Understanding the City Size Wage Gap*

Nathaniel Baum-Snow, Brown University
Ronni Pavan, University of Rochester

March, 2009

Abstract

In 2000, wages of full time full year workers were over 30 percent higher in metropolitan areas of over 1.5 million people than rural areas. The monotonic relationship between wages and city size is robust to controls for age, schooling and labor market experience. In this paper, we decompose the city size wage gap into various components. We propose a labor market search model that incorporates endogenous migration between large, medium and small cities. This model is sufficiently rich to allow for recovery of the underlying ability distributions of workers by city size, arrival rates of job offers by ability and location, and experience profiles by ability and location, when structurally estimated using longitudinal data. Parameter estimates from our structural model indicate that for both college and high school graduates differences in wage level effects and returns to experience across location types are important mechanisms contributing to the wage premium for medium sized cities. Ability sorting across locations at the time of labor force entry and search frictions are important mechanisms generating the wage premium of large cities.

*The authors gratefully acknowledge financial support for this research from National Science Foundation Award SES - 0720763. Mike Kuklik and Cemal Arbatli provided excellent research assistance. We have benefited from comments in seminars at Purdue and Yale. We thank Emek Basker for generously providing us with ACCRA price index data.
1 Introduction

It is widely documented that wages are higher in larger cities. In the 2000 census, average hourly wages of white prime-age men working full-time and full-year were 32 percent higher in metropolitan areas of over 1.5 million people than in rural areas. The relationship between wages and population is monotonically increasing by about 1 percentage point for each additional 100 thousand in population over the full range of metropolitan area size. This monotonous relationship is robust to controls for age, schooling and labor market experience. In addition, it has become considerably steeper since 1980 when large metropolitan areas had wages that were 23 percent greater than rural areas.

In this paper, we investigate the causes of the city size wage gap. In particular, we propose a unified framework for empirically investigating the extent to which selection on latent ability, firm-worker matching, returns to experience and amenity differences can account for observed differences in wages between cities of different sizes. Our analysis utilizes a model of job search that incorporates endogenous migration between small, medium and large cities. This model is rich enough to allow for recovery of the underlying ability distributions of workers by location, arrival rates of job offers by ability and location, and returns to experience by ability and location, when structurally estimated using longitudinal data. Our estimates facilitate a more complete empirical decomposition of the city size wage gap than is possible using results in existing research. In particular, this paper presents new empirical evidence on the relative importance of various mechanisms by which workers in larger cities are more productive.

Table 1 summarizes patterns in city size wage premia using census data from 1980, 1990 and 2000. Table 1 presents results from regressing the log hourly wage for full time full year white men on indicators for living in metropolitan areas of 250 thousand to 1.5 million and more than 1.5 million. The excluded category includes small metropolitan areas and rural areas. Results in Panel A Specification 1 show that the city size wage premium is monotonic and has been increasing over time. Specification 2 shows that in each year one-quarter to one-third of the two estimated size premia can be explained with observables. Specification 3 shows that including additional controls for local average education levels reduces the gaps further to about one-half of those implied by unconditional means, suggesting that productivity premia can be partially explained through local spillovers.

Parameter estimates from our structural model indicate that for both college and high school graduates differences in wage level effects and returns to experience across location types are the most important mechanisms contributing to the wage premium for medium sized cities. Ability sorting across locations at the time of labor force entry and search frictions are the most important mechanisms for generating the wage premium of large cities for both samples. For college graduates, ability sorting additionally contributes to the medium sized city wage premium while wage level effects and returns to experience across location types contribute to the large city wage premium.

Roback's (1982) model forms a natural starting point for conceptualizing how wage
gaps can persist between cities. Its basic insight is that in order for there to be no
incentive for workers to migrate between cities, wages plus the value of amenities minus
cost of living must be equalized everywhere for individuals with identical endowments and
preferences. Thus, differences in wages adjusted for cost of living differences for equally
productive individuals across cities must solely represent amenity differences. Therefore,
to the extent that larger cities have more valuable consumer amenities, they should actually
exhibit lower wages than small cities for similar workers. Glaeser, Kolko & Saiz (2001)
dub this the "Consumer City" phenomenon. Lee (2006) provides evidence that similar
workers in the medical professions do indeed earn lower wages in larger cities.

A location equilibrium also requires that similar firms have the same profits wherever
they are located. Therefore, if nominal wages and rents are higher in cities, productivity
for firms producing traded goods must also be higher to compensate. Otherwise, firms
would move to smaller places in search of cheaper labor and rents. This logic reinforces
the intuition from the workers' decision that the city size wage gap implies higher worker
productivity in larger cities. Examination of wages that are not deflated for cost of living
differences thus directly reveals locations where workers are more productive.

Why are larger cities more productive? Two broad explanations exist. More pro-
ductive workers may be concentrated in larger cities and/or agglomeration economies may
make identical workers more productive in cities\(^1\). A considerable amount of empirical
evidence supports both explanations. In the 2000 census, 41 percent if prime-age white
males living in metropolitan areas of over 2.5 million people were college graduates relative
to just 20 percent of those living rural areas, with the fraction monotonically increasing
in city size. Glaeser & Maré (2001) argue that sorting on human capital levels accounts
for about one-third of the city-size wage gap in the United States. Combes, Duranton
& Gobillon (2006) demonstrate using French data that up to half of the wage disparity
across French cities can be accounted for by skill differences in their working populations,
as captured by individual fixed effects from panel data.

Several important studies provide evidence supporting the existence of agglomeration
economies in cities. Henderson, Kuncoro & Turner (1995) show that firms in several man-
facturing industries are more productive when they are located in the same metropolitan
area as other firms in the same industry. This phenomenon is known as "localization
economies". These authors also provide evidence for cross-industry agglomeration forces,
or "urbanization economies", for some new industries. Glaeser et al. (1992) also provide
empirical evidence on the existence of "Jacobs" urbanization economies. Ciccone and Hall
(1996) find a positive relationship between employment density and productivity at the
county level.

While there is fairly conclusive evidence that similar workers are more productive in
bigger cities, there is less empirical evidence on the relative importance of the different

\(^1\) In addition, Manning (2008) proposes monopsonistic labor markets in small cities as a mechanism that
could generate a city size wage premium.
mechanisms that may generate this productivity difference. Duranton & Puga (2004) review many of the existing micro-founded theories explaining aggregate agglomeration economies. They break up explanations into three broad categories: sharing, matching and learning. Glaeser & Maré (2001) show that wage growth is faster in larger cities and that high wages persist for migrants. From this they conclude that larger cities speed human capital accumulation, or that "learning" is important. Moretti (2004) supports this view, providing evidence that human capital spillovers exist from cities to industrial plants located within them. However, based on comparisons of within versus between job wage growth, Wheeler (2006) argues that better matching is the primary mechanism by which wage growth is faster in larger cities. Evidence in support of localized agglomeration economies within industries by Arzhagi and Henderson (2006) and Rosenthal & Strange (2003) for example, indicates that input sharing may also be important. Rosenthal & Strange (2004) exhaustively review the empirical literature on agglomeration economies.

One theme that recurs in much of the empirical work on agglomeration economies is that schooling and city size are complements. Why do highly educated people choose to live in cities? Shapiro (2005) demonstrates that employment growth is higher in better educated cities. He provides evidence that about 60 percent of this employment growth can be attributed to associated productivity enhancements while the remainder is because of improvements in the quality of life associated with skilled cities. Glaeser & Saiz (2003) argue that skilled cities’ success comes in part from their ability to better weather economic shocks. Carlino, Chatterjee & Hunt (2007) demonstrate that the patenting rate is increasing in city size, indicating that cities may make higher ability individuals more innovative. Finally, Costa & Kahn (2000) argue that job matching for "power couples" is a force pushing the more highly educated to larger cities.

While convincing evidence exists that larger cities are more productive, existing empirical work on the topic has several limitations. One difficulty is the potential endogenous sorting that exists across cities on unobserved skill. A common procedure for estimating productivity differences between cities essentially examines the relative wages of migrants in big and small cities. However, there is little reason to believe that migrants are representative of the population as a whole, even when conditioning on observables. An additional limitation exists on the types of mechanisms that can be examined independently. A lack of exogenous variation at many margins has made it difficult to differentiate between various explanations for agglomeration economies using standard regression procedures. This has led many studies to argue for the relative importance of one theory versus another based on descriptions of equilibrium outcomes rather than on evidence from natural experiments. Further, even if exogenous variation can be found, it generally only occurs on one margin at once, thereby making it difficult to understand potential interactions between different mechanisms.

In this paper, we attempt to fill some of these holes in the literature by specifying and estimating a dynamic model of job search that incorporates many of the elements listed above. The model laid out in Section 4 allows for endogenous migration, unemployment,
and job changing decisions. The model is parameterized such that skill differences may imply very different patterns of behavior as a function of underlying parameters and allows for econometric recovery of its deep parameters. The model is sufficiently flexible to allow for separate identification of amenity values, job arrival rates and returns to experience that vary as a function of interactions between underlying unobserved skill of individuals and city size.

Estimated parameters from the model allow for a decomposition of the observed city-size wage gap into four components that interact with each other: 1) sorting by ability across locations, 2) differences in arrival rates of job offers and job separation rates ("matching") across locations and abilities, 3) wage level effects ("sharing") across locations and abilities, and 4) different returns to experience ("learning") across locations and abilities. Longitudinal data from the work history file of the NLSY with restricted use geocodes allows us to evaluate the relative importance of these explanations for generating city size wage gaps in the United States.

Our results allow us to gain a better understanding of the importance that differences in matching, learning and their interaction with ability between city size categories have for generating productivity differences. These questions are particularly difficult to address with cross-sectional studies because of the inherently dynamic nature of the underlying data generating process. Even given panel data, special care has to be taken to account for the possibility that more able workers may be more likely to locate in larger cities and also may receive more job offers and have steeper experience profiles independent of city size. Structural estimation of a model incorporating both endogenous job search and migration along with a latent ability distribution handles these difficulties.

The methodological approach employed in this paper is similar to that used by Gould (2007) to examine the importance of ability sorting in generating the urban wage premium. Gould’s estimation of a search model with endogenous migration between urban and rural locations indicates that selective migration of high ability workers is an important force behind the urban productivity premium that gets amplified by steeper experience profiles in urban areas. This paper complements Gould’s analysis by incorporating an additional location type, job search, matching and amenities into a similar model. Further, we account for cost of living differences across locations in the data construction.

We should emphasize that the model specified in this paper is partial equilibrium in nature. That is, firm location is taken as given. Part of the city size productivity gap is likely to come from selection of more productive firms into larger cities. Ellison & Glaeser (1997) document that firms systematically locate in ways that generate industrial agglomerations. To the extent that some industries are more productive than others, this pattern implies that more productive firms may also systematically locate in larger cities. While the framework developed in this paper has little to say about the process that might generate such firm selection, it still allows us to learn much about why cities are more productive. If input costs are higher in cities, it would be difficult for a general equilibrium model to justify the selective location of productive firms to larger cities without their
workers also being more productive. Therefore, understanding why workers earn more in larger cities is still informative about why larger cities are more productive.

The next section describes some relevant patterns in the data. Section 3 discusses data construction. Section 4 presents the model. Section 5 discusses how we estimate the model. Section 6 presents model parameter estimates and counterfactual city size wage premia given a range of simulated scenarios. Finally, Section 7 concludes.

