.51**	0.36	**-3.15**	0.34
ASC for debit	**-0.99**	0.08	**-1.35**	0.05	**-1.22**	0.18	**-2.07**	0.31	**-2.05**	0.32	**-3.34**	0.44	**-4.16**	0.46
annual fee	**-0.08**	0.01	**-0.14**	0.02	**-0.13**	0.01	**-0.18**	0.02	**-0.19**	0.02	**-0.27**	0.03	**-1.14**	0.23
trans fee	**-0.53**	0.07	**-0.80**	0.11	**-0.82**	0.11	**-1.34**	0.20	**-1.37**	0.21	**-1.53**	0.27	**-7.90**	1.77
overdraft facility	**0.28**	0.06	**0.58**	0.09	**0.43**	0.09	**0.70**	0.15	**0.75**	0.16	**0.80**	0.20	**4.05**	0.93
overdraft free days	0.04	0.02	**0.06**	0.02	**0.06**	0.02	0.07	0.03	0.07	0.03	0.08	0.04	**0.35**	0.13
interest charged	**-0.43**	0.06	**-1.26**	0.15	**-0.67**	0.09	**-1.00**	0.15	**-1.01**	0.16	**-1.29**	0.21	**-6.45**	1.26
interest earned	**0.04**	0.01	0.02	0.01	0.04	0.02	0.06	0.03	0.06	0.03	0.08	0.04	0.31	0.13
access_1	-0.05	0.02	**-0.06**	0.02	**-0.08**	0.02	-0.05	0.03	-0.06	0.03	**-0.14**	0.05	-0.30	0.16
access_2	**-0.21**	0.05	**-0.35**	0.07	**-0.31**	0.08	**-0.42**	0.13	**-0.39**	0.12	**-0.54**	0.16	**-1.77**	0.61
access_3	0.06	0.05	**0.26**	0.07	0.11	0.07	0.22	0.11	0.23	0.11	0.32	0.14	0.81	0.50
cash advance interest	-0.06	0.05	**-0.39**	0.07	-0.12	0.08	-0.29	0.13	-0.34	0.14	-0.33	0.15	**-1.91**	0.63
loyal scheme	**0.26**	0.06	**0.56**	0.08	**0.33**	0.08	**0.44**	0.14	**0.47**	0.15	0.37	0.20	**3.18**	0.83
loyal fee	**-0.03**	0.01	**-0.04**	0.01	**-0.05**	0.01	**-0.06**	0.02	**-0.06**	0.02	**-0.08**	0.03	-0.15	0.11
loyal point	-0.04	0.04	0.04	0.04	0.04	0.06	0.07	0.09	0.07	0.09	0.13	0.13	0.73	0.49
merchant surcharge	-0.02	0.01	**-0.09**	0.02	**-0.07**	0.02	**-0.08**	0.03	**-0.08**	0.03	-0.10	0.04	**-0.57**	0.16
surcharge at other ATM	-0.10	0.04	**-0.22**	0.04	**-0.17**	0.06	-0.20	0.11	-0.19	0.11	-0.20	0.12	**-1.99**	0.44
τ	-		**1.86**	0.17	**0.40**	0.17	-		0.21	0.24	-		**2.17**	0.20
γ									0.50	0.56			0.00	0.18
No. of parameters	17		18		21		51		53		35		37	
LL	-3354		-3217		-2768		-2735		-2734		-2868		-2820	
AIC	6742		6470		5579		**5572**		5574		5806		5714	
BIC	6846		6580		**5707**		5883		5898		6020		5940	
CAIC	6863		6598		**5728**		5934		5951		6055		5977	

Note: Bold estimates are statistically significant at the 1% level.

Table 15: Charge Card B (3 ASCs)

