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Utilizing Artificial Neural Network Model to Predict Stock Markets

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Abstract

The objective of this paper is to examine the dynamic interrelations among major world stock markets through the use of artificial neural networks. The data was derived from daily stock market indices of the major world stock markets of Canada, France, Germany, Japan, United Kingdom (UK), the United States (US), and the world excluding US (World). Multilayer Perceptron models with logistic activation functions were better able to foresee the daily stock returns than the traditional forecasting models, in terms of lower mean squared errors. Furthermore, a multilayer perceptron with five units in the hidden layer seemed to predict more precisely the returns of stock indices than a neural network with two hidden elements. Hence, it is inferred that neural systems could be used as an alternative or supplemental method for predicting financial variables and thus justified the potential use of these model by practitioners.

JEL: C3, C32, C45, C5, C63, F3, G15.

Keywords: Neural Networks, Major Stock Markets, Dynamic Interrelations, Forecasting.

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1. INTRODUCTION

Neural networks are powerful forecasting tools that draw on the most recent developments in artificial intelligence research. They are non-linear models that can be trained to map past and future values of time series data and thereby extract hidden structures and relationships that govern the data. Neural networks are applied in many fields such as computer science, engineering, medical and criminal diagnostics, biological investigation, and economic research. They can be used for analysing relations among economic and financial phenomena, forecasting, data filtration, generating time-series, and optimization (Hawley, Johnson, and Raina, 1990; White, 1988; White 1996; Terna, 1997; Cogger, Koch and Lander. 1997; Cheh, Weinberg, and Yook, 1999; Cooper, 1999; Hu and Tsoukalas, 1999; Moshiri, Cameron, and Scuse, 1999; Shtub and Versano, 1999; Garcia and Gencay, 2000; and Hamm and Brorsen, 2000).

This paper investigates the application of artificial neural networks to the dynamic interrelations among major world stock markets. These stock market indices are: Canada, France, Germany, Japan, United Kingdom (UK), the United States (US), and the world excluding US (World). Based on the criteria of Root Mean Square Error (RMSE), Maximum Absolute Error (MAE), and the value of the objective function the model is compared to other statistical methods such as Ordinary Least Squares (OLS) and General Linear Regression Model (GLRM).

Neural networks have found ardent supporters among various avant-garde portfolio managers, investment banks and trading firms. Most of the major investment banks, such as Goldman Sachs and Morgan Stanley, have dedicated departments to the implementation of neural networks. Fidelity Investments has set up a mutual fund whose portfolio allocation is based solely on recommendations produced by an artificial neural network. The fact that major companies in the financial industry are investing resources in neural networks indicates that artificial neural networks may serve as an important method of forecasting.

Artificial neural networks are information processing systems whose structure and function are motivated by the cognitive processes and organizational structure of neuro-biological systems (Stephen, Luit and Sema, 1992). The basic components of the networks are highly interconnected processing

elements called neurons, which work independently in parallel (Consten and May, 1996). Synaptic connections are used to carry messages from one neuron to another. The strength of these connections varies. These neurons store information and learn meaningful patterns by strengthening their interconnections. When a neuron receives a certain number of stimuli, and when the sum of the received stimuli exceeds a certain threshold value, it fires and transmits the stimulus to adjacent neurons (Sohl, 1995).

The power of neural computing comes from the threshold concept. It provides a way to transform complex interrelationships into simple yes-no situations. When the combination of several factors begins to become overly complex, the neuron model posits an intermediate yes-no node to retain simplicity. As a given algorithm learns by synthesizing more training records, the weights between its interconnected processing elements strengthen and weaken dynamically (Baets, 1994). The computational structure of artificial neural networks has attractive characteristics such as graceful degradation, robust recall with noisy and fragmented data, parallel distributed processing, generalization to patterns outside of the training set, non-linear modelling, and learning (Tours, Rabelo, and Velasco, 1993; Ripley, 1993; Terna, 1997; Cogger, Koch and Lander. 1997; Cheh, Weinberg, and Yook, 1999; Cooper, 1999; Hu and Tsoukalas, 1999).

Multilayer networks are formed by cascading a group of single layers. In a three layer network, for example, there is an input layer, an output layer, and a "hidden" layer. The nodes of different layers are densely interconnected through direct links. At the input layers, the nodes receive the values of input variables and multiply them through the network, layer by layer. The middle layer nodes are often characterized as feature-detectors. The number of hidden layers and the number of nodes in each hidden layer can be selected arbitrarily. The initial weights of the connections can be chosen randomly.