2 Empirical Observations

The city size wage premium shows up pervasively in the data. In this section, we present evidence on the existence of the city size wage gap using data from the National Longitudinal Surveys of Youth 1979 (NLSY). We then summarize patterns in wage growth, job transitions, unemployment and human capital as functions of experience and city size. While some of the patterns presented in this section resemble those already documented in the studies cited above, we additionally demonstrate that accounting for differences in cost of living, unemployment spells and job turnover across locations is important for gaining a more complete understanding of patterns in the data. These descriptive results are consistent with agglomeration economies, ability sorting and compensating differentials for amenities differences across cities all operating simultaneously.

Table 2 Panel A presents estimates of city size wage premia using data from the NLSY. Magnitudes of the city size wage premium estimated from the NLSY data are very similar to those from the 1990 and 2000 censuses with the wage premium for medium sized cities at 20 percent and that for largest cities at 30 percent, indicating that even though it only includes young adults in 1979, the NLSY is a reasonable data set with which to evaluate reasons for the city size wage premium. Controlling for education and quadratics in age and work experience reduces these coefficients to 0.15 and 0.23 respectively. Additionally controlling for individual fixed effects reduces the coefficients to 0.08 and 0.14. That the inclusion of individual fixed effects generates larger reductions in the city size wage gradient than individual controls indicates that positive sorting on unobservable skill may be an important component of the city size wage premium. However, the fixed effects results should be interpreted with caution given that the city size coefficients are identified off of movers who are unlikely to be a random sample of the population. Indeed, evidence presented below indicates that more educated individuals are more mobile. This is an example of why it is fruitful to appeal to a full structural model to evaluate the sources of the city size wage premium.

Table 2 Panel B presents analogous regression results when wages are adjusted for cost of living differences across metropolitan areas. Estimates in Panel B reflect the fact that cost of living in large metropolitan areas is much higher than in smaller places. All specifications in Panel B exhibit an inverse U shaped pattern. Real wages in medium sized

\footnote{The next section details how we implement this cost of living adjustment.}
metropolitan areas are the highest, even when controlling for observables and fixed effects. Commensurate with the discussion in the previous section, this evidence is consistent with medium sized cities having the lowest levels of consumer amenities such that individuals are willing to take a 5 percent wage cut to live in large metropolitan areas over medium sized metropolitan areas. While the estimated amenity value of large relative to medium sized cities is very stable across specifications, estimates of that for small cities are more heterogeneous. Controls for observables reduce the estimated relative amenity value of small places over medium sized cities from 15 to 10 percent of the wage while inclusion of individual fixed effects reduces it another 5 percentage points.

The results in Table 2 exhibit several features that should invite consideration in any analysis of the city size wage premium. First, adjustment for cost of living is crucial for understanding compensating wage differentials between the largest cities and other locations. Table 2 indicates that using panel data on workers to understand sources of the city size wage premium requires a model with endogenous migration between at least three size categories. Second, while controlling for observables reduces the city size wage premium, doing so does not eliminate it. Therefore, there is likely a significant amount to be learned about the sources of agglomeration economies.

Tables 3 to 6 examine outcomes as a function of labor market experience using the NLSY data. Table 3 examines wage growth over the first 1, 5, 10 and 15 years of labor market experience. To make the sample as consistent as possible across experience categories, we restrict it to include only those for whom we observe at least 15 years of labor market experience. This represents 80 percent of the NLSY sample described in more detail in the next section. (Only 48 percent of the sample survives to at least 20 years of labor market experience.) The left side of Table 3 shows wages only deflated by the CPI and the right side shows wages deflated over both time and space.

Table 3 Panel A shows that while wages of those entering the labor market are higher in larger cities, this gap increases as a function of experience. At labor force entry, the city size wage premia of medium and large MSAs are 12 and 13 percent respectively. By 15 years of experience, they grow to 34 and 43 percent respectively. The inverse U profile of wages adjusted for cost of living persists at all indicated levels of experienced except 10. This pattern is evidence that the relative amenity values of cities do not change much with experience. Table 3 Panel B shows wage growth rates by experience and city size. The largest cities saw wage growth of 72 percent on average relative to just 49 percent in the smallest areas. Glaeser & Maré (2001) find the same pattern and conclude that the city size wage gap is primarily generated from wage growth differences rather than higher initial wage levels in larger cities. Accounting for cost of living differences does not have much of an effect on wage growth profiles.

As discussed above, one potential explanation for the city size wage growth premium is systematic migration of higher human capital individuals to larger cities over the lifecycle while another is that faster turnover generates more efficient firm-worker matches in larger cities. Table 4 describes patterns in job turnover, unemployment and general human
capital accumulation as functions of experience and city size. The left side of Panel A shows that the mean number of jobs held is constant or decreasing in city size at every experience level. The right side of Panel A shows that the mean number of weeks of unemployment is also decreasing in city size. Panel B provides evidence that sorting on human capital levels may explain the patterns in Panels A and B. It shows the fraction who have ever graduated from college and mean years of schooling ever completed by city size. College graduation rates and years of schooling are increasing in city size at all levels of experience. Furthermore, both measures of the human capital gap widen with experience. This implies that skilled individuals are systematically migrating to larger cities over the course of their careers.3

Table 5 presents evidence of such selective migration. It presents transition matrices between city size categories for high school and college graduates. Panel A shows that under 20 percent of high school graduates move between city sizes during their first 15 years in the labor force. Those that do move out of medium and large cities are more likely to move to small cities and rural areas than medium sized cities. Those who move out of small places are more likely to move to medium sized cities than large cities. In contrast, Panel B shows college graduates are more mobile and exhibit migration patterns that are more oriented toward larger cities. 36 percent of college graduates entering the labor force in small places move compared to just 13 percent of high school graduates. Of the 24 percent who move out of medium sized cities, more than half migrate to large cities. Of the 26 percent who migrate out of large cities, about two-thirds move to medium sized cities. These differences in migration patterns as a function of education indicate the utility of estimating parameters of the structural model separately by education.

Table 6 presents a decomposition of the mean log wage growth numbers by city size for 15 years of experience reported in Table 3 Panel B into four components: within job, between jobs with no unemployment in between, between jobs when individuals experienced an unemployment spell in between and unknown. The unknown category consists of wage growth that occurred between jobs sandwiched by a third job for which we have no wage information. Reported values are means across all individuals in each city size-experience cell. Regardless of how wages are deflated, within job wage growth is increasing in city size whereas between job wage growth is a fairly flat inverse U in city size. The job to unemployment component of wage growth is small and negative in small and medium sized cities and 0 in large cities. Therefore, the bulk of the faster wage growth rates in larger cities comes from steeper tenure profiles.

Consistent with other studies, the descriptive evidence in Tables 5 and 6 points to systematic differences in human capital levels as one important driver of city size productivity differences. Indeed, weeks of unemployment and wage growth profiles match up well to human capital levels across city sizes at 15 years of experience. However, the profile of

3 Analogous results using contemporaneous education reveals that the human capital growth as a function of experience is more rapid in larger cities, indicating that post labor force entry educational attainment is more rapid in larger cities.
wage growth due to job to job transitions seen in Table 6 is a fact that has not been recognized before and invites further investigation. The compendium of evidence in Tables 5 and 6 does not indicate that thick labor market search externalities associated with larger cities is enough to generate city size wage gaps. However, it appears that attributes of larger cities that contribute to job specific human capital accumulation are important for generating higher wages in larger cities.

While the descriptive evidence presented here and in other studies points to explanations for the city size productivity premium that involve different wage experience profiles across cities of different sizes, the mechanism is still far from clear. Evidence presented above indicates that individuals in larger cities match into their primary job more quickly than in smaller cities, potentially allowing for more specific human capital to develop. Existing research does not address the extent to which productivity gaps of larger cities come through better matching or returns to experience, and how this interacts with observed and unobserved skills. Estimation of the model specified in Section 4 therefore facilitates an improved understanding of the mechanisms behind the city size productivity premium.

3 Data

3.1 NLSY Sample and Data Construction

The primary data set used for the analysis is the National Longitudinal Survey of Youth (NLSY) 1979 restricted use geocoded and work history files. With this data set, we construct information on jobs, unemployment, wages and migration patterns for a sample of young white men ages 14 to 21 on December 31st, 1978 from the time of their entry into the labor force until 2004 or their attrition from the survey. The sample includes 1,758 men from the NLSY79 random sample of 3,003 men. We lose 20 percent of the full sample because they entered the labor force before we observe their initial attachment. An additional 12 percent of individuals are dropped because they were in the military at some point, never entered the labor market, dropped out of the labor market for at least 4 contiguous years, or had significant missing job history data. The remaining individuals excluded from the sample are nonwhites.

We sample the weekly job history data four times every year for those who become attached to the labor force after January 1st, 1978. Sampled weeks always include the annual interview date (which varies) and the seventh week of the three remaining quarters. Our goal is to sample often enough such that we capture all job and location changes but not so often such that numerical maximization of the likelihood function implied by our structural model is computationally infeasible. Given the number of individuals in the NLSY, quarterly sampling maximizes the number of job and location transitions observed under the constraint that the likelihood function is computable in a reasonable period of time. Wages are only observed on interview dates and in the last observation on each job. In Section 5 we discuss how we handle missing wage data. We keep track of the number
of months in each unemployment spell that occurs in between sampled weeks.

We assign individuals to locations based on reported state and county of residence, which is available on interview dates and between interviews during the periods 1978-1982 and 2000-2004 only. We assign most location observations in remaining quarters by assuming that individuals must remain at one location for the duration of each job. We impose that unemployed individuals must remain at the same location as the last job held.\footnote{In the vast majority of cases, we do not observe the location at which individuals are unemployed. The model specified in the next section assumes that individuals cannot move to a new location to go unemployed.} Those jobs with multiple reported locations are assigned to the modally reported location. Jobs with multiple modes are assigned the modal location that occurred latest in time.\footnote{The model specified in the next section imposes that workers must remain at one location throughout each job.} This leaves 5 percent of quarterly observations with no location information. Sixty percent of these observations are for jobs sandwiched between two other jobs at the same location. In these cases, we assume that individuals did not move. For the remaining 2 percent of the sample, we impute locations to be that of the first job after the unobserved location spell for which we observe location.\footnote{We re-estimate the model using location of the previous job instead and results are very similar.}

For the purpose of assigning locations into size categories, we use metropolitan area definitions from county agglomerations specified in 1999 but assign them into size categories based on aggregated component county populations in 1980. We select the three size categories used throughout the paper such that the sample is split roughly into thirds.\footnote{There is a compelling argument to instead split the sample such that rural areas have their own category as in Gould (2007). We plan to re-estimate the model with this categorization as a robustness check.}

We think it is important to allow potential mechanisms behind the city size wage premium to differ by the skill set of workers. Indeed, the city size wage premium is increasing in education. As such, we estimate the model specified in the next section separately for those achieving high school graduation only and those with a college education or more. In the high school sample we have 50,665 observations on 675 individuals. In the college sample, we have 42,334 observations on 586 individuals. We observe a wage in about one-quarter of the observations.