	MNL		Scale heterogeneity S-MNL		Random Effects S-MNL		Correlated errors 1-Factor MIXL		Correlated errors 1-Factor G-MNL		Uncorrelated errors Mixed logit MIXL		Uncorrelated errors G-MNL	
	est	s.e.	est	s.e.	est	s.e.	est	s.e.	est	s.e.	est	s.e.	est	s.e.
ASC for credit	**-0.97**	0.07	**-1.02**	0.05	**-0.83**	0.18	**-1.29**	0.24	**-1.29**	0.24	**-3.06**	0.29	**-2.72**	0.25
ASC for debit	**-1.29**	0.08	**-1.78**	0.07	**-1.47**	0.20	**-1.99**	0.27	**-1.99**	0.27	**-4.18**	0.37	**-4.54**	0.34
ASC for transaction	**-1.32**	0.08	**-1.72**	0.06	**-1.59**	0.21	**-2.12**	0.29	**-2.12**	0.29	**-4.30**	0.38	**-4.76**	0.36
annual fee	**-0.10**	0.01	**-0.13**	0.01	**-0.16**	0.01	**-0.22**	0.02	**-0.22**	0.02	**-0.28**	0.02	**-0.49**	0.05
trans fee	**-0.61**	0.07	**-0.71**	0.07	**-0.94**	0.10	**-1.32**	0.17	**-1.32**	0.17	**-1.72**	0.23	**-3.48**	0.45
overdraft facility	**0.30**	0.06	**0.54**	0.06	**0.42**	0.08	**0.48**	0.11	**0.48**	0.11	**0.98**	0.15	**1.77**	0.22
overdraft free days	**0.06**	0.02	**0.08**	0.01	**0.09**	0.02	**0.10**	0.03	**0.10**	0.03	**0.15**	0.04	0.18	0.07
interest charged	**-0.56**	0.06	**-0.96**	0.08	**-0.80**	0.08	**-0.90**	0.12	**-0.90**	0.13	**-1.65**	0.19	**-3.21**	0.34
interest earned	0.02	0.01	0.02	0.01	0.02	0.02	0.02	0.02	0.02	0.02	0.03	0.03	0.00	0.04
access_1	-0.01	0.02	**0.11**	0.02	0.00	0.02	-0.01	0.03	-0.01	0.03	-0.01	0.05	**0.19**	0.07
access_2	**-0.21**	0.05	**-0.22**	0.05	**-0.35**	0.07	**-0.44**	0.10	**-0.44**	0.10	**-0.58**	0.13	**-1.08**	0.22
access_3	**0.13**	0.05	**0.16**	0.04	**0.19**	0.06	**0.32**	0.09	**0.32**	0.09	0.28	0.11	**0.48**	0.17
cash advance interest	**-0.19**	0.05	**-0.27**	0.05	**-0.32**	0.06	**-0.45**	0.11	**-0.45**	0.11	**-0.50**	0.13	**-0.89**	0.20
loyal scheme	**0.24**	0.05	**0.50**	0.05	**0.37**	0.07	**0.46**	0.11	**0.46**	0.11	**0.44**	0.17	**1.56**	0.23
loyal fee	-0.02	0.01	**-0.03**	0.01	**-0.04**	0.01	-0.04	0.02	-0.04	0.02	-0.07	0.03	-0.07	0.04
loyal point	-0.03	0.04	-0.09	0.04	-0.06	0.06	-0.06	0.08	-0.06	0.08	-0.22	0.11	-0.41	0.16
merchant surcharge	**-0.06**	0.01	**-0.04**	0.01	**-0.08**	0.02	**-0.13**	0.03	**-0.13**	0.03	**-0.13**	0.03	**-0.20**	0.05
surcharge at other ATM	-0.07	0.03	-0.05	0.03	-0.11	0.04	**-0.19**	0.07	**-0.19**	0.07	-0.18	0.08	-0.17	0.11
τ	-		**1.18**	0.09	**0.38**	0.12	-		0.00	0.19	-		**1.52**	0.11
γ									0.99	171			0.01	0.25
No. of parameters	18		19		25		54		56		36		38	
LL	-4100		-3947		-3402		-3364		-3364		-3528		-3447	
AIC	8236		7932		6854		**6836**		6840		7128		6970	
BIC	8346		8048		**7007**		7166		7182		7348		7202	
CAIC	8364		8067		**7032**		7220		7238		7384		7240	

Note: Bold estimates are statistically significant different at the 1% level.