The computed output is compared to the known output. If the computed output is correct, then nothing more is necessary. If the computed output is incorrect, then the weights are adjusted so as to make the computed output closer to the known output. This process is continued for a large number of cases, or time-series, until the net gives the correct output for a given input. The entire collection of cases learned is called a "training sample" (Connor, Martin, and Atlas, 1994). In most real world problems, the neural network is never 100% correct. Neural networks are programmed to learn up to

a given threshold of error. After the neural network learns up to the error threshold, the weight adaptation mechanism is turned off and the net is tested on known cases it has not seen before. The application of the neural network to unseen cases gives the true error rate (Baets, 1994).

Artificial neural networks present a number of advantages over conventional methods of analysis. First, artificial neural networks make no assumptions about the nature of the distribution of the data and are not therefore, biased in their analysis. Instead of making assumptions about the underlying population, neural networks with at least one middle layer use the data to develop an internal representation of the relationship between the variables (White, 1992).

Second, since time-series data are dynamic in nature, it is necessary to have non-linear tools in order to discern relationships among time-series data. Neural networks are best at discovering non-linear relationships (Wasserman, 1989; Hoptroff, 1993; Moshiri, Cameron, and Scuse, 1999; Shtub and Versano, 1999; Garcia and Gencay, 2000; and Hamm and Brorsen, 2000). Third, neural networks perform well with missing or incomplete data. Whereas traditional regression analysis is not adaptive, typically processing all older data together with new data, neural networks adapt their weights as new input data becomes available (Kuo and Reitch, 1994). Fourth, it is relatively easy to obtain a forecast in a short period of time as compared with an econometric model.

However, there are some drawbacks connected with the use of artificial neural networks. No estimation or prediction errors are calculated with an artificial neural network (Caporaletti, Dorsey, Johnson, and Powell, 1994). Also, artificial neural networks are "black boxes," for it is impossible to figure out how relations in hidden layers are estimated (Li, 1994). In addition, a network may become a bit overzealous and try to fit a curve to some data even when there is no relationship.

Another drawback is that a neural networks have long training times. Reducing training time is crucial because building a neural network forecasting system is a process of trial and error. Therefore, the more experiments a researcher can run in a finite period of time, the more confident he can be of the result.

The remainder of the paper is organized in the following sections. Section two offers a brief review of the current literature. Section three summarizes the neural network model. Section four describes the data used in this study. Section five presents the empirical results for the major stock

market indices. Section six concludes.

2. LITERATURE REVIEW

There is a growing body of literature based on the comparison of neural network computing to traditional statistical methods of analysis. Hertz, Krogh, and Palmer (1991) offer a comprehensive view of neural networks and issues of their comparison to statistics. Hinton (1992) investigates the statistical aspects of neural networks. Weiss and Kulikowski (1991) offer an account of the classification methods of many different neural and statistical models.

The main focus for the artificial neural network technology, in application to the financial and economic fields, has so far been data involving variables in non-linear relation. Many economists advocate the application of neural networks to different fields in economics (Kuan and White, 1994; Bierens, 1994; Lewbel, 1994). According to Granger (1991) non-linear relationships in financial and economic data are more likely to occur than linear relationships. New tests based on neural network systems therefore have increased in popularity among economists. Several authors have examined the application of neural networks to financial markets, where the non-linear properties of financial data provide many difficulties for traditional methods of analysis (Omerod, Taylor, and Walker, 1991; Grudnitski and Osburn, 1993; Altman, Marco, and Varetto, 1994; Kaastra and Boyd, 1995; Witkowska, 1995).

Yoon and Swales (1990) compare neural networks to discriminant analysis with respect to prediction of stock price performance and find that the neural network is superior to discriminant analysis in its predictions. Surkan and Singleton (1990) find that a neural network models perform better than discriminant analysis in predicting future assignments of risk ratings to bonds.

Trippi and DeSieno (1992) apply a neural network system to model the trading of Standard and Poor 500 index futures. They find that the neural network system outperforms passive investment in the index. Based on the empirical results, they favor the implementation of neural network systems into the mainstream of financial decision making.

3. THE NEURAL NETWORK MODEL¹

A single artificial neuron is the basic element of the neural network. It comprises several inputs $(x_1, x_2, ..., x_m)$ and one output y that can be written as follows:

$$(1) \qquad y = f(x_i, w_i)$$

where, w_i are the function parameter weights of the function f.