3.2 Spatial Price Index

Using wages and migration patterns to understand productivity differences across cities requires accounting for cost of living differences across space and time. We denote the exogenously given price of good $i$ in time/location $j$ as $p_{ij}$. We assume that consumers have Cobb-Douglas utility over $I$ goods, meaning expenditure shares for each good are the same in each location. Our price index measures the relative expenditure required across time and locations to hold utility constant given observed price differences. The
expenditure function in every location $j$ must thus achieve the same level of utility $U_0$ as that achieved in an arbitrarily chosen base time period and location 0.

$$\sum_i \alpha_i \ln \left( \frac{\alpha_i E^j}{p^j_i} \right) = \ln(U_0) \quad (1)$$

Equating utility in time/locations $j$ and 0, we obtain the ideal index relating prices in time/location $j$ to those in 0, capturing the percent increase in expenditure required to keep an individual at the same utility.

$$INDEX_j = E^j / E^0 = \exp \sum_i \alpha_i \ln \left( \frac{p^j_i}{p^0_i} \right) = \prod_i \left( \frac{p^j_i}{p^0_i} \right)^{\alpha_i} \quad (2)$$

This is the index we use to deflate wages across locations and over time.

Building this index requires price data by time and location for different goods and information on expenditure shares. We get prices by location from the American Chamber of Commerce Research Association (ACCRA) data sets from 2000 to 2002.\(^8\) These data report prices in six broad expenditure categories for most metropolitan areas and some rural counties nationwide. When possible, we take data from 2001. For the few regions not sampled in 2001 we take data from either 2000 or 2002. ACCRA reports provide us with price data for 244 metropolitan areas and 179 rural counties.\(^9\) We impute price data for remaining areas as follows. Metropolitan counties are assigned the average prices from other MSAs in the same size category and state when possible. If there are no other MSAs of the same size in their state, we impute using data from MSAs of the same size by census division. Price data for rural counties are imputed analogously.

For time series variation in prices, we use regional and metropolitan price index data from the BLS disaggregated into the same six categories used for the ACCRA data. We assign each county to be represented by the most geographically specific index possible in each year. Together, the ACCRA and regional CPI data allow us to calculate the relative price in each expenditure category for time location/time period $j$ relative to the base location/time period. We define the base time/location as the average ACCRA location from 2001 but deflated to be index value 100 in 1999.\(^10\)

Rather than take expenditure shares $\alpha_i$ directly from the CPI-U, we build expenditure shares for households including white men working full time using data from the biannual Consumer Expenditure Surveys (CEX) starting in 1982. We build shares directly from the CEX in order to best capture preferences of those in our sample and because the weights

---

\(^8\)The ACCRA data set commenced being collected in the early 1980s. However, since its coverage and quality increased over time, we choose to use one high quality and complete more cross section rather than trying to use the data set as a panel.

\(^9\)ACCRA reports prices separately for different counties within some large metropolitan areas. In these cases, we allow our price index to differ accordingly within MSA. Otherwise, we assign the ACCRA reported prices to all counties in a given MSA.

\(^10\)We choose 1999 as the base year so that 2000 census data does not have to be temporally deflated.
used for the CPI-U sometimes fluctuate significantly from year to year. We find that the expenditure shares implied by the CEX differ slightly for different education groups and city sizes but these differences have a minimal impact on the resulting price index. As such, we prefer to use the sample from the CEX that best matches our full sample to calculate one set of expenditure weights that we apply to all individuals in our sample.

4 The Model

The model described in this section is specified to be simple enough to be tractably estimated yet sufficiently rich to capture all of the potential explanations for the city size wage and productivity gaps discussed in the introduction. We specify a "finite mixture" model, meaning that we have a finite number of latent agent types by which some parameters of interest are indexed. Our most constraining simplifying assumptions limit the number of these underlying worker types to two and city size categories to three.\(^\text{11}\) Though it would be possible to expand the number of both objects, our specification allows for simpler interpretation of estimated parameters and simulations of the estimated model. In addition, our specification facilitates computational tractability.

Individuals derive utility from the sum of a location and type specific amenity and their log wage or unemployment benefit. The different types of locations, characterized by different population size categories, are denoted with subscripts \(j \in \{1, 2, 3\}\) respectively. We denote "ability" levels as \(h_i\) where \(i \in \{h_L, h_H\}\). These are intended to capture underlying productivity differences between workers either from innate ability or because of different amounts of human capital accumulation prior to entrance into the labor market. We allow the probability that a given worker is of type \(i\) to depend on the location in which he enters the labor market.

The observed log wage depends on the worker’s ability, labor market experience in each location type, a firm-specific stochastic component and classical measurement error. The returns to experience and the individual specific intercepts are functions of worker type. The firm-specific stochastic component of the wage \(\varepsilon\) is drawn from a distribution of productivities from which workers sample when they receive a job offer. This distribution \(F_{\varepsilon_j}(\varepsilon)\) differs by location and is taken as exogenous. Finally, the unexplained component of the wage, which can be thought of as a measurement error term, is independent across individuals and time and is drawn from the distribution \(F_u(u)\). Put together, we parameterize the wage process of an individual working in location type \(j\) and having experience from location types indexed by \(k\) as follows:

\[
\ln w_j (h, x_1, x_2, x_3, \varepsilon) = \varepsilon + \beta_0^j (h) + \sum_{k=1}^3 \beta_1^j_k (h) x_k + \beta_2^j \left( \sum_{k=1}^3 x_k \right)^2 + u. \tag{3}
\]

\(^{11}\) Finite mixture models are widely used in the structural estimation literature. Heckman and Singer (1984) and Keane and Wolpin (1997) are two notable examples of studies using this approach.
The wage process expressed in Equation (3) captures the extent to which sorting on ability may influences wage growth and levels differently for small and large cities. The unit of time is a quarter. We denote experience at time \( t + 1 \) for an individual working at location \( j \) and time \( t \) by \( x'_j = x_j + 1 \), while experience in each other location type remains constant. Individuals accrue experience at the beginning of each working period. We assume that an individual works for 160 periods (40 years) and then retires with a pension equal to the last wage. After retiring he will live for an additional 80 periods (20 years).\(^{12}\)

We allow the job search technology to differ by city size, ability and employment status. We denote the arrival rates of job offers from the same location to be \( \lambda^u_j(h) \) for unemployed workers and \( \lambda_j(h) \) for employed workers, where \( j \) is the worker’s location. The arrival rates of job offers from different locations are \( \lambda^u_{jj'}(h) \) for unemployed workers and \( \lambda_{jj'}(h) \) for employed workers, where \( j' \) is the location of the job offer. We allow job arrival rates for the city of residence and other cities of the same size to differ. For analytical simplicity, we assume that individuals may only receive one job offer each period. Workers who choose to switch jobs at the same location must pay a stochastic switching cost \( v_S \) with zero mean and finite variance. This cost potentially captures differences in non-pecuniary benefits across jobs that might lead workers to accept wage cuts. Exogenous separation rates \( \delta_j(h) \) similarly depend on location and ability. With a job offer at location \( j' \), individuals have the option to move and pay a one-time cost of \( C_M + v_M \), where \( v_M \) is a random component with zero mean and finite variance. To keep the model simple and because we only observe the location of unemployment in at most 1 week per year, we assume that all unemployment occurs in the same location as the previous job.

We denote the value of being unemployed at location \( j \) as \( V_j^{UN} \) and the value of holding a job with match quality \( \varepsilon \) at location \( j \) as \( V_j^{WK}(\varepsilon) \). The state spaces of all value functions that we discuss contain individual specific “ability” \( h \) and experience in all location types \( x_1, x_2, x_3 \). For expositional simplicity we suppress this dependence in the notation. We assume that the current utility of an unemployed worker depends additively on the unemployment benefit and on an i.i.d. preference shock \( v_U \) with zero mean and and finite variance. This shock captures the random component of the disutility of work. Given these definitions, the deterministic component of the present value of being unemployed and the present value of working are given by the following expressions:

\[
V_j^{UN} = \frac{\alpha_j(h)}{3} + b + \beta^3 V_j^u,
\]

\[
V_j^{WK}(\varepsilon) = \alpha_j(h) + \ln w(\varepsilon) + \beta V_j(\varepsilon).
\]

Individuals receive their flow utility at the beginning of each period. At the end of each period, available options and the value of shocks for the following period are revealed.

\(^{12}\)In order to reduce the computational burden we assume that the unit of time is a quarter for the first 60 quarters while it is a year for the remaining 25 years of working life. The likelihood function is computed only using information on the first 15 years of labor force participation for each individual. More than 75% of observations and 90% of location changes in our data happen during this period.
and individuals make job transition and/or migration decisions. Because doing so does not significantly affect computation time, we take advantage of the high frequency of the job history data and index time in months for the unemployed. For this reason, the unemployed agent receives the amenity benefit of the employed worker and discounts utility by $\beta^3$, whereas the employed worker discounts by $\beta$ to represent quarters. The expressions above are of use for clarity of exposition and notational convenience. The key elements of interest are $V_j^u$ and $V_j$ which we specify next.

We first consider the environment for an unemployed individual at location $j$ with $X < 160$. At the beginning of each period, the agent observes whether he is faced with one of 5 possible scenarios. With probability $1 - \lambda_j^u(h) - \sum_{j' = 1}^{3} \lambda_{jj'}^u(h)$ he does not receive a job offer, with probability $\lambda_j^u(h)$ he receives a job offer from the same location, and with probability $\lambda_{jj'}^u(h)$ he receives an offer in location type $j'$. The individual decides at the beginning of each period whether to accept a potential job offer or remain unemployed in location 1. If he accepts an offer, he pays a cost to move to the relevant new location if necessary.

Equation (4) shows the value function for an unemployed agent in location $j$:

$$
V_j^u = \left(1 - \lambda_j^u(h) - \sum_{j' = 1}^{3} \lambda_{jj'}^u(h)\right) E_{vU}(V_j^{UN} + v_U) + \lambda_j^u(h) E_{vU\varepsilon_j} \max \left[V_j^{UN} + v_U, V_j^{WK}(\varepsilon)\right] + \sum_{j' = 1}^{3} \lambda_{jj'}^u(h) E_{vUv_M\varepsilon_j} \max \left[V_j^{UN} + v_U, V_{j'}^{WK}(\varepsilon) - [C_M + v_M]\right].
$$

The first term of Equation (4) represents the case in which the individual receives no job offers. In this case, he has no choice and must remain unemployed for an additional period, receiving utility from the amenity in his location, the unemployment benefit and a utility shock. The second term gives the case in which the individual receives a job offer in his city of residence. Under this scenario, he may choose to accept the job immediately or remain unemployed. The third term states that the unemployed agent will accept a potential job offer in another city of type $j'$ if the job’s option value $V_{j'}^{WK}(\varepsilon)$ net of the moving cost exceeds that of remaining unemployed. The option value of having a job offer in location $j'$ is the discounted value of holding the job next period plus the current utility implied by the wage offer. The expectation is taken with respect the distribution of $\varepsilon$ in location type $j'$ and the distribution of the random components $v_U$ and $v_M$ (expressed as $E_{vUv_M\varepsilon_j}$).