Table 16: Comparing Model Fit Across Data Sets

	Criteria	Scale heterogeneity		Random effects	Correlated errors		Uncorrelated errors	
		MNL	S-MNL	S-MNL	MIXL	G-MNL	MIXL	G-MNL
Tay Sachs Disease & Cystic Fibrosis test Jewish sample (3 ASCs)	AIC	7455	6469	5666	5154	**5118**	5550	5535
	BIC	7523	6543	5777	5626	**5601**	5684	5682
	CAIC	7534	6555	5795	5703	**5680**	5706	5706
Tay Sachs Disease & Cystic Fibrosis test General population (3 ASCs)	AIC	9320	7158	6487	6047	**5986**	6507	6446
	BIC	9390	7234	6601	6535	**6487**	6646	6598
	CAIC	9401	7246	6619	6612	**6566**	6668	6622
Mobile phone (1 ASC)	AIC	8980	8236	8014	8014	**7986**	8002	7996
	BIC	9074	8336	**8121**	8297	8281	8190	8197
	CAIC	9089	8352	**8138**	8342	8328	8220	8229
Pizza A (No ASC)	AIC	3330	3179		2847	**2741**	2838	2782
	BIC	3378	3233		3109	3015	2933	**2889**
	CAIC	3386	3242		3153	3061	2949	**2907**
Holiday A (No ASC)	AIC	6149	5952		5097	**5031**	5139	5074
	BIC	6201	6011		5386	5333	5244	**5192**
	CAIC	6209	6020		5430	5379	5260	**5210**
Papsmear test (1 ASC)	AIC	3069	2262	2143	1899	**1887**	1914	1897
	BIC	3104	2303	2189	2057	2056	1984	**1979**
	CAIC	3110	2310	2197	2084	2085	1996	**1993**
Pizza B (No ASC)	AIC	13525	13249		11810	**11436**	11849	11446
	BIC	13641	13372		12159	11799	12081	**11693**
	CAIC	13657	13389		12207	11849	12113	**11727**
Holiday B (No ASC)	AIC	26988	26088		23236	**22992**	23263	23019
	BIC	27116	26224		23619	23391	23519	**23291**
	CAIC	27132	26241		23667	23441	23551	**23325**
Charge card A (2 ASCs)	AIC	6742	6470	5579	**5572**	5574	5806	5714
	BIC	6846	6580	**5707**	5883	5898	6020	5940
	CAIC	6863	6598	**5728**	5934	5951	6055	5977
Charge card B (3 ASCs)	AIC	8236	7932	6854	**6836**	6840	7128	6970
	BIC	8346	8048	**7007**	7166	7182	7348	7202
	CAIC	8364	8067	**7032**	7220	7238	7384	7240

Table 17: Comparing the Importance of Heterogeneity Across Data Sets

	No. of choices	No. of attributes	No. of occasions	No. of people	MNL	S-MNL	MIXL	G-MNL	% Improvement MNL to S-MNL/ MNL to G-MNL	MNL to G-MNL
1 Tay Sachs Disease & Cystic Fibrosis test Jewish sample (3 ASCs)	4	11	16	210	-3717	-3223 [a] -2815 [b]	-2500	-2480	40% 73%	33%
2 Tay Sachs Disease & Cystic Fibrosis test General population sample (3 ASCs)	4	11	16	261	-4649	-3567 [a] -3226 [b]	-2946	-2914	62% 82%	37%
3 Mobile phone (1 ASC)	4	15	8	493	-4475	-4102 [a] -3990 [b]	-3962 [c]	-3949 [c]	71% 92%	12%
4 Pizza A (No ASC)	2	8	16	178	-1657	-1581	-1379	-1324	23%	20%
5 Holiday A (No ASC)	2	8	16	331	-3066	-2967	-2504	-2469	17%	19%
6 Papsmear test (1 ASC)	2	6	32	79	-1528	-1124 [a] -1063 [b]	-923	-914	66% 76%	40%
7 Pizza B (No ASC)	2	16	32	328	-6747	-6607	-5857 [c]	-5668 [c]	13%	16%
8 Holiday B (No ASC)	2	16	32	683	-13478	-13027	-11570 [c]	-11446 [c]	22%	15%
9 Charge card A (2 ASCs)	3	17	4	827	-3354	-3217 [a] -2768 [b]	-2735 [c]	-2734 [c]	22% 95%	18%
10 Charge card B (3 ASCs)	4	18	4	827	-4100	-3947 [a] -3402 [b]	-3364 [c]	-3364 [c]	21% 95%	18%

[a]   S-MNL with fixed ASCs
[b]   S-MNL with random ASCs
[c]   Imposing 1-factor model restriction on variance-covariance matrix

Table 18: Willingness to Pay Estimates vs. Aggregate Choice Probabilities

MIXL	% choosing A when A's attribute changes & charges $4 more	% people with WTP $4 or more	WTP distribution						
			10th	20th	25th	50th	75th	80th	90th
Traditional to Gourmet	39.43	23.17	-Inf	-2.15	-1.27	0.16	2.96	5.85	Inf
Canned to fresh ingredient	52.08	49.70	-3.19	-0.34	0.25	3.69	23.08	53.37	Inf
Warm to steaming hot	52.05	52.13	-1.87	0.33	0.79	4.22	26.08	74.75	Inf
No Veg. to Veg avail.	43.68	33.23	-6.04	-1.17	-0.46	1.33	9.55	21.41	Inf

G-MNL	% choosing A when A's attribute changes & charges $4 more	% people with WTP $4 or more	WTP distribution						
			10th	20th	25th	50th	75th	80th	90th
Traditional to Gourmet	38.98	20.12	-8.66	-1.36	-0.78	0.31	2.39	4.10	Inf
Canned to fresh ingredient	50.80	48.48	-1.38	0.25	0.64	3.80	29.50	96.80	Inf
Warm to steaming hot	53.25	61.59	0.55	1.41	1.85	6.23	39.57	1308.71	Inf
No Veg. to Veg avail.	43.50	30.79	-8.77	-1.24	-0.85	1.06	6.40	11.57	Inf