Equation (1) is called an activation function. It maps any real input into a usually bounded range, often [0, 1] or [-1, 1]. This function may be linear or non-linear such as one of the following:

A. Hyperbolic tangent:
$$f(x) = tanh(x) = 1 - \frac{2}{1 + exp(2x)}$$
,

- B. Logistic $f(x) = \frac{1}{1 + \exp(-x)}$,
- C. Threshold f(x) = 0 if x < 0, 1 otherwise,

D. Gaussian
$$f(x) = \exp(\frac{x^2}{2})$$
.

If equation (1) transforms inputs into output linearly, then a single neuron is described by the following:

(2)
$$y = \sum_{i=1}^{m} x_i w_i = \mathbf{w}^{\mathrm{T}} \mathbf{x}$$

where, $\mathbf{w} = [w_i]$, the vector of weights assigned for each input x_i ,

$$\mathbf{x} = [\mathbf{x}_i], (i = 1, 2, ..., m).$$

The neuron layer can be constructed having several neurons with the same sets of inputs but with different outputs. The layer of neurons is the simplest network. Assuming that the network consists of only one layer, and the activation function is linear, the output vector \mathbf{y} can be derived from input data \mathbf{x} as the weighted sum of the inputs, as follows:

$$(3) \qquad \mathbf{y} = \mathbf{W}^{\mathrm{T}} \mathbf{x}$$

where,

 $\mathbf{y} = [\mathbf{y}_i]$ - the vector consists of n outputs,

 $\mathbf{W}^{T} = [\mathbf{w}_{ij}]^{T}$ - transposed matrix [nxm] of weights,

 $\mathbf{x} = [\mathbf{x}_i]$ - the vector comprises m inputs.

To solve a problem using neural networks, sample inputs and desired outputs must be given. The network then learns by adjusting its weights.

The daily stock price indices, $ly^{j}(L)$, are transformed to daily rates of return as follows:

(4)
$$ly^{j}(L) = \log[y^{j}(L)] - \log[y^{j}(L-1)]; \text{ for } j = 0, 1, ..., 6;$$

 $L = 1, 2, ..., 15$

where,

L - is the lag index,

 $y^{j}(L)$ - is daily stock returns in the j-th country lagged by L periods.

Two stages of experiments can be distinguished: regression analysis and application of the artificial neural networks. The regression analysis is designed to help identify the statistically significant variables of the model. Then, in the second stage, the significant variables are inputted to the neural network model. The regression model is:

(5)
$$ly^{0}(1) = f[ly^{0}(L), ly^{j}(L-1), ly^{j}(L)]; \text{ for } j = 1, 2, ..., 5; L = 2, ..., 15.$$

is the aim of the first stage of the investigation.

When f is a linear function, equation (5) can be written as:

(6)
$$ly^{0}(1) = a_{1}^{0} + \sum_{L=2}^{15} a_{L}^{0} ly^{0}(L) + \sum_{L=1}^{15} a_{L}^{1} ly^{1}(L) + \sum_{L=1}^{15} a_{L}^{2} ly^{2}(L) + \dots + \sum_{L=1}^{15} a_{L}^{5} ly^{5}(L)$$

where,

 a_1^0 - the intercept,

 a_{L}^{j} - parameter estimates (j = 0, 1, ..., 5; L = 1, 2,..., 15).

Several models are considered in this paper. The models include different sets of daily stock returns $ly^{j}(L)$ as explanatory

variables. Model (6) can be written as:

(7)
$$ly^{0}(1) = a_{1}^{0} + \sum_{L=2}^{LMAX} a_{L}^{0} ly^{0}(L) + \sum_{L=LMIN}^{LMAX} a_{L}^{1} ly^{1}(L) + \sum_{L=LMIN}^{LMAX} a_{L}^{2} ly^{2}(L) + ... + \sum_{L=LMIN}^{LMAX} a_{L}^{5} ly^{5}(L)$$

where,

LMAX - the highest index L,

LMIN - the smallest index L.

4. **DESCRIPTION OF THE DATA**

The data base for this study consists of daily stock market indices of major stock markets. These stock market indices are: Canada, France, Germany, Japan, the United States (US), United Kingdom (UK), and the world excluding US (WORLD). The indices for the rest of the countries were calculated by Morgan Stanley Capital International Perspective, Geneva (MSCIP). One of the main advantages of the stock market indices compiled by the MSCIP is that these indices do not doublecount those stocks which are multiple-listed on other foreign stock exchanges. Thus, any observed interdependence among stock markets cannot be attributed to the multiple listings (Eun and Shim, 1989; Shachmurove, 1996; Friedman and Shachmurove, 1996; Friedman and Shachmurove, 1997). The data base covers the period January 3, 1987, through November 28, 1994, with a total of 2,064 observations per stock market.

5. THE EMPIRICAL RESULTS

The empirical results are based on two stages. In stage one, a regression analysis is designed to help identify the statistically significant variables of the model. In section two, the significant variables are inputted to the neural network model.