The parameter $\lambda_{jj'}^u(h)$ represents the probability that an unemployed individual at location $j$ receives a wage offer in a different city also of size category $j$ whereas the parameter $\lambda_j^u(h)$ represents the probability that this individual receives a wage offer in the same city as his last job.
The value function for a worker at location \( j \) resembles that for an unemployed individual except that it also includes potential exogenous job separations and job switching costs. A worker in location \( j \) faces six potential scenarios: being exogenously separated and going unemployed, not receiving a wage offer, receiving an offer in any of the 3 types of locations and receiving a wage offer in the same city. To simplify the computational intensity of the model and because this assumption has little impact on the results, we assume that a worker decides whether to go unemployed before knowing whether he will receive a wage offer from a different employer. As such, the value to a worker with ability \( h \) at location \( j \) of being employed with firm match \( \varepsilon \) is given by Equation (5):

\[
V_j(\varepsilon) = \delta_j(h) V_j^{UN} + (1 - \delta_j(h)) E_{wu} \max \{ V_j^{UN} + v_U, \\
(1 - \lambda_j(h) - \sum_{j=1}^{3} \lambda_{jj'}(h))V_j^{WK}(\varepsilon) \\
+ \lambda_j(h) E_{vS} \max \{ V_j^{WK}(\varepsilon), V_j^{WK}(\varepsilon') - v_S \} \\
+ \sum_{j'=1}^{3} \lambda_{jj'}(h) E_{vSwM} \max \{ V_j^{WK}(\varepsilon), V_j^{WK}(\varepsilon') - v_S - [C_M + v_M] \} \}.
\]

As is evident in Equation (5), an exogenously separated worker at location \( j \) may only become unemployed in location \( j \). If the worker is not exogenously separated, he can still choose to go unemployed if \( v_U \) is large enough. If he chooses to keep working, with probability \( 1 - \lambda_j(h) - \sum_{j'} \lambda_{jj'}(h) \) he does not receive a wage offer. In this event, he remains employed in the same job. If he receives an offer, he either accepts it and moves if necessary, or remains at his old job.

To conceptualize how the model works, it is convenient to define a set of reservation functions \( \{ \varepsilon_A^j, \varepsilon_B^j, \varepsilon_C^j, \varepsilon_D^j, \varepsilon_E^j \} \) that can be thought of as hypothetical firm-worker matches at which agents would be indifferent between two choices conditional on the regime in which a certain choice set is available. We define these functions such that if a new draw for a firm-worker match is \( \varepsilon' > \varepsilon_R \), then the agent optimally chooses to accept a job offer if available or remain employed if unemployment is the only other option. Regime A occurs when an unemployed agent receives an own-location job offer. Regime B occurs when a worker is choosing whether to go unemployed. Regime C occurs when an unemployed agent receives an offer in another location. Regime D occurs when a worker receives an own-location offer. Regime E occurs when a worker receives an offer in another location. For simplicity, we suppress dependence of the reservation functions on type \( h \) and work experience in each location \( \{ x_1, x_2, x_3 \} \). The definitions of these reservation rules are given
as follow where $\bar{\epsilon}$ is the match quality of the incumbent job:

$\epsilon_j^A (v_U)$ solves: $V_j^{UN} + v_U = V_0^{WK} (\epsilon),$

$\epsilon_j^B (v_U)$ solves: $V_j^{UN} + v_U = (1 - \lambda_j (h) - \sum_{j=1}^{3} \lambda_{jj'} (h)) V_j^{WK} (\epsilon) +$

$+ \lambda_j (h) E_{v_S \epsilon_j} \max [V_j^{WK} (\epsilon), V_j^{WK} (\epsilon') - v_S] +$

$+ \sum_{j'=1}^{3} \lambda_{jj'} (h) E_{v_M \epsilon_j} \max [V_j^{WK} (\epsilon), V_j^{WK} (\epsilon') - v_S - [C_M + v_M]]$

$\epsilon_{jj'}^C (v_U, v_M)$ solves: $V_j^{UN} + v_U = V_{jj'}^{WK} (\epsilon) - C_M - v_M,$

$\epsilon_j^D (\bar{\epsilon}, v_S)$ solves: $V_j^{WK} (\bar{\epsilon}) = V_j^{WK} (\epsilon) - v_3,$

$\epsilon_{jj'}^E (\bar{\epsilon}, v_S, v_M)$ solves: $V_{jj'}^{WK} (\bar{\epsilon}) = V_{jj'}^{WK} (\epsilon) - C_M - v_M - v_S.$

The reservation rules are specified to take account of the fact that every example of migration must result in accepting a new job offer. The shocks $v_U, v_M$ and $v_S$ are meant to capture the effects of non-pecuniary factors that may affect worker behavior.

This model captures each of the components of wage growth discussed in the introduction. The location specific component of utility $\alpha_j (h)$ captures the difference in amenity values and regulates ability sorting across locations. The job arrival rate parameters $\lambda_{jj'} (h)$ and $\lambda_u (h)$ capture the potential importance of matching. The coefficients on experience in Equation (3) capture differences in "learning". The intercepts in the wage process capture fixed differences across locations like input sharing and technological spillovers.

5 Estimation

This section outlines how we estimate the parameters of the model detailed in the previous section using maximum likelihood. We then intuitively explain how parameters of the model are identified.

5.1 The Likelihood Function

The general form for the contribution to the likelihood of an individual that enters in the market in location $j$ and is observed for $T$ periods is given by:

$L (\theta) = \pi_j f (Y^T | h_L; \theta) + (1 - \pi_j) f (Y^T | h_H; \theta)$

where $\pi_j$ is the probability that an individual is of type $h_L$ given that he enters in location $j$ and $\theta$ is the vector of parameters.\footnote{The individual index is suppressed for notational simplicity.}
Define $Y_t$ the vector of labor market outcomes of time $t$ which consist of a wage, if any, the location of the worker and the type of labor market transition that the worker has experienced since the previous period. We can then define $Y^T = \{Y_1, \ldots, Y_t\}$ as the vector of all labor market observations in an individual’s job history up to and including period $t$. We decompose $f(Y^T|h; \theta)$ as follows:

$$
f(Y^T|h; \theta) = f(Y_1|h; \theta) \prod_{t=2}^{T} f(Y_t|Y^{t-1}, h; \theta).$$

In the previous section we saw how the job switching and migration behavior of individuals depends on the set of four classes of reservation rules. It is more convenient to express the likelihood function in terms of probabilities that one of five types of event occurs. The five events are: finding a job in the same location if unemployed, finding a job in a different location if unemployed, having a job to job transition within the same location, having a job to job transition changing location, and entering unemployment. These probabilities are defined as functions of $\varepsilon$ and, if relevant, $\varepsilon'$ but they also depend on the other state variables $\{h, x_1, x_2, x_3\}$:

$$\left\{ P_{ue}^j(\varepsilon), P_{ue}^j(\varepsilon, \varepsilon'), P_{ee}^j(\varepsilon, \varepsilon'), P_{ue}^{jj'}(\varepsilon), P_{ee}^{jj'}(\varepsilon, \varepsilon') \right\}_{j, j'=1}^3.$$

These functions capture the probabilities of each transition and that the new match quality $\varepsilon$ is drawn, and facilitate derivation of the likelihood function. For example, the transition probability between unemployment and employment at location $j$ with firm specific component $\varepsilon$ is as follows.

$$P_{ue}^j(\varepsilon) = \lambda_j^u(h) f_{\varepsilon j}(\varepsilon) \int \mathbf{1}(\varepsilon > \varepsilon_{\lambda}^{A}(v_U)) \, dF(v_U)$$

The offer $\varepsilon$ at location $j$ is received by an unemployed worker with probability $\lambda_j^u(h) f_{\varepsilon j}(\varepsilon)$ and is accepted only if it exceeds the reservation wage $\varepsilon_{\lambda}^{A}$. Appendix A specifies the remaining probabilities and specifies in more detail how we build the functions $f(Y^T|h; \theta)$ and $f(Y^T|Y^{T-1}, h; \theta)$ using available information in the data. There are two important considerations here. First, wages are not always observed when they should be. We assume that missing wage observations happen with an exogenous probability and we condition that probability out of the likelihood function since it is not of interest. Secondly, we have to deal with the fact that the firm-worker match $\varepsilon$ is unobserved. Appendix A shows how we use Bayesian updating methods to handle this difficulty.

5.2 Identification

The model we specify in the previous section is in the class generally known as finite mixture models. This class of models features a finite number of latent agent types in the
economy and a subset of parameters that are indexed by type. By following individuals over time, these type-specific parameters are identified, subject to standard constraints on identification. The distribution of types is nonparametrically identified. Kasahara (forthcoming) discusses identification of parameters in this class of models.

We cannot nonparametrically identify distributions of the firm specific wage components \( \varepsilon_j \). This is a standard limitation of structural estimation of search models that occurs because the set of wage offers generated by the left tails of the \( \varepsilon_j \) distributions are not accepted and therefore are not observed. As such, we are required to make assumptions about the forms of the \( F_{\varepsilon_j}(\varepsilon) \) distributions. We assume that these firm-specific components are distributed \( N(0, \sigma_{\varepsilon_j}) \).

Migration plays a crucial role for the identification of many parameters of the model. If no migration were observed, there would be no way to distinguish between the differences in the composition of the population across locations and the inherent differences that exist between location types. When we observe an individual that moves across location types, the different labor market histories within each location type are informative about differences across locations in parameters indexed by location. Parameters indexed by type are identified from the full labor market histories of individuals regardless of their location. Parameters indexed by both type and location are identified from the relative labor market experiences across locations of workers of a given type. Identification of these type and location specific parameters does not require that migration is exogenous, but only that workers’ types are constant over time. In fact, we leverage the life cycle nature of the model to strengthen separate identification of these different parameters.

Table 9 describes all of the estimated parameters of the model. We partition them into six broad groups: components of the wage in Equation (3), amenities, arrival and separation rates, costs and benefits, type probabilities, and distributional measures. We choose to normalize amenities to 0 in location type 0 as they would not otherwise be separately identified from the wage shifters and returns to experience in location type 0.\(^{15}\)

The one parameter of the model that we do not estimate is the discount factor \( \beta \). This is standard practice in the structural estimation of search models. Based on estimates from the literature, we set the discount factor to 0.95 per year.

6 Results

6.1 Model Fit

Figure 1 shows graphs of spatially deflated average log hourly wages (in cents) from the data and those predicted by the model as functions of experience for college graduates for each city size category. Figure 1 Panel A shows that the model fits the data well for small

\(^{15}\)As seen in the list of parameters in Block C of Table 9, we make some assumptions that limit the number of parameters needed to capture heterogeneity in arrival rates of job offers from one location type to another. Details on our procedure for doing this are in Appendix B.
locations while Panel B shows that we have a good fit in medium sized cities up to 13 years of experience. Panel C shows that for large cities the model slightly over-predicts actual wages at low levels of experience and more severely under-predicts wages at high levels of experience. Figure 2 shows that the fit for the high school sample is slightly less good than that for the college sample. In particular, the model over-predicts wages beyond 12 years of experience in small metropolitan areas and over much of the range beyond 5 years of experience in large metropolitan areas.

One explanation for the pattern of gaps in actual versus predicted wages as a function of experience is that returns to experience may be more concave in large locations than in small locations and we do not allow the concavity parameter $\beta_2$ to differ by location type. We plan to correct this weakness in future versions of the paper by adding a total of six linear and quadratic experience effects indexed by current residential location to our specification of the wage process.

Tables 7 and 8 provide further evidence that the model fits the data well. Table 7 shows actual and predicted job, unemployment and location transitions. The model generates simulated data that is at most 0.5 percentage points off from the model for the college sample while the fraction of observations that are location changes is predicted almost perfectly. Commensurate with evidence if Figure 2, Table 7 shows that the high school sample generates a fit that is slightly less good than does the college sample with a gap of 1.6 percentage points between predicted and actual fraction of observations that are job changes. However, the high school sample also generates predicted fraction of observations with location moves within 0.01 percentage points of the actual.

Table 8 presents predicted and actual mobility conditional on moving location. At left are location types in period $t-1$ while along the top are location types at time $t$. Diagonal entries give the fraction of moves between different cities of the same location type. The largest gaps between actual and predicted for each sample are 2.4 percentage points for migration between different large cities in the college sample and 2.8 percentage points for migration from medium cities to small cities from the high school sample.

### 6.2 Parameter Estimates

While we present counterfactual simulation results in the following subsection, many of the lessons from these exercises can be seen qualitatively through examination of parameter estimates. Table 9 presents parameter estimates of the structural model for both samples. As discussed in the identification subsection, we have broken the parameter set into six categories.

Category A includes location and ability specific wage level and growth estimates. As expected, high ability types have greater estimated wage intercepts and returns to experience than low ability types in all cases. Constants of the wage process are similar in small and large locations for all high school graduates and low ability college graduates and about 8 to 15 percent higher in medium sized locations. However, this intercept component
of wages is monotonically increasing in city size for high ability college graduates. Once cost of living adjustments are removed from wages using average prices by city size category, intercepts are monotonically increasing in city size for all four groups, indicating that level effects are an important component of the city size productivity premium. Among college graduates, level effects for marginal products of labor are 19 percent higher in the largest cities than small places for low ability types and 27 percent greater for high ability types.\footnote{Because the model has no predictions about the exact city of each size to which migrating individuals move, it is impossible for us to exactly undeflate wages back to marginal productivities. Given the equilibrium location of college graduates observed in the data, prices are 8 percent higher in medium sized cities and 18 percent higher in large cities compared to small cities and rural areas. Because within size category they live in smaller cities, these price premia are 2 percent and 17 percent respectively for high school graduates.}

Returns to experience are monotonically increasing in city size for low ability types and exhibit an inverse U shape for high ability types of both education levels. Low ability college graduates have the largest variation in returns to experience with about a 1 percentage point premium for movement to larger size categories. This large differences in returns to experience indicates that differences in human capital accumulation by location may be an important driver of the city size productivity premium. Because, as seen in Table 3, price differences across cities primarily influence wage levels rather than growth rates, we view these differences in returns to experience as primarily representing true differences in the slopes of worker marginal products by city size.

Block B of Table 7 reports estimated amenity parameters. Since amenities for small locations are not separately identified, all estimates are relative to the amenity value of small cities. Results indicate that for the college sample, the highest amenity locations are the small cities and rural areas for low ability types and medium sized cities for high ability types. For the high school sample, both ability groups prefer to live in the smallest location category.

Table 7 Block C reports estimated job arrival and separation rates by location and worker type. Interestingly, among college graduates estimated arrival and separation rates for low ability workers are higher than for high ability workers whereas this ordering is if anything reversed for high school graduates. The groups with higher arrival and separation rates switch jobs more often, perhaps because individuals therein are more likely to work in sectors for which the idiosyncratic match is a smaller component of worker productivity. Job offer arrival rates for workers are generally very flat as a function of city size. Arrival rates for the unemployed are if anything increasing in city size for all groups except low ability high school graduates. Arrival rates of offers from different locations are flat or declining in the size of the receiving location and migrating workers are almost twice as likely to move within city size category than across categories. Exogenous job separation rates are up to 5 times larger for low ability types than high ability types in the college sample, though they are similar across types in the high school sample. Separation rates are fairly flat as a function of city size and low for college graduates whereas they are
roughly decreasing in city size for high school graduates. Overall, these results show that low ability college graduates and high ability high school graduates cycle through different jobs at higher rates than the other groups. These results indicate the importance of accounting for variation in the ability distribution across locations so as not to attribute differences in search frictions across locations to location-specific effects.

Block D reveals that the benefit required to convince individuals to go unemployed is higher for high school graduates than for college graduates. This result makes sense given the greater returns to experience, and associated higher opportunity cost of unemployment, borne by college graduates. Additionally, high school graduates are estimated to have higher implied moving costs than college graduates. This result may reflect their higher psychic costs of setting up in a new city.

Results in Block E demonstrate that there is selection on unobserved worker ability from the point of entry into the labor market. Indeed, for both education groups low ability types are most likely to enter in small locations while high ability types are more likely to enter in medium or large locations. Given the differences in relative amenity values across groups, the sorting equilibrium is likely to evolve over workers’ life cycles so as only to exacerbate this pattern of sorting, especially for college graduates.

Results in Block F show estimated standard deviations of all of the distributions in the structural model. The two that stand out are the standard deviation of the moving and job switching shocks. Apparently there are many idiosyncratic reasons why individuals change jobs and locations that are not captured by the model.

6.3 Simulations

Using the parameter estimates from the structural model, Table 10 evaluates the importance of potential mechanisms for generating the city size wage premium in the college sample. As a baseline, row 1 in Panel A shows that the raw data imply city size wage premia of 0.15 for medium sized cities and 0.09 for large cities. Data simulated from the parameter estimates in Table 9 also imply wage premia of 0.15 and 0.09 for the two size categories respectively, indicating a very good fit. Panel A row 3 gives counterfactual city size wage premia in the case where individuals are forced to stay in their location of labor market entry. Restricting mobility actually increases wage premia between rural areas and cities to about 0.17, as it forces individuals to stay in larger cities, where wage levels are greater for high types and returns to experience are greater for low types, than they would choose to locate on their own. Results in Row 2 are used as a benchmark for counterfactuals in Panel B for which we sequentially shut off potential channels other than mobility for the city size wage premia. Results in Row 3 benchmark results in Panel C for which we shut off the same potential channels in addition to mobility.

\[^{17}\text{For the purpose of generating counterfactuals, we choose not to undo the adjustment to wages for cost of living differences. The reason is that the model has no prediction about in which metropolitan areas individuals live within size categories.}\]
For the simulations, we assign the average value of the parameters in each listed group for each type across locations. The final two columns in Table 10 show the resulting reductions in the premia relative to the benchmark. Results from the set of experiments in Panel B are comparable to evidence in the reduced form literature using cross-sectional or repeated cross-section data.

The channels that independently generate the greatest portions of the city size wage premium given endogenous mobility are differences in wage levels and returns to experience by location. Absent differences in wage process intercepts across locations and maintaining endogenous sorting across locations, the counterfactual city size wage premia for medium cities would be about one-third as big, with no effect on the premium for large cities. This may reflect the importance of input sharing or human capital spillovers. Equalizing returns to experience reduces the city size wage premium by about one-fifth both in medium and large cities. Interestingly, eliminating labor market frictions generates marked increases in wage premia for medium and large cities while equalizing the ability distribution across locations at labor force entry causes in increase in the premium for large cities.

Because our model cannot take into account potential general equilibrium responses to the endogenous changes in the sorting equilibrium that occur in response to equalization of parameters across city size categories, it may be more natural to examine counterfactuals holding the sorting equilibrium fixed. While imposing the distribution of types across locations to be the same at all levels of experience also generates general equilibrium effects, they are the same general equilibrium effects given each counterfactual experiment, meaning that the results in Panel C may be somewhat more comparable to each other. In terms of the reduced form literature, the results in Panel C are more comparable to estimates derived using individual level panel data.

Counterfactuals without mobility generate larger location-specific wage level effects for every channel than those in Panel B. Endogenous mobility neutralizes forces that push up the city size wage premium. For medium sized cities, equalization of wage process intercepts, the initial ability distribution, returns to experience, match distributions and search frictions respectively generate the largest to smallest reductions in the wage premium. For large cities, each channel generates larger effects with the same ordering.

Table 11 reports analogous results as those in Table 10 but for high school graduates. Since the high school sample is less mobile than the college sample, as seen in its higher estimated moving cost in Table 9, the results in Table 11 Panels B and C are more similar than in Table 10. Wage level effects are by far the most important components of the city size wage premium in medium sized cities, followed by returns to experience and search frictions. For large cities, search frictions and ability sorting are most important.
7 Conclusions

In this paper, we lay out a systematic framework to empirically examine reasons for which larger cities have higher wages and are more productive. Using data from the census and the NLSY, we show that hourly wages are higher in bigger cities, and this is associated with higher levels of human capital and lower levels of unemployment. A decomposition of log wage growth over the first 15 years of experience reveals that within job wage growth generates more of the city size wage gap than between job wage growth. While interesting, these observations are not sufficient to causally determine the mechanism by which cities are more productive. In particular, estimation of the model specified in this paper allows us to sort out the extent to which sorting across locations on ability interacts with sharing, learning and matching to generate city size wage and productivity gaps.

Parameter estimates indicate that for both college and high school graduates differences in wage level effects and returns to experience across location types are the most important mechanisms contributing to the wage premium for medium sized cities. Ability sorting across locations at the time of labor force entry and search frictions are the most important mechanisms for generating the wage premium of large cities for both samples. For college graduates, ability sorting additionally contributes to the medium sized city wage premium while wage level effects and returns to experience across location types contribute to the large city wage premium.
A Construction of the Likelihood Function

In this appendix, we present expressions for the contribution of each potential type of event in an individual’s job history to the likelihood function. Though we suppress this dependence in the notation, the objects $f(\cdot), A(\cdot), B(\cdot)$ and $P(\cdot)$ derived below are functions of type $h$ and location-specific work experience $\{x_1, x_2, x_3\}$.

A.1 Fundamentals

Computation of $f(Y_t|Y^{t-1})$ is complicated by the fact that we do not observe the firm match $\varepsilon$. While it is not observed directly, we can treat it as a latent variable in a non-gaussian state space model. That is, we can recover the conditional density of $\varepsilon$ and then integrate the likelihood function with respect to $\varepsilon$ given that we know the likelihood contribution for each value of $\varepsilon$. Assuming that we know the unconditional distribution of the firm match, we use Bayes’ rule to update the conditional distribution of $\varepsilon$ with updated wage information each period. This implies the following updating rule:

$$f(\varepsilon|Y^t) = \frac{f(Y_t|Y^{t-1}, \varepsilon) f(\varepsilon|Y^{t-1})}{f(Y_t|Y^{t-1})} \quad (6)$$

This expression is used extensively as we build components of the likelihood function below.

Additionally, wages are not always observed when they should be. To deal with this, we define the functions $B_{jt}(\cdot)$ and $A_{jt-1}(\cdot)$. $B_{jt}(\cdot)$ gives the distribution of wage information for the final observations covered by each interview while the function $A_{jt-1}(\cdot)$ gives that for job changes that are reported within an interview cycle. As mentioned in the data section, wages are observed once a year for up to 5 different jobs. Therefore if a worker does not change employer, we have only one wage observation a year for that worker, while if a worker changes employer within a cycle, we may have more than one wage observation. Because the wage is recorded in $t-1$ only because the worker has changed job in the previous period, this information must be included in the contribution to the likelihood function of period $t$ using the function $A_{jt-1}(\cdot)$. These functions include the parameter $p_n$, the probability of observing a wage.

$$B_{jt}(\varepsilon) = \left[ p_n F_u(u_t) 1(w_t \text{obs}) [1 - p_n] 1(w_t \text{not obs}) \right] 1(\text{int}_t \neq \text{int}_{t+1})$$

$$A_{jt-1}(\varepsilon) = \left[ p_n F_u(u_{t-1}) 1(\text{int}_{t-1} \text{obs}) [1 - p_n] 1(\text{int}_{t-1} \text{not obs}) \right] 1(\text{int}_{t-1} = \text{int}_t \land \text{job}_{t-1} \neq \text{job}_t)$$

Because we have no interest in the value of $p_n$ and we take it as exogenous, we can simplify the expressions above by conditioning the likelihood on observing the wages. Therefore, we define these functions to be

$$B_{jt}(\varepsilon) = F_u(u_t) 1(w_t \text{obs} \land \text{int}_t \neq \text{int}_{t+1})$$

$$A_{jt-1}(\varepsilon) = F_u(u_{t-1}) 1(w_{t-1} \text{obs} \land \text{int}_{t-1} = \text{int}_t \land \text{job}_{t-1} \neq \text{job}_t)$$
instead.