5.1 Empirical Results Based on OLS

Five variants of the regression model denoted by A, B, C, D and E are constructed. The five regression models differ by the maximum number of lags (LMAX) and the number of minimum lags (LMIN) and thus result in a different number of parameters to be estimated. For all models, except model B, LMIN = 1, otherwise LMIN = 2. The LMAX values are: 3 for model A, 5 for models B and C, 7 for model D, and 15 for model E.

All variants of the regression model are described in Tables 1-7 by:

- The symbol of the model together with the numbers of minimum and maximum lags (*LMIN*, *LMAX*) in the variables $ly^{j}(L)$,

- Number of explanatory variables in the model,

- Adjusted determination coefficient, R², and

- RMSE - Root Mean Squared Error.

All models are run with and without trend, denoted by T. In all models the trend variable is found insignificant.²

Tables 1-7 present the significant variables in all variants of the model for all investigated countries. It is interesting to note that the Canadian stock exchange index influences all stocks in the majority of countries and models except for the French index in models C and D. Except in model A, France does not influence the Japanese financial market. France does not have auto-correlation except for the seventh daily lag in models D and E. Except for Germany and the World, Japanese daily stock returns are significant after 7 or even more days for the majority of models and countries. Germany does not influence Canada, except for model B, but it strongly influences Japan.

Model E describes all explanatory variables the best since adjusted R^2 is the highest and RMSE is the smallest for this variant of the regression model. Though for other models, except for model B, fitness statistics are similar. The lowest determination coefficients are found for Japan and World while the percentage errors are the highest for Japan and Germany.

Based on the data presented in Tables 1 - 7 it can be ascertained that only some variables, usually the same for all variants of the model, are significant and R^2 does not essentially increase due to the increase of the number of explanatory variables. In such situations, it is assumed that reducing (in model E) the number of the explanatory variables to the ones that are significant will not essentially affect the fitness statistics. Table 8 presents the comparison of the parameter estimates, t-statistics, and RMSE for two linear models describing rates of daily stock returns for World. These models contain, on one hand, all 89 variables and, on the other hand, the reduced number of explanatory variables, i.e., only variables which are significant in the general model.

5.2 Empirical Results Based On Neural Network Models

Application of the artificial neural networks, constructed on the basis of model E, for further analysis is the second stage of this investigation. Since it is impossible to introduce all 89 variables into ANN experiments, the input layer contains only the significant, according to the regression analysis, variables. Thus, the set of input variables is different for each country. Two types of ANN models are constructed:

1. The simple neuron (1) with linear activation function GLRM,

$$(8) \quad ly^{0}(1) = b_{1}^{0} + \sum_{L \in \mathbf{b}^{0}} b_{L}^{0} ly^{0}(L) + \sum_{L \in \mathbf{b}^{1}} b_{L}^{1} ly^{1}(L) + \dots + \sum_{L \in \mathbf{b}^{5}} b_{L}^{5} ly^{5}(L)$$

where,

 b^0 , b^1 ,..., b^5 - are the sets of L indices defining significant variables,

 b_1^0 - the intercept (bias),

2. Multilayer perceptron (MLP) with one hidden layer containing two MLP(2) or five MLP(5) units with the logistic activation function for the hidden layer and linear activation function for the output layer. Elements in the hidden layer are estimated on the basis of the following relation:

(9)
$$h_{n} = f \left[c_{n1}^{0} + \sum_{L \in \mathbf{b}^{0}} c_{nL}^{0} l \tilde{y}^{0} (L) + \sum_{L \in \mathbf{b}^{1}} c_{nL}^{1} l \tilde{y}^{1} (L) + \dots + \sum_{L \in \mathbf{b}^{5}} c_{nL}^{5} l \tilde{y}^{5} (L) \right];$$

for n = 1, 2 or n = 1, 2, ..., 5,

where,

f - the logistic function,

 $l\tilde{y}^{j}(L)$ - standardised variables $ly^{j}(L)$,

 c_{n1}^{0} - the intercept - bias of the n-th unit in the hidden layer (n= 1, 2 or n = 1, 2,..., 5),

 c_{nL}^{j} - are weights estimated for the n-th unit in the hidden layer standing by L-th variable from the jthe country (j = 0, 1, ..., 5; L = 1, 2,..., 15).

The output layer consists of one variable $ly^{0}(1)$ that is estimated according to the following relation:

(10)
$$ly^{0}(1) = d_{0} + \sum_{n=1}^{H} d_{n}h_{n}$$

where,

 d_0 - the intercept - bias estimated for the output variable $ly^0(1)$,

 d_n - are the estimated weights standing by n-th (n = 1,..., H) unit in the hidden layer,

H - number of elements in the hidden layers of the ANN.