A.2 Transition Probabilities

In cases where a new match is drawn and the worker has an existing match quality, \( \varepsilon' \) denotes the new match and \( \varepsilon \) denotes the firm-specific component of the existing job. If the worker is unemployed, \( \varepsilon \) denotes the new match draw. The probability of exiting unemployment and finding a job with match \( \varepsilon \) in the same location \( j \) is given by:

\[
P_{jue} (\varepsilon) = \lambda_j^u (h) f_{\varepsilon_j} (\varepsilon) \int 1 (\varepsilon > \varepsilon_j^A (v_U)) \ dF(v_U).
\]

The probability of exiting unemployment and finding a job with match \( \varepsilon \) in a different location \( j' \) is:

\[
P_{jue} (\varepsilon) = \lambda_{j,j'}^u (h) f_{\varepsilon_{j'}} (\varepsilon) \int \int 1 (\varepsilon > \varepsilon_{j,j'}^C (v_U, v_M)) \ dF(v_U) dF(v_M)
\]

The probability of entering unemployment given that a worker had a job with match \( \varepsilon \) is:

\[
P_{jeu} (\varepsilon) = \delta_j (h) + (1 - \delta_j (h)) \int 1 (\varepsilon < \varepsilon_j^B (v_U)) \ dF(v_U)
\]

The probability of changing employer from match \( \varepsilon \) to match \( \varepsilon' \) in the same location is:

\[
P_{j\varepsilon} (\varepsilon, \varepsilon') = \left[ 1 - P_{jue} (\varepsilon) \right] \times \lambda_j (h) f_{\varepsilon_j} (\varepsilon') \\
\quad \times \int \int 1 (\varepsilon' > \varepsilon_j^D (\varepsilon, v_S)) \ dF(v_S) dF_{\varepsilon_j} (\varepsilon')
\]

Finally, the probability of changing employer from match \( \varepsilon \) in location \( j \) to match \( \varepsilon' \) in location \( j' \) is:

\[
P_{j\varepsilon} (\varepsilon, \varepsilon') = \left[ 1 - P_{jue} (\varepsilon) \right] \times \lambda_{jj'} (h) f_{\varepsilon_{j'}} (\varepsilon') \\
\quad \times \int \int \int 1 (\varepsilon' > \varepsilon_{jj'}^E (\varepsilon, v_S, v_M)) \ dF(v_S) dF(v_M) dF_{\varepsilon_{j'}} (\varepsilon')
\]

A.3 First Period

Because we condition on working in the first period, the contribution to the likelihood of an individual entering in location \( j \) is:

\[
L^j_1 = \frac{\int B_{j1} (\varepsilon) P_{jue} (\varepsilon) \ d\varepsilon}{\int P_{jue} (\varepsilon) \ d\varepsilon}
\]

25
The resulting posterior distribution of the firm match is:

\[ f(\varepsilon|Y^1) = \frac{B_{j1}(\varepsilon) P_{ue}^j(\varepsilon)}{\int B_{j1}(\varepsilon) P_{ue}^j(\varepsilon) d\varepsilon} \]

### A.4 Unemployment

An individual of ability \( h \) enters unemployment in location \( j \) and has an unemployment spell that lasts \( NW_t \) weeks. The probability of not accepting a job for \( NW_t - 1 \) weeks is given by

\[
\Pi_{2}^j(NW_t) = \left(1 - \int P_{ue}^j(\varepsilon) d\varepsilon - \sum_{j=1}^{3} \int P_{ue}^{jj'}(\varepsilon) d\varepsilon \right)^{NW_t-1}
\]

After \( NW_t \) weeks, the worker finds a job in location \( j \) or in location \( j' \). If he finds a job in location \( j \), the total contribution of this unemployment spell to the likelihood function is:

\[
L_{2a}^j = \Pi_{2}^j(NW_t) \int B_{jt}(\varepsilon) P_{ue}^j(\varepsilon) d\varepsilon
\]

The posterior distribution of the match then becomes:

\[ f(\varepsilon|Y^t) = \frac{B_{jt}(\varepsilon) P_{ue}^j(\varepsilon)}{\int B_{jt}(\varepsilon) P_{ue}^j(\varepsilon) d\varepsilon} \]

If after \( NW_{it} \) weeks he finds a job in location \( j' \), the contribution of the unemployment spell to the likelihood function is:

\[
L_{2b}^j = \Pi_{2}^j(NW_t) \int B_{jt}(\varepsilon) P_{ue}^{jj'}(\varepsilon) d\varepsilon
\]

The posterior distribution of the match is then:

\[ f(\varepsilon|Y^t) = \frac{B_{jt'}(\varepsilon) P_{ue}^{jj'}(\varepsilon)}{\int B_{jt'}(\varepsilon) P_{ue}^{jj'}(\varepsilon) d\varepsilon} \]

### A.5 Becoming Unemployed

A worker in location \( j \) goes unemployed with probability \( P_{eu}^j(\varepsilon) \) and the density of the observed wage is \( A_{jt-1}(\varepsilon) \). From the previous period we know \( f(\varepsilon|Y^{t-1}) \). Given this, we can express the contribution of becoming employed to the likelihood as:

\[
L_{3}^j = \int A_{jt-1}(\varepsilon) P_{eu}^j(\varepsilon) dF(\varepsilon|Y^{t-1})
\]
A.6 Working

If the worker remains with the same employer, the likelihood contribution and the conditional distribution of the firm match after this period can be written as:

\[
L_{4a}^j = \int B_{jt}(\varepsilon) \left( 1 - P_{e\ell}^j(\varepsilon) - \int P_{ee}^j(\varepsilon, \varepsilon') d\varepsilon' - \sum_{j=1}^{3} \int P_{ee}^{jj'}(\varepsilon, \varepsilon') d\varepsilon' \right) dF(\varepsilon|Y^{t-1})
\]

\[
f(\varepsilon|Y^t) \propto B_{jt}(\varepsilon) \left( 1 - P_{e\ell}^j(\varepsilon) - \int P_{ee}^j(\varepsilon, \varepsilon') d\varepsilon' - \sum_{j=1}^{3} \int P_{ee}^{jj'}(\varepsilon, \varepsilon') d\varepsilon' \right) f(\varepsilon|Y^{t-1})
\]

Alternately, the employed worker may move to a different employer in the same type of location.

\[
L_{4b}^j = \int \int A_{jt-1}(\varepsilon) B_{jt}(\varepsilon') P_{ee}^j(\varepsilon, \varepsilon') dF(\varepsilon|Y^{t-1}) d\varepsilon'
\]

\[
f(\varepsilon'|Y^t) = \frac{B_{jt}(\varepsilon') \int A_{jt-1}(\varepsilon) P_{ee}^j(\varepsilon, \varepsilon') dF(\varepsilon|Y^{t-1})}{L_{4b}^j}
\]

Note that the inclusion of the function \( A_{jt-1}(\varepsilon) \) captures the fact that we in \( t - 1 \) we have observed a wage only because the worker has changed job in period \( t \). Hence this wage information is included in period \( t \) and not in period \( t - 1 \).

Finally, the employed worker may move to a different employer in a different type of location.

\[
L_{4c}^j = \int \int A_{jt-1}(\varepsilon) B_{jt}(\varepsilon') P_{ee}^{jj'}(\varepsilon, \varepsilon') dF(\varepsilon|Y^{t-1}) d\varepsilon'
\]

\[
f(\varepsilon'|Y^t, h) = \frac{B_{jt}(\varepsilon') \int A_{jt-1}(\varepsilon) P_{ee}^{jj'}(\varepsilon, \varepsilon') dF(\varepsilon|Y^{t-1})}{L_{4c}^j}
\]

B Normalizations of Job Offer Arrival Rates

In the model that are 48 free parameters that measure arrival rates of job offers of which 36 are probabilities of receiving a wage offer from a different location. Given that changing location is a rare event in the data, these parameters cannot be estimated precisely. Instead we estimate freely the 12 parameters that describe the probability of receiving a wage offer from the same location and we assume that the remaining probabilities are scaled by the 4 estimated parameters \( \rho_{jt} \) and \( \gamma \). We define \( \rho_{jt} \) to be a multiplier for arrival rates to a given city \( j \) and \( \gamma \) to be a parameter that scales the product \( \lambda_j(h)\rho_{jt} \) if the two location sizes are the same but the individual changes city. We use the same scaling factors for
unemployed and worker arrival rates. Arrival rates of job offers across locations are thus specified as follows.

\[
\lambda_{j'j}(h) = \lambda_j^u(h)\rho_{j'} \quad \text{if } j \neq j' \\
\lambda_{j'j}(h) = \lambda_j^u(h)\rho_{j'\gamma} \quad \text{if } j = j'
\]

\[
\lambda_{jj'}(h) = \lambda_j(h)\rho_{j'} \quad \text{if } j \neq j' \\
\lambda_{jj'}(h) = \lambda_j(h)\rho_{j'\gamma} \quad \text{if } j = j'
\]

These normalizations reduce the number of arrival rate parameters to be estimated from 48 to 16.
References

David Albouy 2008 “Are Big Cities Really Bad Places to Live? Improving Quality of Life Estimates Across Cities” working paper

Arzhagi, Muhammad and J. Vernon Henderson, 2006 “Networking off Madison Avenue,” manuscript.


N. Baum-Snow and R. Pavan. 2009 “Inequality and City Size” working paper


M. Greenstone, R. Hornbeck and Enrico Moretti. 2008 “Identifying Agglomeration Spillovers: Evidence from Million Dollar Plants” working paper


Lee, Sanghoon. “Ability Sorting and Consumer City,” manuscript.