The results of the experiments are presented in Tables 9 - 11. Comparing relations (8) and (9), it can be noted that in the GLRM model the variables are original i. e. $Iy^{j}(L)$ while in the MLP model, the variables are standardised, i.e., $I\tilde{y}^{j}(L)$. So even if there are no hidden layers in the MLP model and the activation function in MLP(0) is linear, the parameter estimates differ from the weights estimated for the GLRM model. Such a case is presented in Table 8, which contains parameter estimates for Canada applying the general linear model (GLRM) and perceptron with no hidden layers MLP(0) and linear activation function. The parameter estimates for both models essentially differ while the fitting statistics, RMSE, MAE, and the values of the objective functions, are the same. Also, in order to test

the sensitivity of the results, the period of the analysis is broken into different sub-periods. The results for the United States are detailed in Appendix 1.

Tables 10 and 11 present the RMSE, MAE, and objective function statistics based on the regression model, GLRM, MLP(2) and MLP(5).

Comparing RMSE estimates for the regression model containing 89 explanatory variables to the one obtained for the GLRM model that contains significant variables only, it can be noticed that both models are not significantly different from one another. The variations of RMSE for the GLRM and MLP models are visible, though the difference among these models are more visible if we compare MAE and values of the objective function criteria. Thus, the multilayer perceptron models with logistic activation functions predict daily stock returns better than traditional OLS and GLRM models.

Furthermore, the multilayer perceptron with five units in the hidden layer better predicts the stock indices for USA, France, Germany, UK and World than the neural network with two hidden elements. This can be seen by examining all the fitness statistics for MLP(5), which are smaller than those for MLP(2). Only MAE estimated for Canada and Japan in the MLP(5) is higher than for MLP(2).

6. Conclusion

This paper applies ordinary least squares, general linear regression, and artificial neural network models, multi-layer perceptron models, in order to investigate the dynamic interrelations of major world stock markets. The Multi-Layer Perceptron models contain one hidden layer with two and five processing elements and logistic activation. The data base consists of daily stock market indices of the following countries: Canada, France, Germany, Japan, United Kingdom, the United States, and the world excluding US. Based on the criteria of Root Mean Square Error, Maximum Absolute Error, and the value of the objective function, the models are compared to eachother.

It is found that the neural network consisting of multilayer perceptron models with logistic activation functions predict daily stock returns better than the traditional ordinary least squares and general linear regression models. Furthermore, it is found that a multilayer perceptron with five units in

the hidden layer better predicts the stock indices for USA, France, Germany, UK and World than a neural network with two hidden elements.

This paper lends support in favour of using neural network models in the study of finance, in particular in the area of international transmission of returns in stock markets. The returns for applying neural network models are positive. Consequently, the results of this paper favor the increased use of these model by practicioners like Goldman Sachs, Morgan Stanley, and Fidelity Investments as alternative or additional tools for financial analysis.

Notes

- 1. Experimental Alpha releases SAS 6.09 and 6.11, 6.12 and 6.13 Systems are used.
- 2. For example, in the US model D* the parameter estimate for the trend variable equals 0.0000 and t-statistic equals 0.2587. The insignificance of the T variable (for the USA) can be noticed in Table 2.

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Model	Number of	Adj. R ²	RMSE	Significant V	Variables				
	Explanatory Variables			CANADA	FRANCE	GERMANY	JAPAN	UK	USA
A (1-3)	17	0.4545	0.0063	LC3	LF2			LU2	LS1, LS2, LS3
B (2-5)	24	0.1162	0.008	LC3, LC5		LG2			LS2, LS3, LS4, LS5
C(1-5)	29	0.4593	0.0062	LC5	LF2			LU2, LU5	LS1, LS2, LS3, LS5
D(1-7)	41	0.4601	0.0062	LC5	LF2, LF6			LU2	LS1, LS2, LS3, LS4, LS5
E(1-15)	89	0.4975	0.006	LC2, LC5, LC14	LF2,LF6, LF8, LF10		LJ8, LJ9, LJ12,LJ13 LJ14,LJ15	LU2, LU8, LU10	LS1, LS2, LS3,LS4, LS5, LS8, LS10, LS14

Table 1. Regression Analysis for CANADA

Table 2. Regression Analysis for FRANCE

Model	Number of	Adj. R ²	RMSE	Significant V	E Significant Variables						
	Explanatory			CANADA	FRANCE	GERMANY	JAPAN	UK	USA		
	Variables										
A(1-3)	17	0.4943	0.0086	LC3		LG1, LG2	LJ3	LU1	LS2, LS3		
B (2-5)	24	0.1501	0.0111	LC2				LU5	LS2, LS3		
C (1-5)	29	0.4958	0.0086			LG1, LG2		LU1	LS2, LS3		
D (1-7)	41	0.4989	0.0085		LF7	LG1, LG2		LU1 LU7	LS2, LS3		
E (1-15)	89	0.5138	0.0084	LC3, LC9,	LF7	LG1, LG2,	LJ11, LJ14	LU1, LU7	LS2, LS3,		
				LC11		LG8			LS9, LS10		