Table 1: Estimates of the City Size Wage Premium from Census Micro Data

<table>
<thead>
<tr>
<th></th>
<th>S1: No Controls</th>
<th>S2: Individual Controls</th>
<th>S3: Individual + Local Ed. Controls</th>
</tr>
</thead>
<tbody>
<tr>
<td>MSAs: 250,000 - 1.5 million</td>
<td>0.141***</td>
<td>0.175***</td>
<td>0.185***</td>
</tr>
<tr>
<td></td>
<td>(0.0104)</td>
<td>(0.00984)</td>
<td>(0.00963)</td>
</tr>
<tr>
<td>MSAs: &gt; 1.5 million</td>
<td>0.238***</td>
<td>0.311***</td>
<td>0.315***</td>
</tr>
<tr>
<td></td>
<td>(0.0141)</td>
<td>(0.0106)</td>
<td>(0.00967)</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.029</td>
<td>0.046</td>
<td>0.039</td>
</tr>
</tbody>
</table>

Notes: The sample includes white men 20-64 working at least 40 weeks and at least 35 hours per week from the 5% census micro data samples. Wages of less than $1 or more than $300 (1999 dollars) are excluded from the sample. Main entries are coefficients and standard errors from regressions of log hourly wage on the control variables indicated at top. Individual controls include age, age squared and indicators for nine levels of education. Local education controls are the fraction of the sample population with each of these nine education levels living in the local county group or PUMA. Standard errors are clustered at the county group or PUMA level. Sample sizes are 1,269,114 in 1980, 1,330,116 in 1990 and 1,245,865 in 2000.
### Table 2: Estimates of the City Size Wage Premium from NLSY Data

<table>
<thead>
<tr>
<th>Specification</th>
<th>No Controls</th>
<th>Individual Controls</th>
<th>Individual + Cnty Educ. Cntrls</th>
<th>Individual Controls and Fixed Effects</th>
<th>All</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>5</td>
</tr>
<tr>
<td><strong>Panel A: CPI Deflated</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MSAs: 250,000 - 1.5 million</td>
<td>0.20</td>
<td>0.15</td>
<td>0.11</td>
<td>0.08</td>
<td>0.07</td>
</tr>
<tr>
<td></td>
<td>(0.008)**</td>
<td>(0.007)**</td>
<td>(0.007)**</td>
<td>(0.012)**</td>
<td>(0.012)**</td>
</tr>
<tr>
<td>MSAs: &gt; 1.5 million</td>
<td>0.30</td>
<td>0.23</td>
<td>0.17</td>
<td>0.14</td>
<td>0.12</td>
</tr>
<tr>
<td></td>
<td>(0.008)**</td>
<td>(0.007)**</td>
<td>(0.008)**</td>
<td>(0.013)**</td>
<td>(0.014)**</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.04</td>
<td>0.30</td>
<td>0.31</td>
<td>0.25</td>
<td>0.26</td>
</tr>
<tr>
<td><strong>Panel B: ACCRA Deflated</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MSAs: 250,000 - 1.5 million</td>
<td>0.15</td>
<td>0.10</td>
<td>0.08</td>
<td>0.05</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>(0.008)**</td>
<td>(0.006)**</td>
<td>(0.007)**</td>
<td>(0.011)**</td>
<td>(0.012)**</td>
</tr>
<tr>
<td>MSAs: &gt; 1.5 million</td>
<td>0.11</td>
<td>0.05</td>
<td>0.02</td>
<td>0.00</td>
<td>-0.01</td>
</tr>
<tr>
<td></td>
<td>(0.008)**</td>
<td>(0.007)**</td>
<td>(0.008)**</td>
<td>(0.013)</td>
<td>(0.013)</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.01</td>
<td>0.29</td>
<td>0.29</td>
<td>0.27</td>
<td>0.27</td>
</tr>
</tbody>
</table>

Each regression uses 1754 individuals and has 30,367 observations based on quarterly data. The sample includes white men in the NLSY79. Complete sample selection rules are explained in the text.
Table 3: Wages As a Function of Labor Force Experience

<table>
<thead>
<tr>
<th>Years of Labor Force Experience</th>
<th>CPI Deflated</th>
<th>CPI &amp; ACCRA Deflated</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Rural and MSAs &lt; 0.25 million</td>
<td>9.00</td>
<td>9.56</td>
</tr>
<tr>
<td>MSAs: 250,000 - 1.5 million</td>
<td>10.18</td>
<td>11.34</td>
</tr>
</tbody>
</table>

Panel A: Mean Wages

Panel B: Mean log Wage Growth from Entry into Labor Force

The sample is the same as that for Table 2 with the additional limitation that we must observe individuals to at least 15 years of labor force experience. This limitation reduces the number of individuals in the sample by 20 percent. Numbers in Panel A are in units of 1999 dollars (left panel) and 1999 dollars in the average priced metropolitan area (right panel).
Table 4: Turnover, Unemployment and Human Capital

| Years of Labor Force Experience | 0 | 1 | 5 | 10 | 15 | 0 | 1 | 5 | 10 | 15 |
|--------------------------------|---|---|---|----|----|---|---|---|----|----|----|
|                                |   |   |   |    |    |   |   |   |    |    |    |
| **Panel A: Turnover & Unemployment** |   |   |   |    |    |   |   |   |    |    |    |
| Number of Jobs                 |   |   |   |    |    |   |   |   |    |    |    |
| Rural and MSAs < 0.25 million  | 1 | 1.6 | 3.5 | 5.5 | 6.7 | 0.0 | 2.9 | 16.2 | 27.7 | 34.3 |
| MSAs: 250,000 - 1.5 million    | 1 | 1.6 | 3.5 | 5.2 | 6.6 | 0.0 | 2.0 | 12.7 | 21.2 | 27.1 |
| MSAs: > 1.5 million            | 1 | 1.5 | 3.2 | 4.8 | 5.9 | 0.0 | 1.7 | 9.9  | 15.7 | 21.0 |
| Weeks of Unemployment          |   |   |   |    |    |   |   |   |    |    |    |
| Rural and MSAs < 0.25 million  | 0.0 | 2.9 | 16.2 | 27.7 | 34.3 | 0.0 | 2.0 | 12.7 | 21.2 | 27.1 |
| MSAs: 250,000 - 1.5 million    | 0.0 | 2.0 | 12.7 | 21.2 | 27.1 | 0.0 | 1.7 | 9.9  | 15.7 | 21.0 |
| MSAs: > 1.5 million            | 0.0 | 1.7 | 9.9  | 15.7 | 21.0 | 0.0 | 1.7 | 9.9  | 15.7 | 21.0 |

**Panel B: Human Capital**

<table>
<thead>
<tr>
<th>Fraction College Graduate</th>
<th>0.22</th>
<th>0.22</th>
<th>0.21</th>
<th>0.21</th>
<th>0.21</th>
<th>13.20</th>
<th>13.22</th>
<th>13.14</th>
<th>13.13</th>
<th>13.12</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rural and MSAs &lt; 0.25 million</td>
<td>0.22</td>
<td>0.22</td>
<td>0.21</td>
<td>0.21</td>
<td>0.21</td>
<td>13.20</td>
<td>13.22</td>
<td>13.14</td>
<td>13.13</td>
<td>13.12</td>
</tr>
<tr>
<td>MSAs: 250,000 - 1.5 million</td>
<td>0.35</td>
<td>0.35</td>
<td>0.35</td>
<td>0.35</td>
<td>0.35</td>
<td>13.84</td>
<td>13.80</td>
<td>13.86</td>
<td>13.79</td>
<td>13.80</td>
</tr>
<tr>
<td>MSAs: &gt; 1.5 million</td>
<td>0.38</td>
<td>0.39</td>
<td>0.39</td>
<td>0.39</td>
<td>0.39</td>
<td>14.17</td>
<td>14.22</td>
<td>14.18</td>
<td>14.29</td>
<td>14.31</td>
</tr>
<tr>
<td>Years of Schooling</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Rural and MSAs &lt; 0.25 million</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MSAs: 250,000 - 1.5 million</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MSAs: &gt; 1.5 million</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

See Table 3 for a description of the sample. Panel B uses highest grade ever completed to define schooling variables.
Table 5: Migration Patterns by Education

<table>
<thead>
<tr>
<th>Location of Labor Force Entry</th>
<th>Location at 15 Years of Labor Force Experience</th>
<th>Rural and MSAs &lt; 0.25 million</th>
<th>MSAs 250,000 to 1.5 million</th>
<th>MSAs: &gt; 1.5 million</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Rural and MSAs &lt; 0.25 million</td>
<td>0.87</td>
<td>0.09</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>MSAs: 250,000 - 1.5 million</td>
<td>0.11</td>
<td>0.87</td>
<td>0.02</td>
</tr>
<tr>
<td></td>
<td>MSAs: &gt; 1.5 million</td>
<td>0.10</td>
<td>0.09</td>
<td>0.81</td>
</tr>
</tbody>
</table>

Panel A: High School Only

Panel B: College or More

|                              | Rural and MSAs < 0.25 million                 | 0.64                         | 0.24                      | 0.12               |
|                              | MSAs: 250,000 - 1.5 million                   | 0.10                         | 0.76                      | 0.14               |
|                              | MSAs: > 1.5 million                           | 0.08                         | 0.18                      | 0.74               |

See Table 3 for a description of the sample. Entries give the fraction of those entering the labor force at the location listed at left residing in the location along the top at 15 years of labor force experience.
Table 6: Log Wage Growth Decomposition  
0 to 15 Years of Labor Force Experience

<table>
<thead>
<tr>
<th></th>
<th>CPI Deflated</th>
<th></th>
<th>CPI &amp; ACCRA Deflated</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Within Job</td>
<td>Job to Job</td>
<td>Job to Unemp</td>
<td>Un-Known</td>
</tr>
<tr>
<td>Rural and MSAs &lt; 0.25 million</td>
<td>0.30</td>
<td>0.24</td>
<td>-0.03</td>
<td>0.01</td>
</tr>
<tr>
<td>MSAs: 250,000 - 1.5 million</td>
<td>0.44</td>
<td>0.30</td>
<td>-0.06</td>
<td>0.00</td>
</tr>
<tr>
<td>MSAs: &gt; 1.5 million</td>
<td>0.50</td>
<td>0.24</td>
<td>0.01</td>
<td>0.00</td>
</tr>
</tbody>
</table>

Reported numbers decompose the wage growth results reported in Table 3. For the purpose of these calculations, we assign individuals only to their locations at 15 years of experience. Sums of wage growth components may differ from Table 3 due to rounding.
Table 7: Model Fit: Mobility Rates

<table>
<thead>
<tr>
<th>Mobility Rates</th>
<th>College Sample</th>
<th>High School Sample</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Data</td>
<td>Model</td>
</tr>
<tr>
<td></td>
<td>Model</td>
<td>Data</td>
</tr>
<tr>
<td>Fraction of Job Changes</td>
<td>8.8%</td>
<td>9.1%</td>
</tr>
<tr>
<td>Fraction of Job to Job Transitions</td>
<td>6.2%</td>
<td>6.7%</td>
</tr>
<tr>
<td>Fraction of Job to Unemployment to Job Transitions</td>
<td>2.6%</td>
<td>2.2%</td>
</tr>
<tr>
<td>Fraction of Location Changes</td>
<td>2.1%</td>
<td>2.1%</td>
</tr>
</tbody>
</table>

Notes: Entries give the percent of observations in each mobility category from actual data and model simulated data.
Table 8: Model Fit: Mobility Rates Conditional on Location Change

<table>
<thead>
<tr>
<th>Period t Location: Data</th>
<th>Period t Location: Model</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Small</td>
</tr>
<tr>
<td>Period t-1 Location</td>
<td></td>
</tr>
<tr>
<td>Small</td>
<td>11.3%</td>
</tr>
<tr>
<td>Medium</td>
<td>8.3%</td>
</tr>
<tr>
<td>Large</td>
<td>4.5%</td>
</tr>
</tbody>
</table>

Panel A: College Sample

<table>
<thead>
<tr>
<th>Period t-1 Location</th>
<th>Small</th>
<th>Medium</th>
<th>Large</th>
</tr>
</thead>
<tbody>
<tr>
<td>Small</td>
<td>22.2%</td>
<td>10.6%</td>
<td>5.0%</td>
</tr>
<tr>
<td>Medium</td>
<td>11.4%</td>
<td>19.4%</td>
<td>4.8%</td>
</tr>
<tr>
<td>Large</td>
<td>5.6%</td>
<td>7.6%</td>
<td>13.3%</td>
</tr>
</tbody>
</table>

Panel B: High School Sample

Notes: Entries give the fraction of location changes for each pair of location types from the actual and simulated data.
Table 9: Parameter Estimates from the Structural Model