 Table 3.
 Regression Analysis for GERMANY

Model	Number of	Adj. R ²	RMSE	Significant V	/ariables				
	Explanatory Variables			CANADA	FRANCE	GERMANY	JAPAN	UK	USA
A (1-3)	17	0.4323	0.0124	LC3	LF1, LF2	LG2	LJ1	LU1	LS3
B (2-5)	24	0.1627	0.0102	LC2, LC3	LF2	LG2		LU4, U5	LS2, S3,LS4, LS5
C (1-5)	29	0.4372	0.0101	LC3	LF1, LF2	LG2	LJ1	LU1, LU5	LS3,LS4
D (1-7)	41	0.4393	0.0101	LC3	LF1, LF2, LF7	LG2	LJ1	LU1, LU5	LS3, LS4
E (1-15)	89	0.4399	0.0101	LC3	LF1, LF2,LF7	LG2	LJ10	LU1	LS3, LS4, LS8, LS10

Table 4. Regression Analysis for JAPAN

Model	Number of	Adj. R ²	RMSE	Significant V	Significant Variables					
	Explanatory Variables			CANADA	FRANCE	GERMANY	JAPAN	UK	USA	
A (1-3)	17	0.1718	0.0138	LC2, LC3	LF3	LG1, LG2, LG3		LU2		
B (2-5)	24	0.1848	0.0137	LC2		LG2, LG3		LU2, LU5	LS4	
C (1-5)	29	0.1858	0.0137	LC2		LG1, LG2, LG3		LU2, LU5	LS4	
D (1-7)	41	0.1848	0.0137	LC2		LG1, LG2		LU2, LU5	LS4	
E (1-15)	89	0.1999	0.0136	LC2		LG2, LG10, L12,L G15	LJ9, LJ10, LJ11, LJ15	LU2,LU5, LU13	LS4	

Model	Number of	Adj. R ²	RMSE	Significant V	/ariables				
	Explanatory Variables			CANADA	FRANCE	GERMANY	JAPAN	UK	USA
A (1-3)	17	0.4171	0.0087	LC2, LC3	LF1, LF2, LF3	LG1	LJ2	LU2	LS2, LS3
B (2-5)	24	0.2354	0.0100	LC2, LC3	LF2, LF3			LU2	LS2, LS3, LS4
C (1-5)	29	0.4204	0.0087	LC2, LC3	LF1, LF2, LF3	LG1		LU2	LS2, LS3, LS4
D (1-7)	41	0.4239	0.0087	LC2, LC3	LF1, LF2, LF3	LG1		LU2, LU5	LS2, LS3, LS4
E (1-15)	89	0.4324	0.0086	LC2, LC3	LF1, LF2, LF3	LG1	LJ7, LJ8, LJ15	LU2, LU9	LS2, LS3, LS4,LS6

Table 5. Regression Analysis for UK

Table 6. Regression Analysis for USA

Model	Number of	Adj. R^2	RMSE	Significant V	/ariables				
	Explanatory Variables			CANADA	FRANCE	GERMANY	JAPAN	UK	USA
A (1-3)	17	0.4124	0.0079	LC1, LC2	LF2	LG3			LS2
B (2-5)	24	0.0288	0.0102	LC2, LC3, LC4, LC5	LF2	LG2			LS2, LS3, LS5
C (1-5)	29	0.4136	0.0079	LC1, LC2	LF2	LG5			LS2
D (1-7)	41	0.4140	0.0079	LC1, LC2, LC6	LF2			LU7	LS2
D*(1-7)	42	0.4145	0.0079	LC1, LC2, LC6	LF2			LU7	LS2
E (1-15)	89	0.4482	0.0077	LC1, LC2	LF2	LG14	LJ8, LJ9, LJ12, LJ13, LJ14	LU7, LU8	

Table 7. Regression Analysis for WORLD

Model	Number of	Adj. R ²	RMSE	Significant Varia	ables				
	Explanatory			CANADA	FRANCE	GERMANY	JAPAN	UK	WORLD
	Varariables								
A (1-3)	17	0.1886	0.0091	LC1, LC2, C3	LF1, LF3	LG2	LJ1, LJ3		LW3
B (2-5)	24	0.0490	0.0099	LC2, LC3	LF1		LJ4		
C (1-5)	29	0.1883	0.0091	LC1, LC2, C3	LF1, LF3	LG2	LJ1, LJ4		LW3
D (1-7)	41	0.1896	0.0091	LC1, LC2, C3	LF1, LF3	LG2	LJ1		LW3
E (1-15)	89	0.2081	0.0090	LC1, LC2, C3	LF1, LF3	LG2, LG7	LJ1, LJ10, LJ12,	LU14	LW3
							LJ13, LJ14		

Table 8. Comparison of Parameter Estimates for Canada Obtained for the Model Defined as General Linear Model and the Multilayer Perceptron with No Hidden Layers with Linear Activitation Function.

Name of	Parameter	Estimates	Name of	Parameter	Estimates
Variable	GLRM	MLP (0)	Variable	GLRM	MLP (0)
Intercerpt	-0.0072	0.0092	LJ8	-2.9943	-0.0456
LC2	6.4658	0.0548	LJ9	2.2191	0.0338
LC5	12.7007	0.1077	LJ12	3.5066	0.0534
LC14	-7.0775	-0.0601	LJ13	-5.1498	-0.0784
LS1	50.4093	0.5233	LJ14	6.1927	0.0943
LS2	14.3979	0.1495	LJ15	-2.7559	-0.0420
LS3	-2.6777	-0.0278	LU1	-0.4169	-0.0048
LS4	5.4651	0.0567	LU2	3.6658	0.0420
LS5	-5.7831	-0.0600	LU3	1.1134	-0.0128
LS8	3.2992	0.0342	LU4	2.2438	0.0257
LS10	-3.5250	-0.0366	LU5	-0.6311	-0.0722
LS14	4.7867	0.0497	LU8	-3.7207	-0.0426
LF2	-4.3135	-0.0520	LU10	3.9289	0.0450
LF6	1.9017	0.0229	RMSE	0.6014	0.6014
LF8	4.6419	0.0560	MAE	5.9170	5.9170
LF10	-2.2179	0.0268	Objective func.	3.6510	3.6510

In Table 8 all parameters were multiplied by 100 since all parameters were very small.

	Regression Model		GLRM Model	
Variable	Estimates	t-Statistic	Estimates	T-Statistic
Intercept	0.0001	0.4485	0.0001	0.62
LC1	0.4090	16.0784	0.4220	17.45
LC2	0.1254	4.4554	0.1307	5.12
LC3	-0.0773	-2.7422	-0.0813	-3.05
LW3	0.1373	2.5867	0.0917	2.13
LF1	0.1060	4.4077	0.1054	5.97
LF2	0.0569	2.3007	0.0370	2.19
LG2	-0.0474	-2.2434	-0.0483	-2.53
LG7	0.0458	2.1643	0.0213	1.43
LJ1	-0.0796	-3.0085	-0.0582	-2.46
LJ10	-0.0651	-2.4413	-0.0027	-0.21
LJ12	-0.0652	-2.4233	-0.0144	-1.08
LJ13	0.1231	-4.6346	-0.0629	-4.48
LJ14	0.0528	3.4979	0.0516	3.85
LU14	-0.0539	-2.0314	0.0088	0.47
RMSE	0.0090		0.0091	

Table 9. Comparison of the Regression Model (with 89 Explanatory Variables) to the General Linear Regression Model (GLRM) (with 14 Explanatory Variables)

Regression	model				ANN – GLRM	1		
Country	Num. of Estimated Parameters	R ²	Adj. R ²	RMSE	Num. of Estimated Parameters	RMSE	MAE	Obj. f.
USA	90	0.4722	0.4482	0.0077	12	0.0077	0.1205	0.061
Canada	90	0.5194	0.4975	0.0060	25	0.0060	0.0593	0.037
France	90	0.5350	0.5138	0.0084	16	0.0084	0.0447	0.072
Germany	90	0.4642	0.4399	0.0101	12	0.0101	0.0762	0.103
U. K.	90	0.4570	0.4324	0.0086	16	0.0087	0.0717	0.072
Japan	90	0.2347	0.1999	0.0136	14	0.0137	0.1656	0.191
World	90	0.2425	0.2081	0.0090	15	0.0091	0.0656	0.083

Table 10. Comparison of Fitness Statistics for the Linear Regression and General Linear Regression Models

Table 11. Comparison of Fitness Statistics for Multilayer Perceptron Models with Two and Five Elements in the Hidden Layer.