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>College Sample</th>
<th></th>
<th>High School Sample</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Low Type</td>
<td>High Type</td>
<td>Low Type</td>
<td>High Type</td>
</tr>
<tr>
<td>A. Components of Wages</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\beta_0$</td>
<td>Wage Constant for Small Locations</td>
<td>6.57</td>
<td>7.08</td>
<td>6.37</td>
<td>6.77</td>
</tr>
<tr>
<td>$\beta_0$</td>
<td>Wage Constant for Medium Locations</td>
<td>6.66</td>
<td>7.14</td>
<td>6.48</td>
<td>6.83</td>
</tr>
<tr>
<td>$\beta_0$</td>
<td>Wage Constant for Large Locations</td>
<td>6.58</td>
<td>7.17</td>
<td>6.33</td>
<td>6.74</td>
</tr>
<tr>
<td>$\beta_1$</td>
<td>Return to Experience from Small</td>
<td>0.042</td>
<td>0.063</td>
<td>0.054</td>
<td>0.061</td>
</tr>
<tr>
<td>$\beta_1$</td>
<td>Return to Experience from Medium</td>
<td>0.053</td>
<td>0.068</td>
<td>0.055</td>
<td>0.071</td>
</tr>
<tr>
<td>$\beta_1$</td>
<td>Return to Experience from Large</td>
<td>0.061</td>
<td>0.065</td>
<td>0.056</td>
<td>0.064</td>
</tr>
<tr>
<td>$\beta_2$</td>
<td>Coefficient On Experience Squared</td>
<td>-0.00081</td>
<td>-0.00184</td>
<td>-0.00184</td>
<td>-0.00184</td>
</tr>
<tr>
<td>B. Amenities</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha_2$</td>
<td>Amenity of Medium Sized Places</td>
<td>-0.131</td>
<td>0.099</td>
<td>-0.012</td>
<td>-0.267</td>
</tr>
<tr>
<td>$\alpha_3$</td>
<td>Amenity of Large Places</td>
<td>-0.051</td>
<td>0.000</td>
<td>-0.041</td>
<td>-0.163</td>
</tr>
<tr>
<td>C. Arrival and Separation Rates</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\lambda_1$</td>
<td>Job Offer Arrival Rate Within Small Locations</td>
<td>0.10</td>
<td>0.05</td>
<td>0.13</td>
<td>0.13</td>
</tr>
<tr>
<td>$\lambda_2$</td>
<td>Job Offer Arrival Rate Within Medium Locations</td>
<td>0.10</td>
<td>0.06</td>
<td>0.12</td>
<td>0.13</td>
</tr>
<tr>
<td>$\lambda_3$</td>
<td>Job Offer Arrival Rate Within Large Locations</td>
<td>0.11</td>
<td>0.06</td>
<td>0.12</td>
<td>0.12</td>
</tr>
<tr>
<td>$\lambda_{11}$</td>
<td>Job Offer Arrival Rate Within Small from Unemployed</td>
<td>0.14</td>
<td>0.11</td>
<td>0.17</td>
<td>0.18</td>
</tr>
<tr>
<td>$\lambda_{21}$</td>
<td>Job Offer Arrival Rate Within Medium from Unemployed</td>
<td>0.19</td>
<td>0.14</td>
<td>0.17</td>
<td>0.23</td>
</tr>
<tr>
<td>$\lambda_{31}$</td>
<td>Job Offer Arrival Rate Within Large from Unemployed</td>
<td>0.16</td>
<td>0.14</td>
<td>0.16</td>
<td>0.23</td>
</tr>
<tr>
<td>$\rho_1$</td>
<td>Receive Rate in Small: $\lambda_{21}=\lambda_{21}^{<em>}p_{1}$ and $\lambda_{21}=\lambda_{21}^{</em>}p_{1}$</td>
<td>0.15</td>
<td>0.09</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\rho_1$</td>
<td>Receive Rate in Medium</td>
<td>0.14</td>
<td>0.09</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\rho_1$</td>
<td>Receive Rate in Large</td>
<td>0.13</td>
<td>0.09</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\gamma$</td>
<td>Own Location Multiplier: $\lambda_{11}=\lambda_{11}^{<em>}p_{1}^{</em>}$ and $\lambda_{11}=\lambda_{11}^{<em>}p_{1}^{</em>}$</td>
<td>1.93</td>
<td>1.80</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\delta_1$</td>
<td>Separation Rate in Small</td>
<td>0.025</td>
<td>0.005</td>
<td>0.033</td>
<td>0.048</td>
</tr>
<tr>
<td>$\delta_2$</td>
<td>Separation Rate in Medium</td>
<td>0.025</td>
<td>0.009</td>
<td>0.038</td>
<td>0.038</td>
</tr>
<tr>
<td>$\delta_3$</td>
<td>Separation Rate in Large</td>
<td>0.024</td>
<td>0.009</td>
<td>0.020</td>
<td>0.022</td>
</tr>
<tr>
<td>D. Benefits and Costs</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$b$</td>
<td>Unemployment Benefit</td>
<td>1.34</td>
<td>1.83</td>
<td></td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>Moving Cost</td>
<td>2.16</td>
<td>4.83</td>
<td></td>
<td></td>
</tr>
<tr>
<td>E. Heterogeneity</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\pi^1$</td>
<td>Probability of Type Given Start in Small Location</td>
<td>0.44</td>
<td>0.56</td>
<td>0.60</td>
<td>0.40</td>
</tr>
<tr>
<td>$\pi^2$</td>
<td>Probability of Type Given Start in Medium Location</td>
<td>0.37</td>
<td>0.63</td>
<td>0.59</td>
<td>0.41</td>
</tr>
<tr>
<td>$\pi^3$</td>
<td>Probability of Type Given Start in Large Location</td>
<td>0.40</td>
<td>0.60</td>
<td>0.50</td>
<td>0.50</td>
</tr>
<tr>
<td>F. Distributions</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma_1$</td>
<td>Standard Deviation of Match in Small</td>
<td>0.30</td>
<td>0.27</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma_2$</td>
<td>Standard Deviation of Match in Medium</td>
<td>0.32</td>
<td>0.22</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma_3$</td>
<td>Standard Deviation of Match in Large</td>
<td>0.31</td>
<td>0.23</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma_U$</td>
<td>Standard Deviation of Utility Shock for Unemployed</td>
<td>1.81</td>
<td>1.51</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma_S$</td>
<td>Standard Deviation of Job Switching Cost Shock</td>
<td>19.92</td>
<td>6.94</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma_M$</td>
<td>Standard Deviation of Moving Cost Shock</td>
<td>16.31</td>
<td>8.28</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma_w$</td>
<td>Standard Deviation of Wage Measurement Error</td>
<td>0.32</td>
<td>0.32</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes: This table shows the universe of estimated model parameters. The discount rate is calibrated to 0.95.
### Table 10: Counterfactual City Size Wage Premia  
College Sample

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Regression Coefficients</th>
<th>Gap With Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Large</td>
<td>Medium</td>
</tr>
<tr>
<td><strong>Panel A: Comparison Counterfactual Wage Premia</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1. Baseline Data</td>
<td>0.15</td>
<td>0.09</td>
</tr>
<tr>
<td>2. Model</td>
<td>0.15</td>
<td>0.09</td>
</tr>
<tr>
<td>3. Restricted Mobility (Compare to Row 2)</td>
<td>0.17</td>
<td>0.16</td>
</tr>
</tbody>
</table>

**Panel B: Counterfactuals With Free Mobility (Compare to Row 2)**

- Equalize Ability Distribution at LF Entry: 0.14, 0.14, 0.00, 0.05
- Equalize Arrival Rates across Locs: 0.18, 0.14, 0.04, 0.05
- Equalize Separation Rates across Locs: 0.19, 0.14, 0.04, 0.05
- Equalize Return to Experience across Locs: 0.12, 0.07, -0.03, -0.02
- Equalize Wage Constant across Locs: 0.10, 0.09, -0.05, 0.00
- Equalize Match Distribution across Locs: 0.16, 0.15, 0.01, 0.06

**Panel C: Restricted Mobility Counterfactuals (Compare to Row 3)**

- Equalize Ability Distribution at LF Entry: 0.11, 0.06, -0.06, -0.11
- Equalize Arrival Rates across Locs: 0.16, 0.10, -0.01, -0.07
- Equalize Separation Rates across Locs: 0.15, 0.08, -0.02, -0.08
- Equalize Return to Experience across Locs: 0.13, 0.08, -0.05, -0.09
- Equalize Wage Constant across Locs: 0.08, 0.03, -0.09, -0.13
- Equalize Match Distribution across Locs: 0.13, 0.10, -0.04, -0.07

Notes: Panel A Row 1 presents average wage premia from the raw data, Row 2 shows premia based on simulated data and Row 3 is based on simulated data where mobility cost is infinite. Other estimates are based on simulated data using parameter values achieving the listed scenario. For ability distribution equalization, we set probabilities of labor force entry by type across locations equal to their weighted average across locations. For search friction equalization, we set the arrival rates equal to their weighted average across locations, where the weights are the initial composition of the labor force. Equalization of return to experience across locations is achieved analogously. Imposing all restrictions in Panel C simultaneously generates simulated wage premia of 0 in both location types.
### Table 11: Counterfactual City Size Wage Premia
High School Sample

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Regression Coefficients</th>
<th>Gap With Fitted Values</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Medium</td>
<td>Large</td>
</tr>
<tr>
<td>1. Baseline Data</td>
<td>0.09</td>
<td>0.03</td>
</tr>
<tr>
<td>2. Model</td>
<td>0.10</td>
<td>0.03</td>
</tr>
<tr>
<td>3. Restricted Mobility (Compare to Row 2)</td>
<td>0.09</td>
<td>0.02</td>
</tr>
</tbody>
</table>

#### Panel A: Comparison Counterfactual Wage Premia

#### Panel B: Counterfactuals With Free Mobility (Compare to Row 2)

| Equalize Ability Distribution at LF Entry | 0.09  | -0.02 | -0.01 | -0.05 |
| Equalize Arrival Rates across Locs | 0.08  | 0.03  | -0.01 | -0.01 |
| Equalize Separation Rates across Locs | 0.09  | 0.02  | 0.00  | -0.01 |
| Equalize Return to Experience across Locs | 0.06  | 0.02  | -0.04 | -0.01 |
| Equalize Wage Constant across Locs | 0.02  | 0.07  | -0.08 | 0.04 |
| Equalize Match Distribution across Locs | 0.12  | 0.06  | 0.02  | 0.03 |

#### Panel C: Restricted Mobility Counterfactuals (Compare to Row 3)

| Equalize Ability Distribution at LF Entry | 0.08  | -0.01 | 0.00  | -0.04 |
| Equalize Arrival Rates across Locs | 0.06  | -0.04 | -0.02 | -0.06 |
| Equalize Separation Rates across Locs | 0.07  | 0.00  | -0.02 | -0.03 |
| Equalize Return to Experience across Locs | 0.04  | 0.01  | -0.05 | -0.01 |
| Equalize Wage Constant across Locs | 0.00  | 0.05  | -0.08 | 0.03 |
| Equalize Match Distribution across Locs | 0.13  | 0.05  | 0.04  | 0.03 |

See notes to Table 8 for an explanation of table entries.
Figure 1: Actual and Predicted Wages by Location
College Sample

Panel A: Rural Areas and Small Metropolitan Areas

Panel B: Medium Sized Metropolitan Areas

Panel C: Large Metropolitan Areas

Predicted values are based on model simulation using parameter values reported in Table 9.
Predicted values are based on model simulation using parameter values reported in Table 9.