ANN – MLF	P (2)				ANN - ML	P (5)		
Country	Num. of	RMSE	MAE	Obj. f.	Num. of	RMSE	MAE	Obj. f.
	est. par.				est. par.			
USA	27	0.0069	0.0419	0.0478	66	0.0066	0.0407	0.044
Canada	53	0.0055	0.0281	0.0307	131	0.0054	0.0287	0.028
France	35	0.0082	0.0390	0.0674	86	0.0080	0.0361	0.063
Germany	27	0.0100	0.0681	0.1020	66	0.0093	0.0505	0.085
U. K.	35	0.0083	0.0578	0.0698	86	0.0081	0.0517	0.065
Japan	31	0.0133	0.1626	0.1796	76	0.0131	0.1758	0.169
World	33	0.0087	0.0655	0.0762	81	0.0085	0.066	0.072

Appendix 1

Based on plotting the data, a few sub-periods are considered. The three following models are tested for the sub-periods:

Model 1.

lusa(1) = f[lcan(1), lcan(2), lfra(1), lfra(2), lger(1), lger(2), ljap(1), ljap(2), luk(1), luk(2), In lusa(2), lusa(3)]

where: f - linear,

lusa(1)= $ly^{j}(L)$ for the USA, L = 1 from relation (7) as follows:

(7)
$$ly^{j}(L) = \log[y^{j}(L)] - \log[y^{j}(L-1)]; \text{ for } j = 0, 1, ..., 6;$$

L = 1, 2, 3

where:

j - the index of each country (USA, Canada, France, Germany, UK or Japan) or "world" (i. e. world without USA),

L - the lag index,

 $y^{j}(L)$ - daily stock returns in j-th country lagged by L periods.

Model 2

lusa(1) = f[lcan(1), lcan(2), lfra(1), lfra(2), lger(1), lger(2), ljap(1), ljap(2), luk(1), luk(2)]

where f is linear activation.

Model 3

lusa(1)= f[lcan(2), lcan(3), lfra(2), lfra(3), lger(2), lger(3), ljap(2), ljap(3), luk(2), luk(3), lusa(2), lusa(3)]

where f is linear or logistic activation.

The statistic MASE is not presented in Tables A1-A3 as it depends on the number of observations, which are different for each of the experiments. The Tables show that the errors are different for different periods. The highest RMSE is obtained for relatively short periods of time. Thus, although the errors are changed in different periods, the results are consistent with the ones reported in the paper. Tables A1-A3 correspond to Models 1-3, respectively, as follows:

Table A1 - Model 1

Obs. Period	Numb. Of obs.	Min. value	Max. value	Mean	Stand. Deviation	MAE	RASE
01/03/87-11/28/94	2060	-0.22	0.08	0.0002	0.0104	0.15	0.0079
01/03/87-11/28/94	2000	-0.22	0.08	3	0.0104	0.15	0.0079
01/03/87-11/28/94	2044	-0.04	0.03	0.0003	0.0080	0.06	0.0067
01/03/87-11/28/94	2038	-0.03	0.03	0.0004	0.0078	0.06	0.0065
01/03/87-11/28/94	1673	-0.01	0.01	0.0003	0.0046	0.01	0.0042
12/24/91-11/28/94	765	-0.027	0.02	0.0002	0.006	0.02	0.0051
12/24/93-11/28/94	464	-0.02	0.02	0.0002	0.006	0.02	0.0050
11/15/90-02/17/93	327	-0.04	0.03	0.0004	0.007	0.03	0.0060
06/01/88-08/04/89	308	-0.02	0.02	0.0010	0.008	0.02	0.0058
12/24/91-02/17/93	300	-0.02	0.02	0.0005	0.006	0.02	0.0055
01/15/90-01/16/91	263	-0.04	0.03	0.0006	0.010	0.04	0.0076
01/06/87-10/16/87	204	-0.04	0.03	0.0004	0.010	0.03	0.0076

Table A2 - Model 2

Obs. Period	Numb.	Min.	Max.	Mean	Stand.	MAE	RASE
	Of obs.	value	value		Deviation		
01/03/87 -	2038	-0.03	0.03	0.0004	0.0078	0.07	0.0066
11/28/94							
01/03/87-11/28/94	1673	-0.01	0.01	0.0003	0.0046	0.01	0.0042

Table A3 - Model 3

Obs. Period	Activation	Numb.	Min.	Max.	Mean	Stand.	MAE	RASE
	function	of obs.	value	value		Deviation		
01/03/87-	Linear	2060	-0.22	0.08	0.00023	0.0104	0.22	0.0010
11/28/94								
01/03/87-	Logistic	2060	-0.22	0.08	0.00023	0.0104	0.23	0.0010
11/28/94								
01/03/87-	Linear	2038	-0.03	0.03	0.0004	0.0078	0.03	0.0078
11/28/94								